

*Planck* launch, 14 May 2009  
ESA Spaceport, French Guyana



# The CMB

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TIARA Winter School  
AS/NTU, Taipei  
February 2014

# Outline

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- What is the CMB?
  - Why is it the best cosmological probe (so far)?
  - What can we learn from it?
- State of the art
  - Planck — CMB intensity
    - primary fluctuations and lensing
  - Suborbital experiments
    - polarization – lensing
- The future:
  - highly sensitive polarization measurements from Planck and suborbital experiments



planck



DTU Space  
National Space Institute



Science & Technology  
Facilities Council



National Research Council of Italy



Deutsches Zentrum  
für Luft- und Raumfahrt e.V.



UNIVERSITY OF  
CAMBRIDGE



IN2P3  
Les deux Infinis



Infrared Processing  
and Analysis Center



Imperial College  
London



UNIVERSITÀ DEGLI STUDI  
DI MILANO



JPL



LERMA



MilliLab

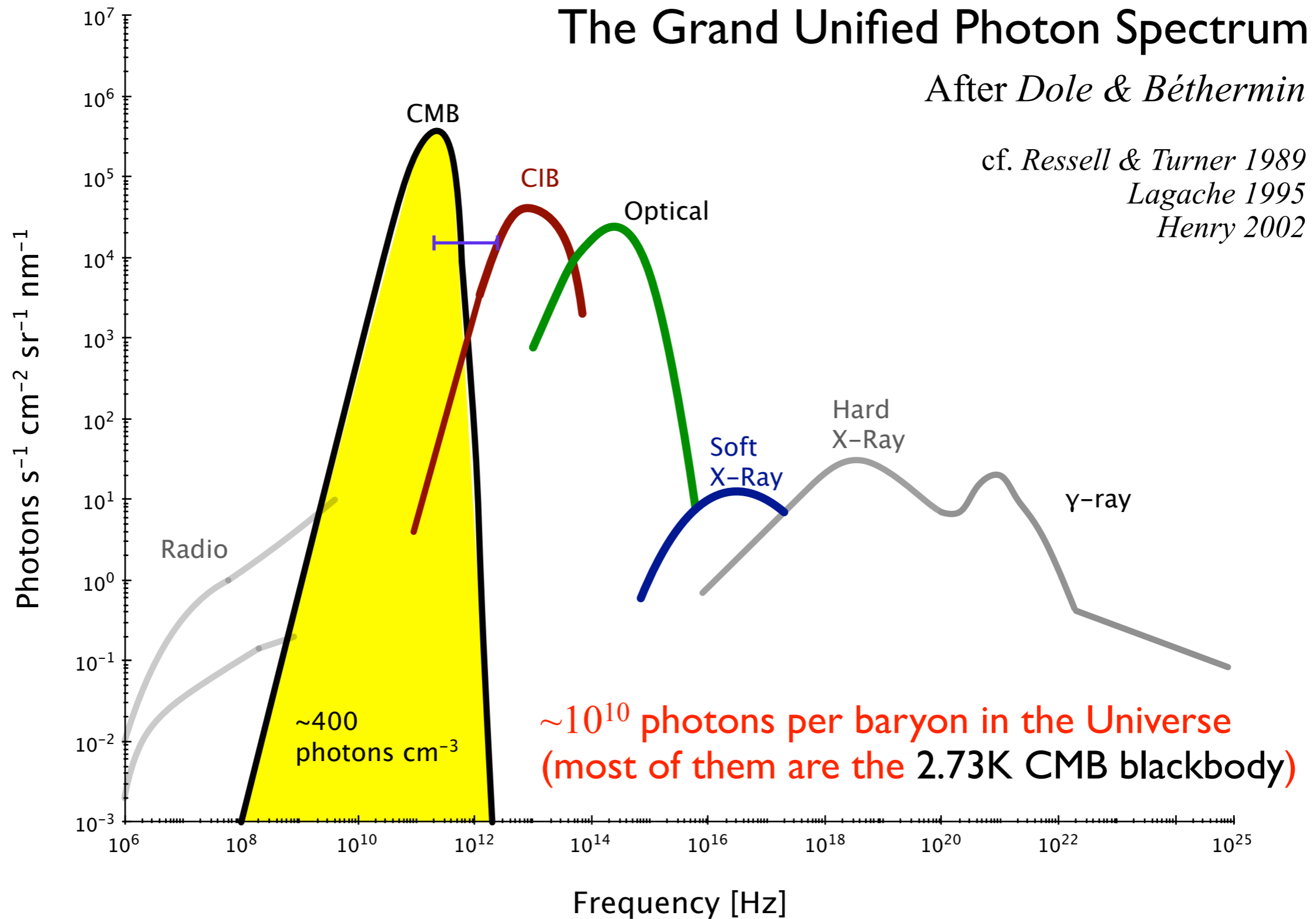


US  
University of Science



Parts of this talk based on data and ~30 papers  
released March 2013 by the 400-person Planck Collaboration

# Light from the Universe



# A standard cosmological model?

$$ds^2 = c^2 dt^2 - a^2(t) \left[ \frac{dr^2}{1 - kr^2} + r^2 d\theta^2 + r^2 \sin^2 \theta d\phi^2 \right]$$

Relativity

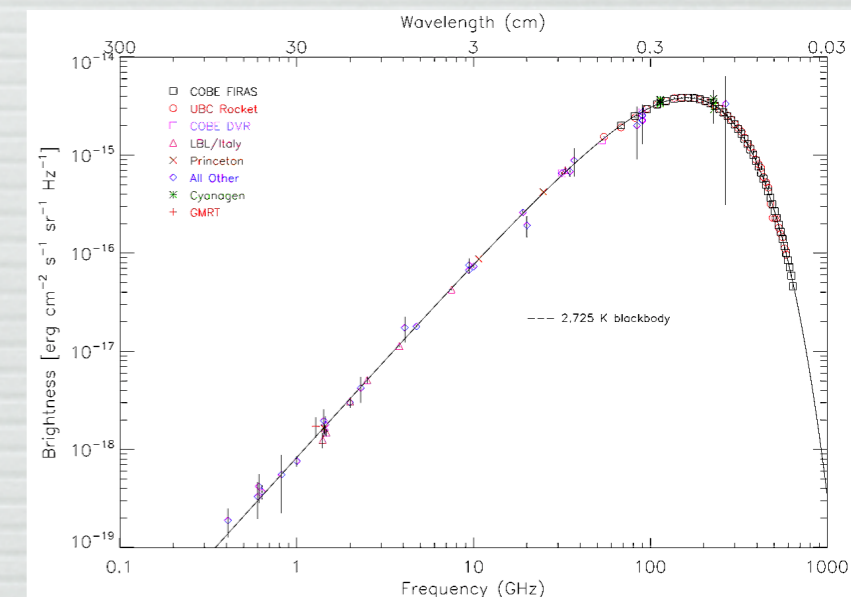
- Predictions: (“pillars of the Big Bang”)
  - Expansion (Hubble)
  - Hot big bang
  - Light element abundances (BBN)
  - Recombination (CMB)

## □ The Hot Big Bang:

- Expansion, cooling from a hot, dense early state
- radiation  $\Rightarrow$  matter (*baryogenesis*)
- quarks  $\Rightarrow$  protons & neutrons
- protons & neutrons  $\Rightarrow$  nuclei (*Big Bang Nucleosynthesis — BBN*)
- nuclei & electrons  $\Rightarrow$  atoms (*Cosmic Microwave Background — CMB*)

## □ Parameters:

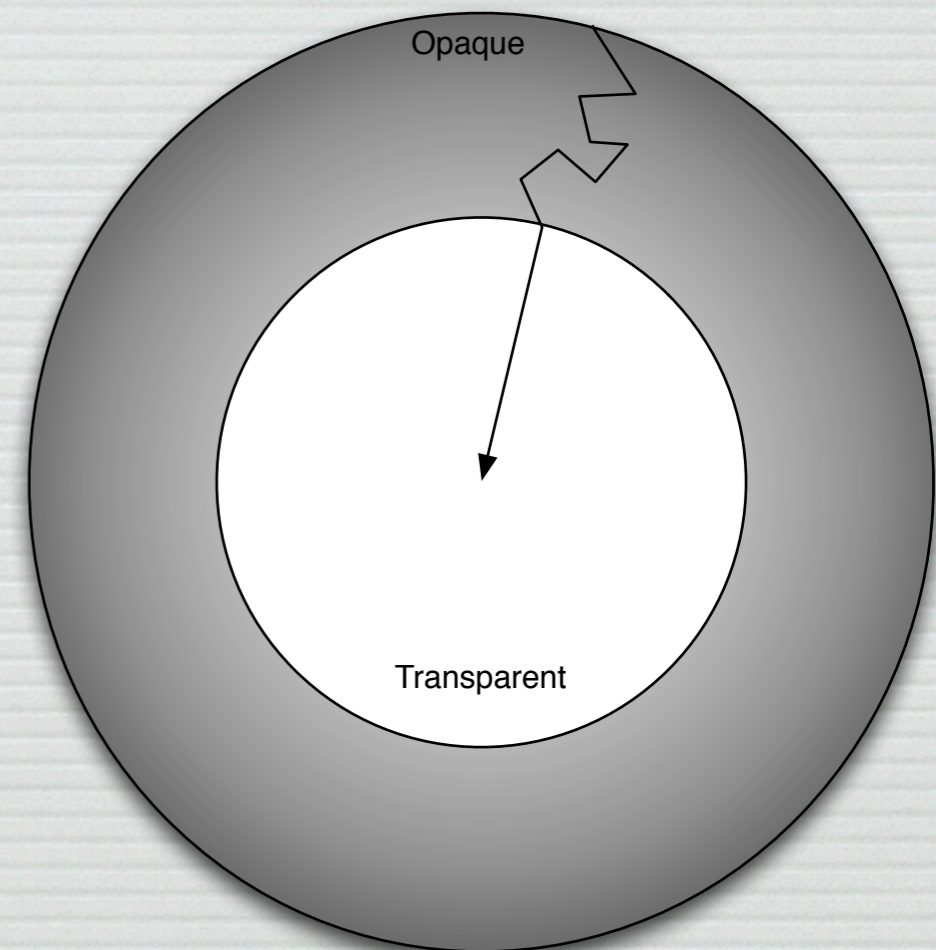
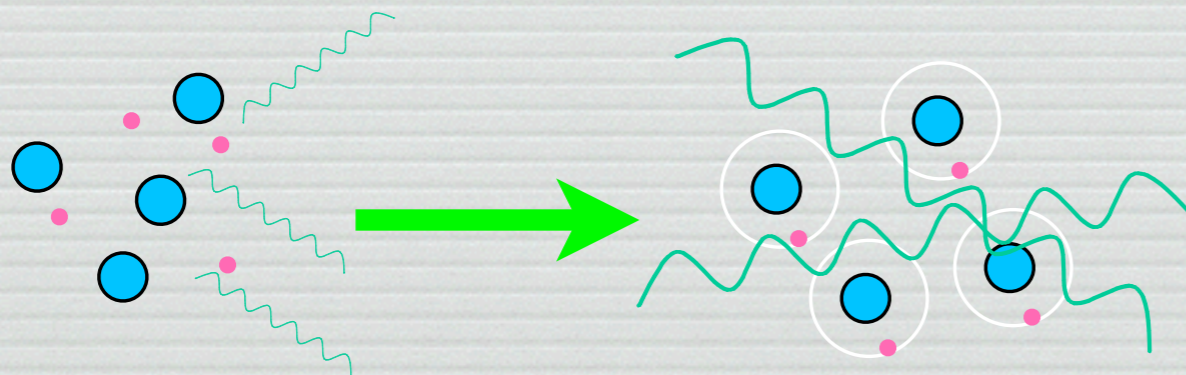
- density of radiation  $\Omega_r$ , baryons  $\Omega_b$ , dark matter  $\Omega_c$ , dark energy  $\Omega_\Lambda$
- Age  $t_0$ , expansion rate  $H_0$
- Curvature:  $\Omega_k$  (=0?)



Also fluctuations—departures from uniformity—needed to form structure

# Evidence & Observations: Cosmic Microwave Background

- 400,000 years after the Big Bang, the temperature of the Universe was  $T \sim 3,000$  K
- Hot enough to keep hydrogen atoms *ionized* until this time
  - *proton + electron* → *Hydrogen + photon* [ $p^+ + e^- \rightarrow H + \gamma$ ]
  - *charged plasma* → *neutral gas*
- depends on *entropy* of the Universe
- Photons (light) can't travel far in the presence of charged particles
  - *Opaque* → *transparent*

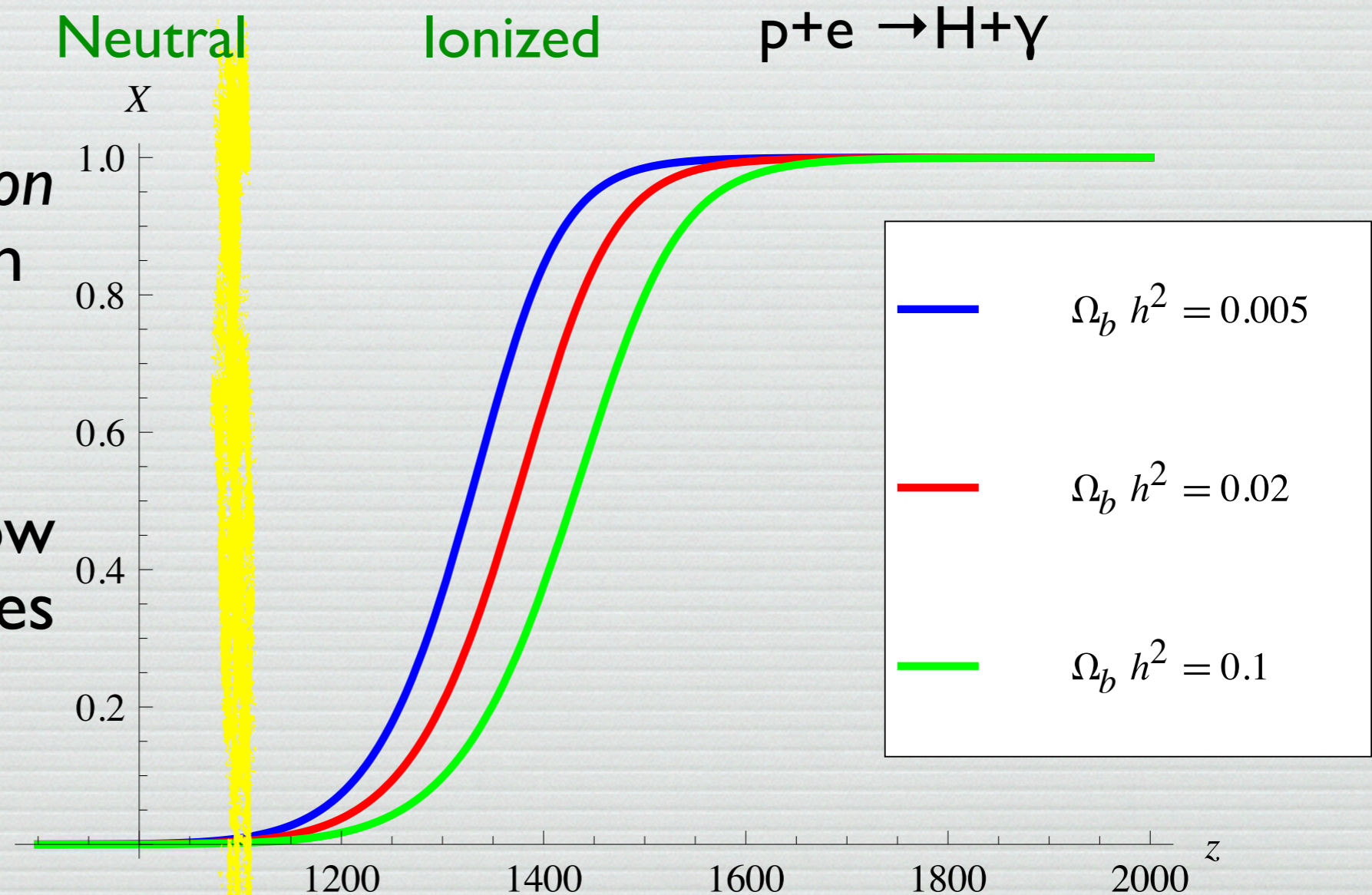


# Ionization fraction: Equilibrium

- large value of  $\eta = n_b/n_\gamma \cong 10^{-9}$  key to “delay” to  $kT \sim 0.6 \text{ eV} \ll 13.6 \text{ eV}$

- Solve *Saha Equation* equilibrium ioniz'n balance

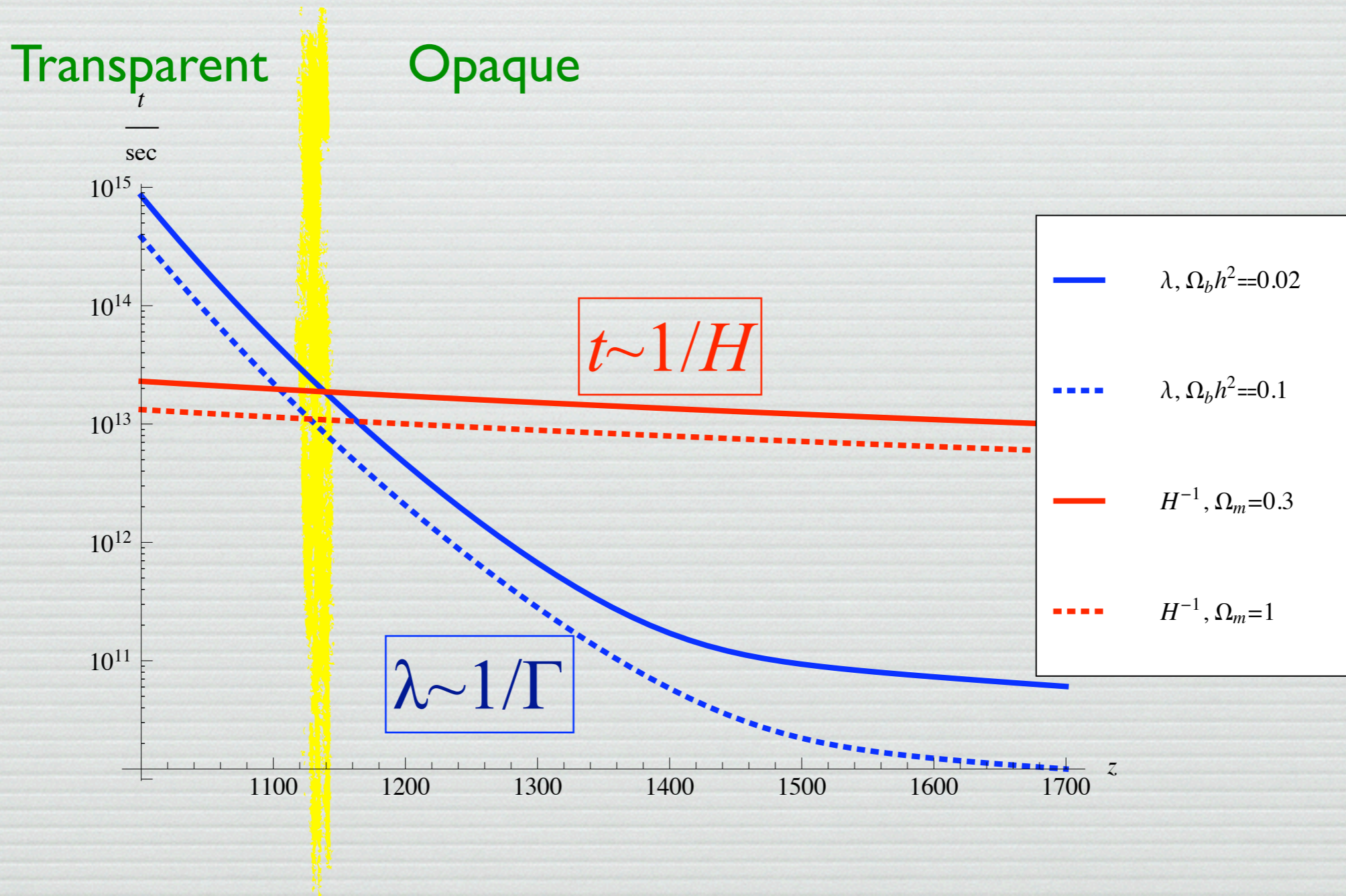
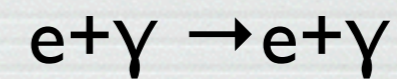
- really should follow many levels, species



Not shown: interaction falls out of equilibrium and freezes out:  $X \sim 10^{-4}$

# Photon Decoupling

Freeze-out when  $\Gamma < H$

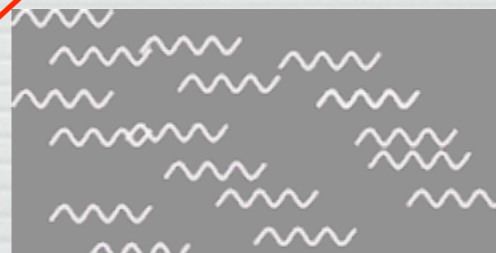
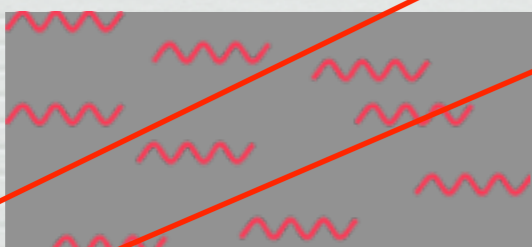


# What affects the CMB temperature?

$$\frac{\Delta T}{T}(\hat{x}) \simeq \frac{1}{4} \frac{\delta \rho_\gamma}{\rho_\gamma} + \mathbf{v} \cdot \hat{x} + \int_{\eta_{rec}}^{\eta_0} d\eta \dot{h}_{ij} \hat{x}_i \hat{x}_j$$

- Initial temperature (density) of the photons

Cooler



Hotter

- Doppler shift due to movement of baryon-photon plasma
- Gravitational red/blue-shift as photons climb out of potential wells or fall off of underdensities



- Photon path from LSS to today
- All linked by initial conditions  $\Rightarrow 10^{-5}$  fluctuations

# The horizon at last scattering

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- Particle (light) horizon at last scattering, corresponding to about  $1^\circ$  on the sky
  - $d_A = D/\theta = a_e r_e = a_o r_e (a_e/a_o) = a_o r_e / (1+z)$  for  $D = d_H$
  - so  $\theta = D/d_A$
- But fluctuations in the CMB are *sound waves*, so

$$d_{\text{sound}} = \frac{1}{H_0(1+z)} \int_z^\infty \frac{dz' c_s}{E(z')}$$

for  $c_s \approx c/\sqrt{3}$  (mostly radiation):

- $d_{\text{sound}} \approx d_H/\sqrt{3}$

# Large scales: the Sachs-Wolfe effect

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- Outside the horizon (greater than a degree)
  - velocity term is negligible
  - metric (potential) term looks like

$$\int_{\text{rec}}^{t_0} dt \dot{\phi} \simeq \phi_{\text{rec}} - \phi_0$$

- $\phi \simeq \text{const}$  for linear evolution in a flat MD universe
- Further, the *potential* is related to the *density* term, so

$$\frac{\Delta T}{T} = \phi_{\text{rec}} - \frac{2}{3}\phi_{\text{rec}} = \frac{1}{3}\phi_{\text{rec}}$$

- “Integrated Sachs-Wolfe effect” occurs when  $\phi$  varies (e.g., nonlinear evolution,  $\Lambda$ , changing eq. of state)

# Oscillations in primordial plasma: Acoustic Peaks

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- Before **recombination**, a tightly-coupled plasma of matter ( $p, e$ ) and photons
- Primordial/inflationary **perturbations on all scales**—can only collapse when in causal contact
- **Pressure** determined by mix of baryons and radiation ( $\sim 10^{10}$  photons/baryon!): baryon “doping” lowers  $c_s$  from  $1/\sqrt{3}$ .
- Higher  $\Omega_b$  decreases rebound force; lowers 2<sup>nd</sup> peak relative to first
- At smaller scales, imperfect coupling between baryons and photons — Silk **damping**

# The CMB transfer function

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$$C_\ell = \int P_i(k) T_\ell^2(k) dk$$

- compare density spectrum:  $P(k) = P_i(k) T^2(k)$
- The transfer function depends on the “cosmological parameters”. For example:
  - matter density—determines sound speed in baryon/ photon fluid
  - curvature—determines angular-diameter distance to horizon
  
- Actually solve **Boltzmann Equation** over thickness of Last-Scattering surface – e.g., CMBFAST, CAMB

# CMB Statistics

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$z \sim 1300$ :  $p+e \rightarrow H$  & Universe becomes transparent.

$$\frac{T(\hat{x}) - \bar{T}}{\bar{T}} \equiv \frac{\Delta T}{T}(\hat{x}) = \sum_{\ell m} a_{\ell m} Y_{\ell m}(\hat{x})$$

i.e., Fourier Transform, but on a sphere

Determined by **temperature**, **velocity** and **metric** on the **last scattering surface**.

**Power Spectrum:**

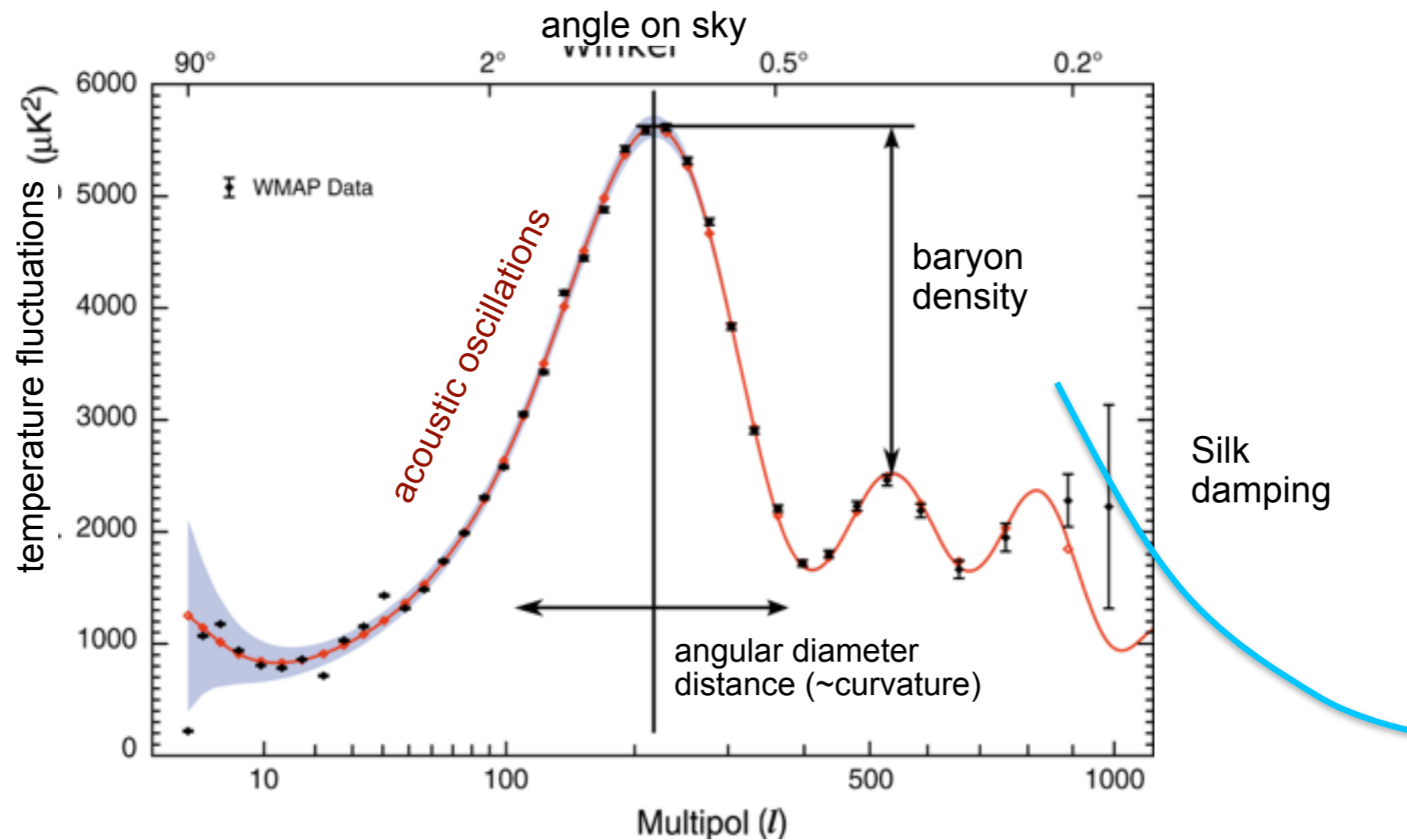
$$\langle a_{\ell m}^* a_{\ell' m'} \rangle = \delta_{\ell \ell'} \delta_{m m'} C_{\ell}$$

Multipole  $\ell \sim$  angular scale  $180^\circ/\ell$

For a **Gaussian** theory,  $C_{\ell}$  completely determines the statistics of the temperature.

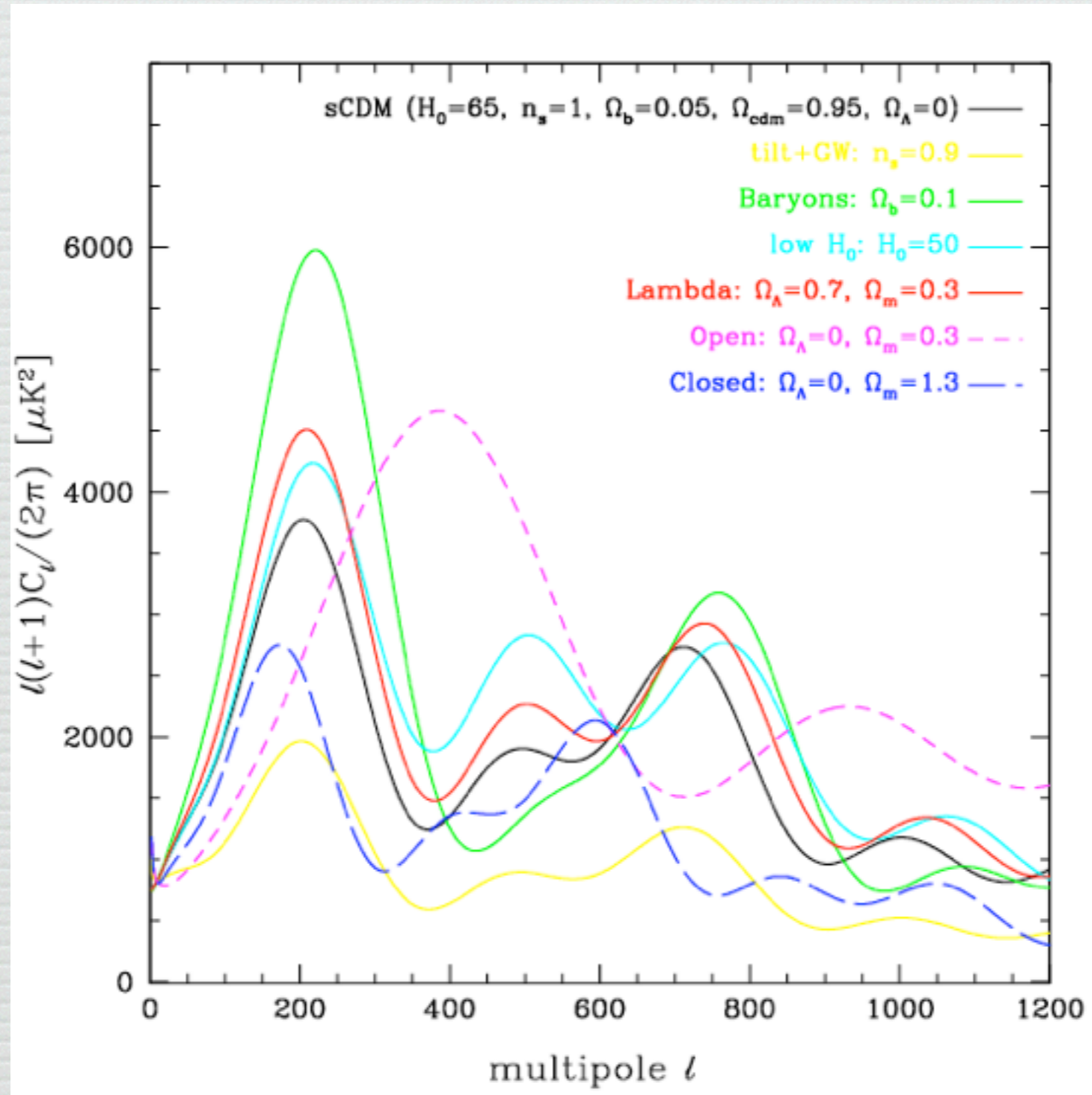
# Physics of the CMB power spectrum

Gravity + plasma physics modulates initial spectrum of fluctuations (from, e.g., inflation)



# Theoretical Predictions

Mean square fluctuation amplitude

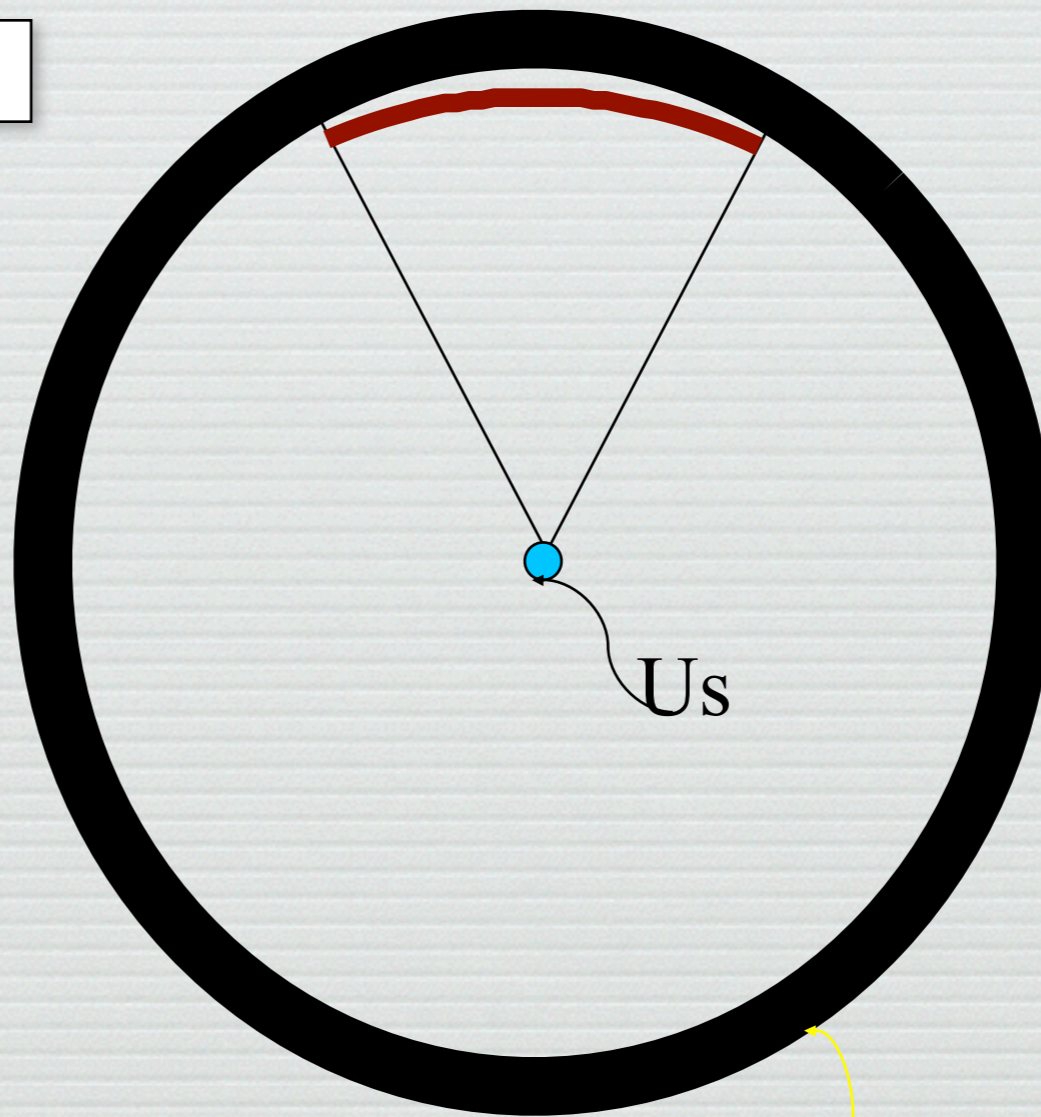


$\sim 180^\circ$ /Angular scale

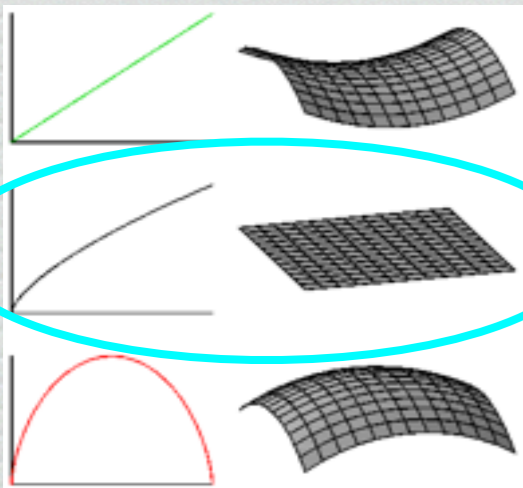
# Measuring Curvature with the CMB

Flat

$\Omega=1$



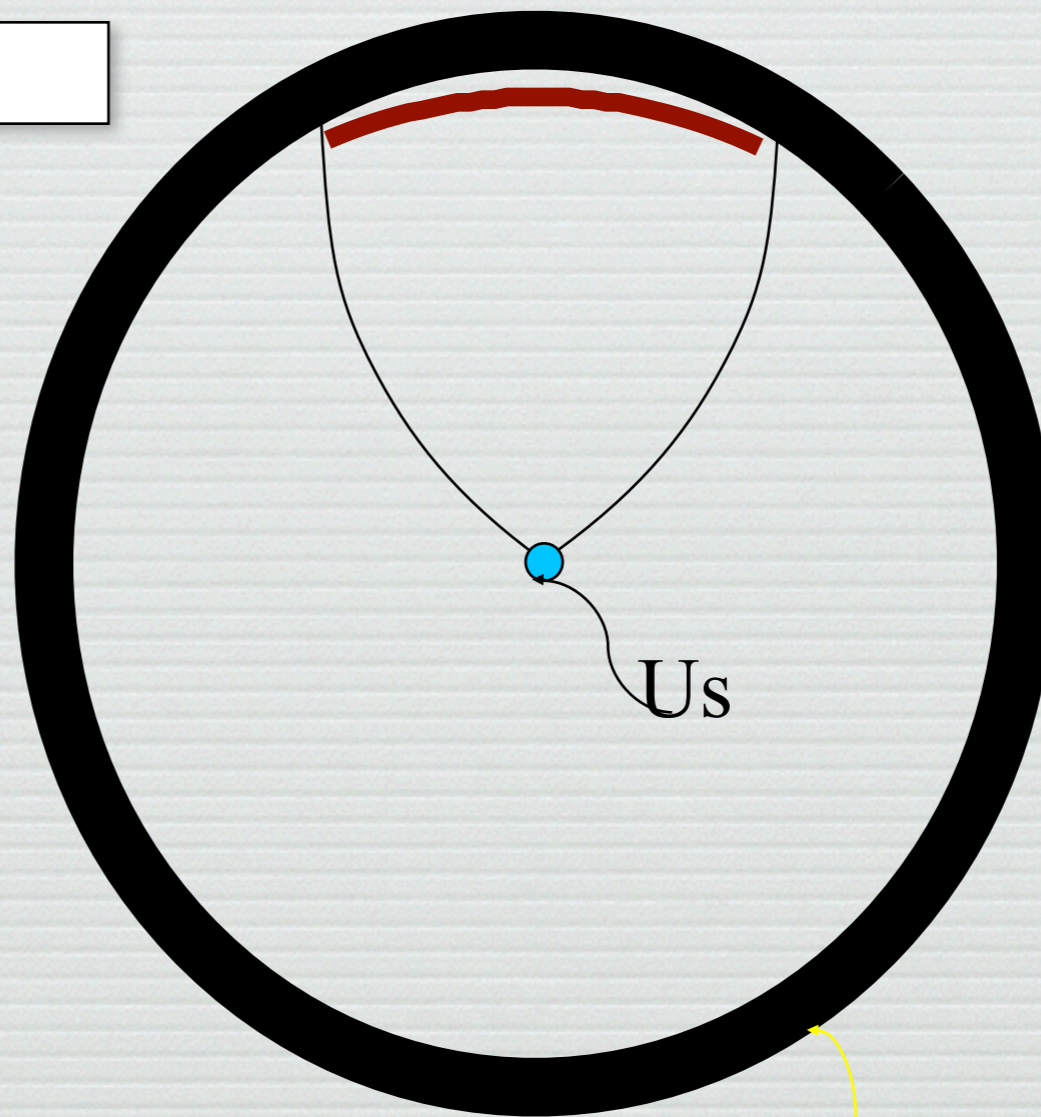
Last Scattering



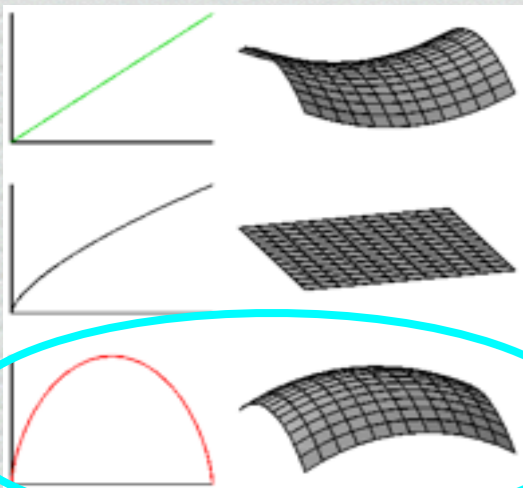
# Measuring Curvature with the CMB

Closed

$\Omega > 1$



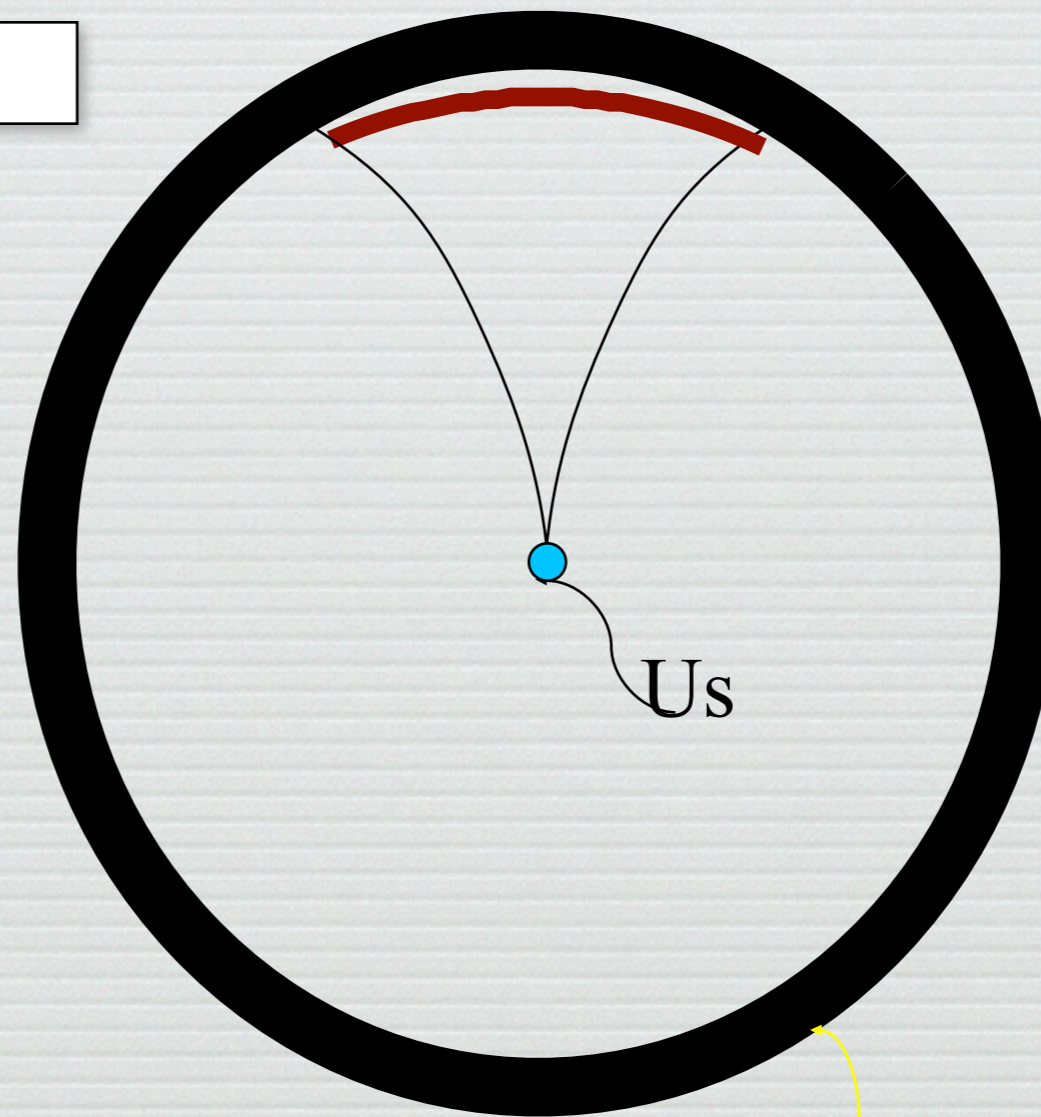
Last Scattering



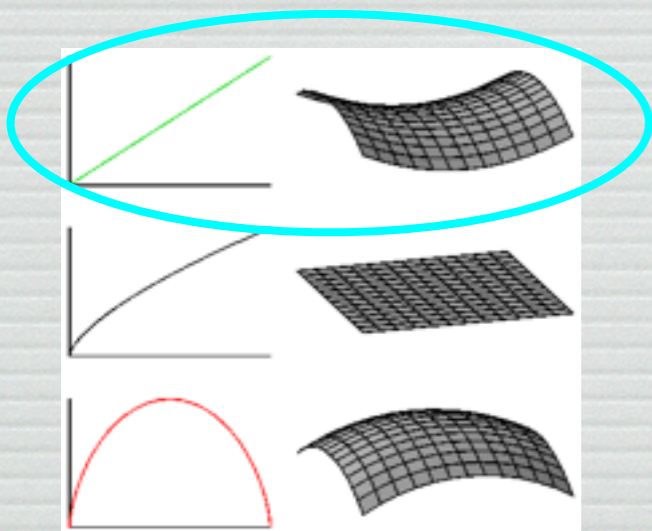
# Measuring Curvature with the CMB

Open

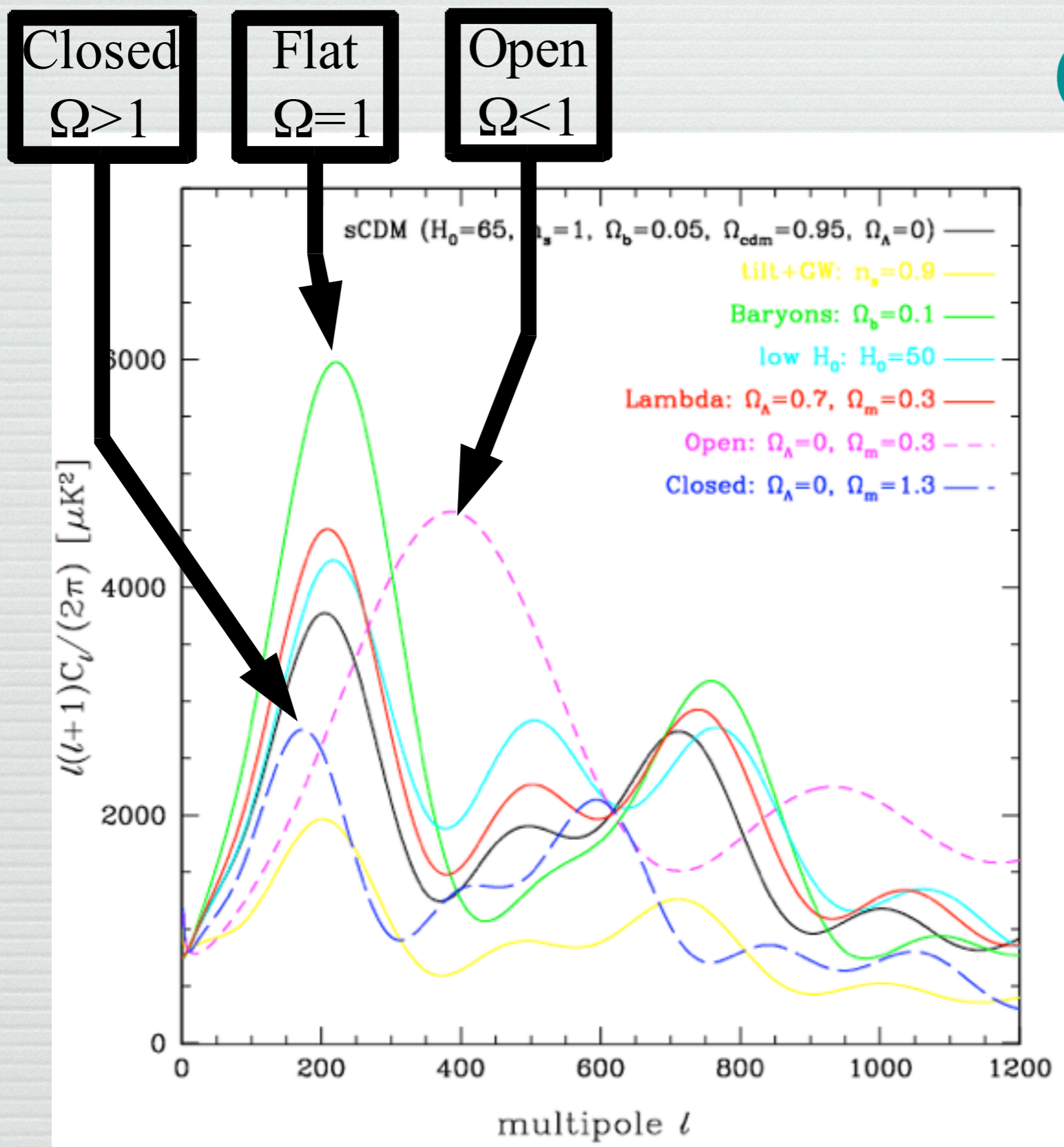
$\Omega < 1$



Last Scattering



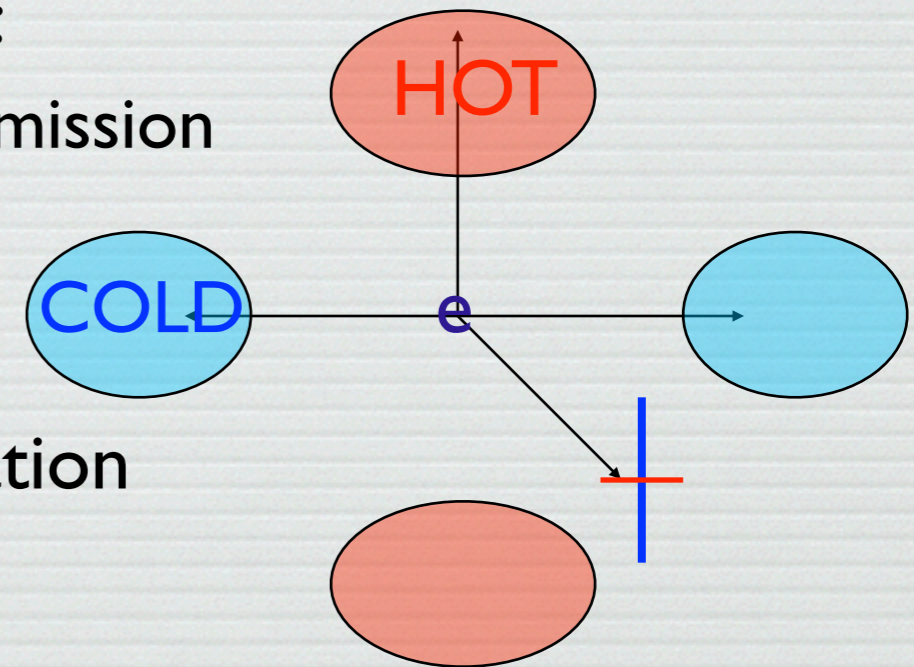
# CMB Power Spectrum



- Model CMB as a **2d stationary Gaussian Random Field** on the sphere
- Motivated by physics, confirmed by observation
  - (linear transform of underlying 3d process)

# CMB Polarization: Generation

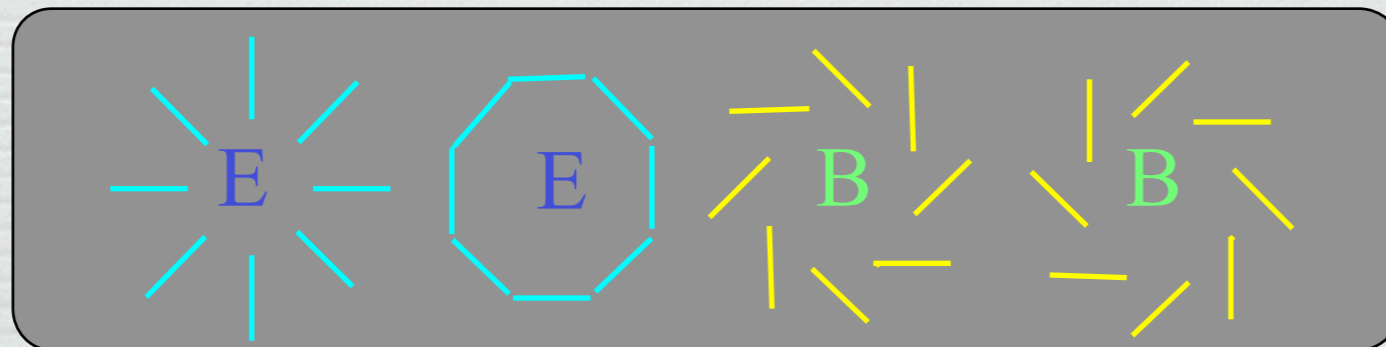
- **Ionized** plasma + **quadrupole** radiation field:
  - Thomson scattering  $\Rightarrow$  [linearly] **polarized** emission



- Unlike intensity, only generated when ionization fraction,  $0 < x < 1$  (i.e., during transition)
- **Scalar** perturbations: traces  $\sim$  gradient of velocity
  - same initial conditions as temperature and density fluctuations
- **Tensor** perturbations: independent of density fluctuations
  - +, × patterns of quadrupoles (impossible to form via linear scalar perturbations)
  - at last-scattering, from primordial background of gravitational radiation, *predicted by inflation* (cf. Senatore's lectures)

# CMB Polarization: E/B Decomposition

- 2-d (headless) vector field on a sphere
- Spin-2/tensor spherical harmonics
- grad/scalar/E + curl/pseudoscalar/B patterns



- NB. From polarization pattern  $\Rightarrow$  E/B decomposition requires integration (*non-local*) or differentiation (*noisy*)
  - *Lewis et al; Bunn et al; Smith & Zaldarriaga; Grain et al; Bowyer & AJ; ...*
  - (data analysis problems)

# Polarization: math

- Scalar and tensor modes are isotropic, parity-symmetric fields on the sky.
- T is a scalar, E is the “gradient” of a scalar, B is the “curl” of a pseudoscalar

$$Q(\hat{n}) = -\frac{1}{2} \sum_{lm} (a_{lm}^E [{}_2Y_{lm}(\hat{n}) + {}_{-2}Y_{lm}(\hat{n})] + ia_{lm}^B [{}_2Y_{lm}(\hat{n}) - {}_{-2}Y_{lm}(\hat{n})])$$

$$U(\hat{n}) = -\frac{1}{2} \sum_{lm} (a_{lm}^B [{}_2Y_{lm}(\hat{n}) + {}_{-2}Y_{lm}(\hat{n})] + ia_{lm}^E [{}_2Y_{lm}(\hat{n}) - {}_{-2}Y_{lm}(\hat{n})])$$

$$e(\hat{n}) = \sum_{lm} \sqrt{\frac{(l-2)!}{(l+2)!}} a_{lm}^E Y_{lm}(\hat{n}) \quad b(\hat{n}) = \sum_{lm} \sqrt{\frac{(l-2)!}{(l+2)!}} a_{lm}^B Y_{lm}(\hat{n})$$

$$\nabla^4 e = -\frac{1}{2} [\bar{\partial}^2(Q + iU) + \partial^2(Q - iU)] \quad \nabla^4 b = \frac{i}{2} [\bar{\partial}^2(Q + iU) - \partial^2(Q - iU)]$$

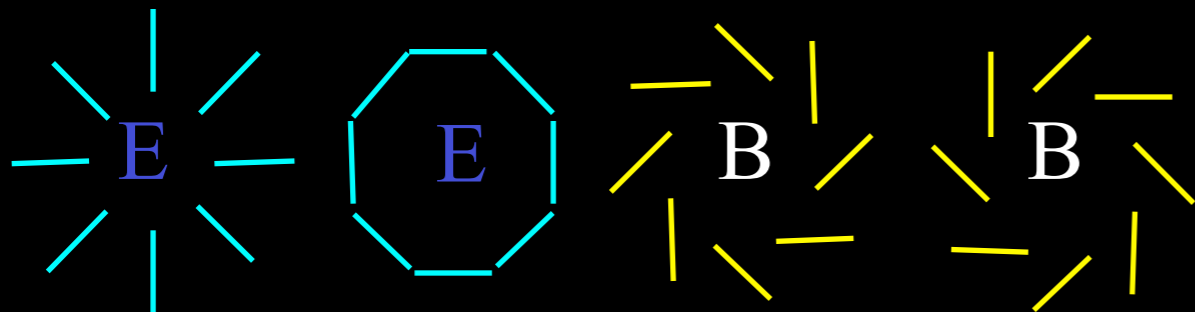
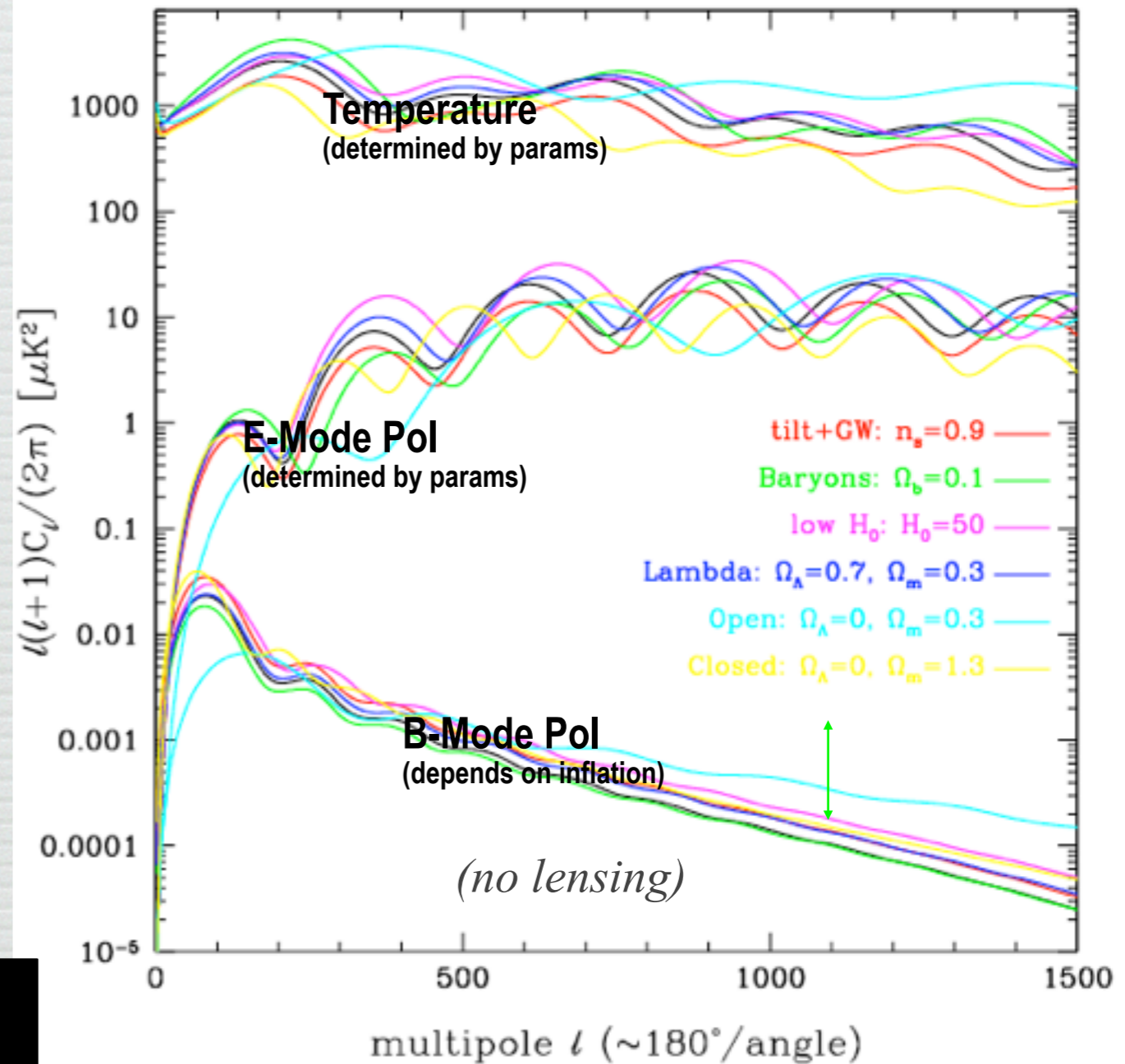
- expect  $\langle EB \rangle = \langle TB \rangle = 0$
- try to measure  $\langle TT \rangle, \langle BB \rangle, \langle EE \rangle, \langle TE \rangle$

# CMB Signals from inflation

- Want to probe **inflaton potential**  $V(\varphi)$
- Induce scalar and tensor power spectra
  - Observables:
    - temperature and polarization CMB spectra
    - functionally linear relationships
$$C_\ell^{BB} = \int dk T_\ell^{hB}(k) P_h(k)$$
$$C_\ell^{TT} = \int dk [T_\ell^{hT}(k) P_h(k) + T_\ell^{RT}(k) P_R(k)]$$
    - Transfer functions  $T$  depend on cosmological parameters
    - Amplitude ( $r=T/S$ ) and shape ( $n_s, n_T$ ) of the spectra probe the inflaton potential
- Non-gaussianity:
  - specific inflationary models  $\Rightarrow$  departures from Gaussianity
  - e.g.,  $f_{NL} \sim 1$  (in reach of Planck, but not [yet] detected)

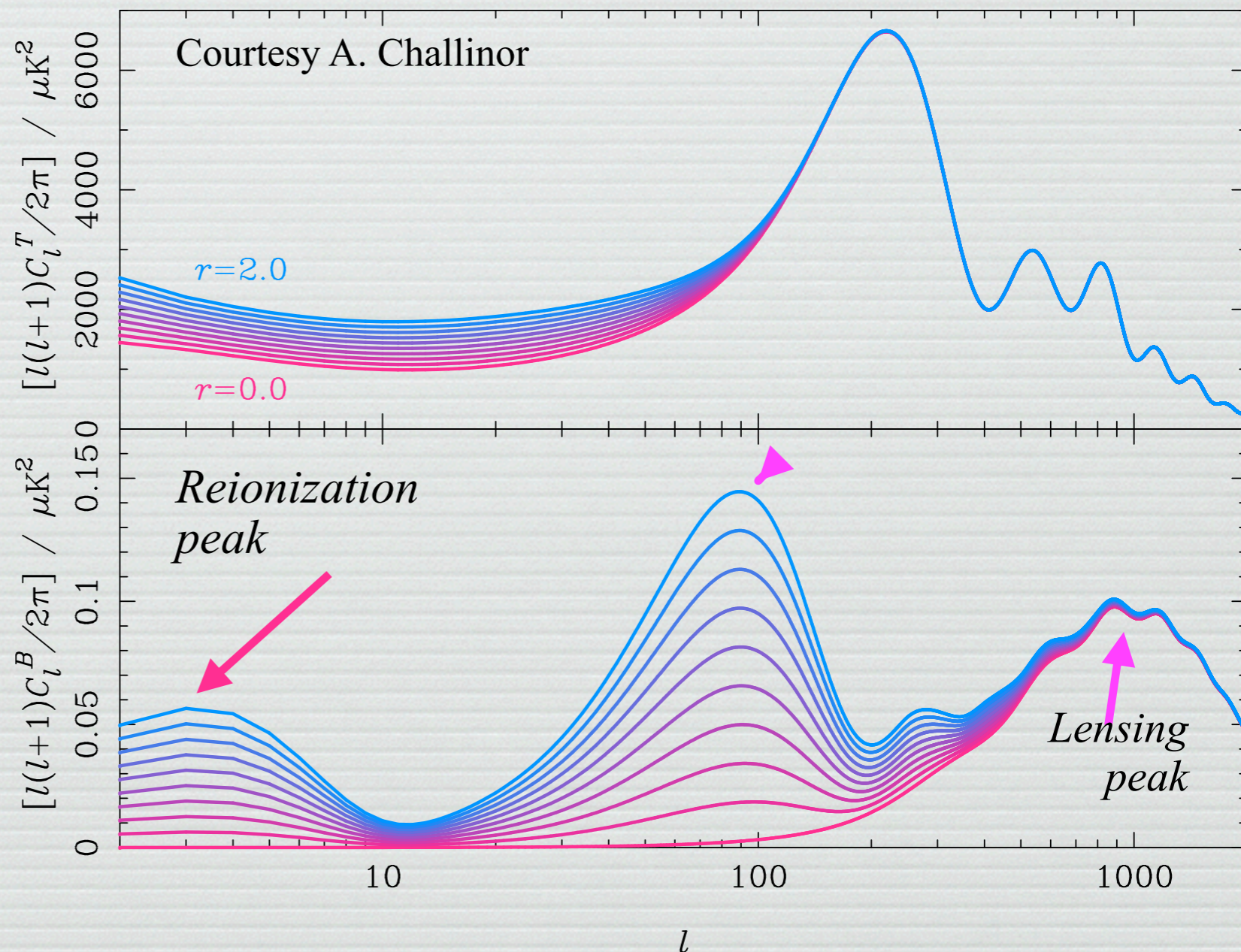
# The Polarization of the CMB

- Anisotropic radiation field at **last scattering** → polarization
  - “Grad” or  $E$  mode
  - Breaks degeneracies
  - New parameters:
    - reionization
- “Curl” or  $B$  sensitive to **gravity waves**
  - “Smoking gun” of inflation?
  - Very low amplitude
- Need better handle on systematics, and...
- Polarized foregrounds?



# Gravitational Radiation & CMB

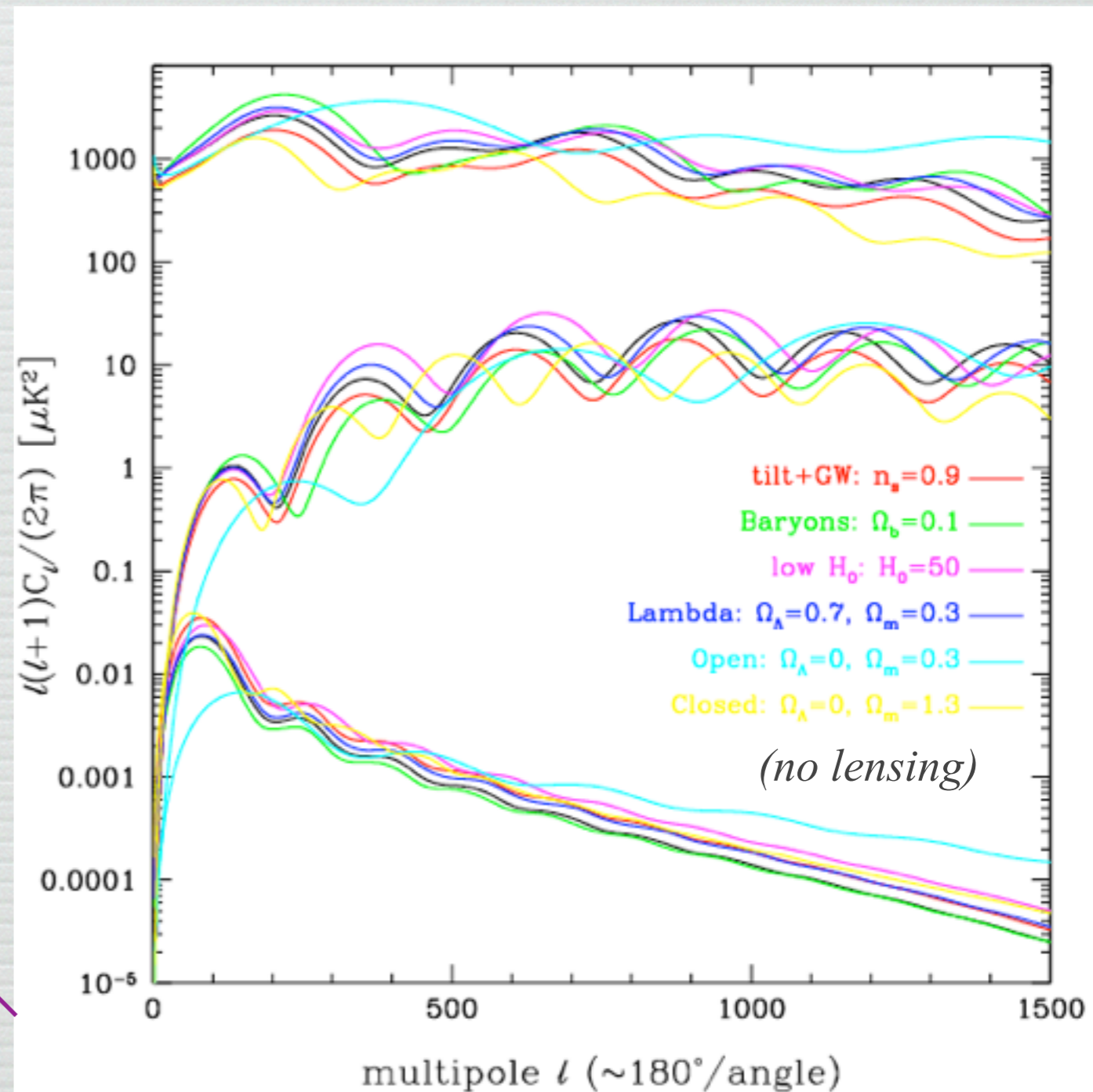
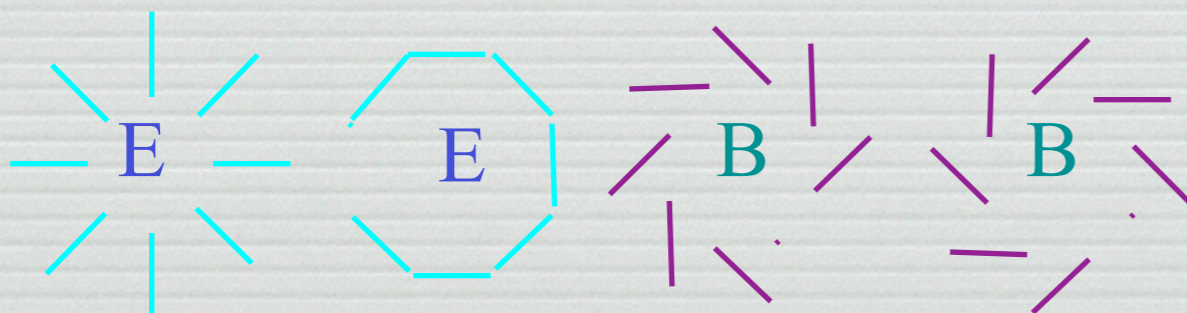
- Last scattering: “direct” effect of **tensor modes** (primordial GWs) on the primordial plasma
- inflationary potential
- dominated by *lensing of E*  $\Rightarrow$  *B* for  $\ell \gtrsim 200$
- sensitive to  $m_\nu \lesssim 0.06 \text{eV}$ 
  - (i.e., hot dark matter)
- Reionization peak  $\ell \lesssim 20$ 
  - need  $\sim$ full-sky. Difficult for single suborbital experiments
- Limits depend on full set of parameters



Suborbital experiments target  $\ell \sim 100$  peak:  
require order-of-magnitude increase in  
sensitivity over Planck

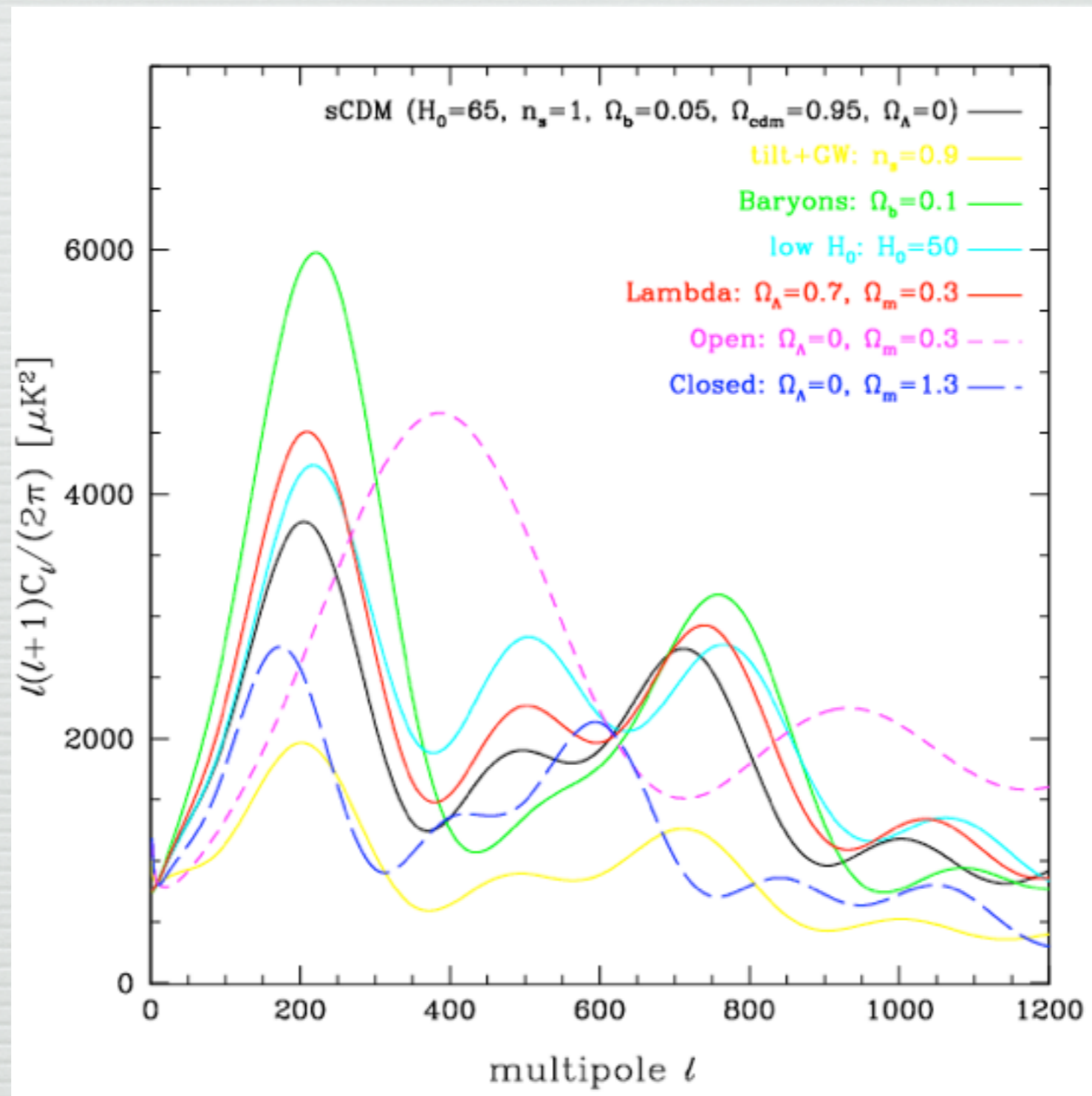
# Polarization from Gravitational Radiation

- Causal physics — scattering in baryon-photon plasma — same as intensity, E-mode polarization
- Specific predictions given primordial  $P(k)$  + parameters



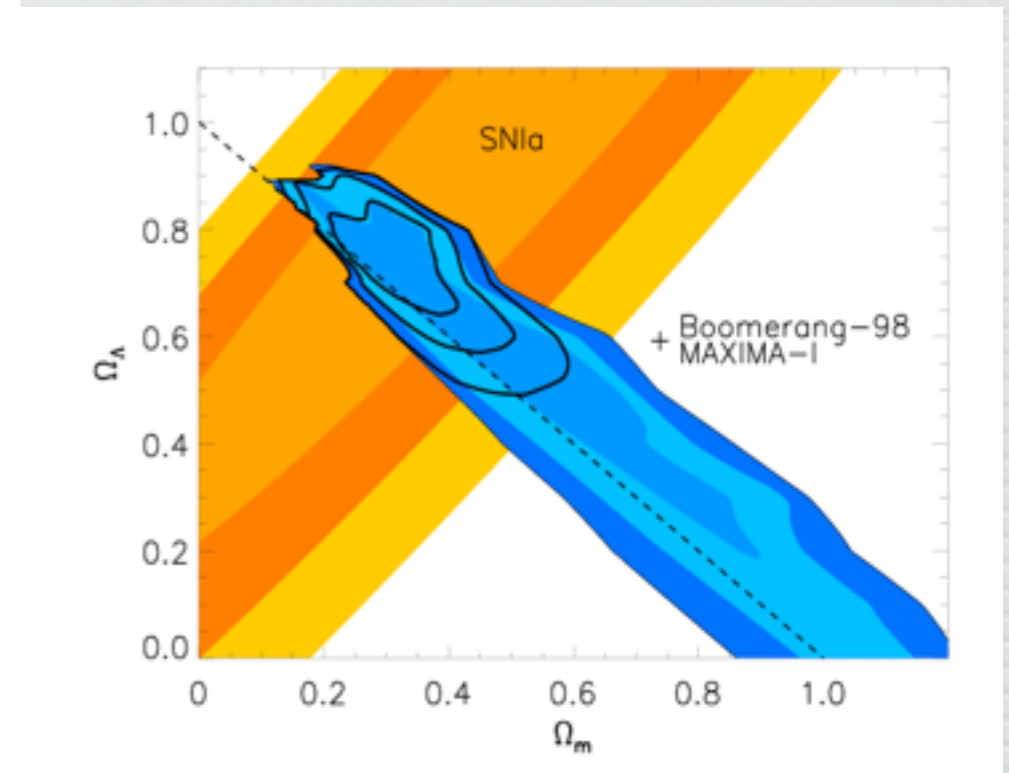
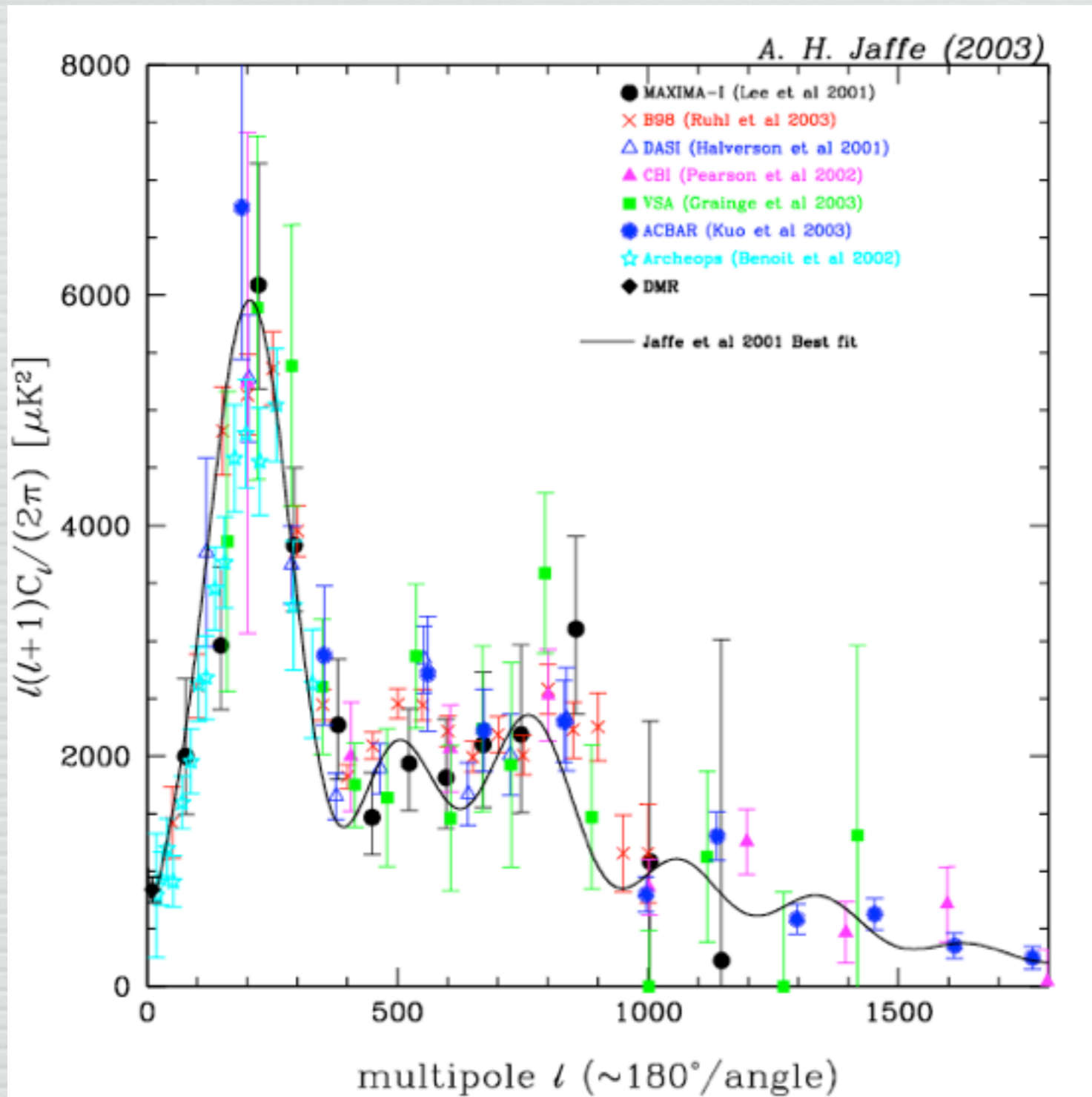
# Theoretical Predictions

Mean square fluctuation amplitude

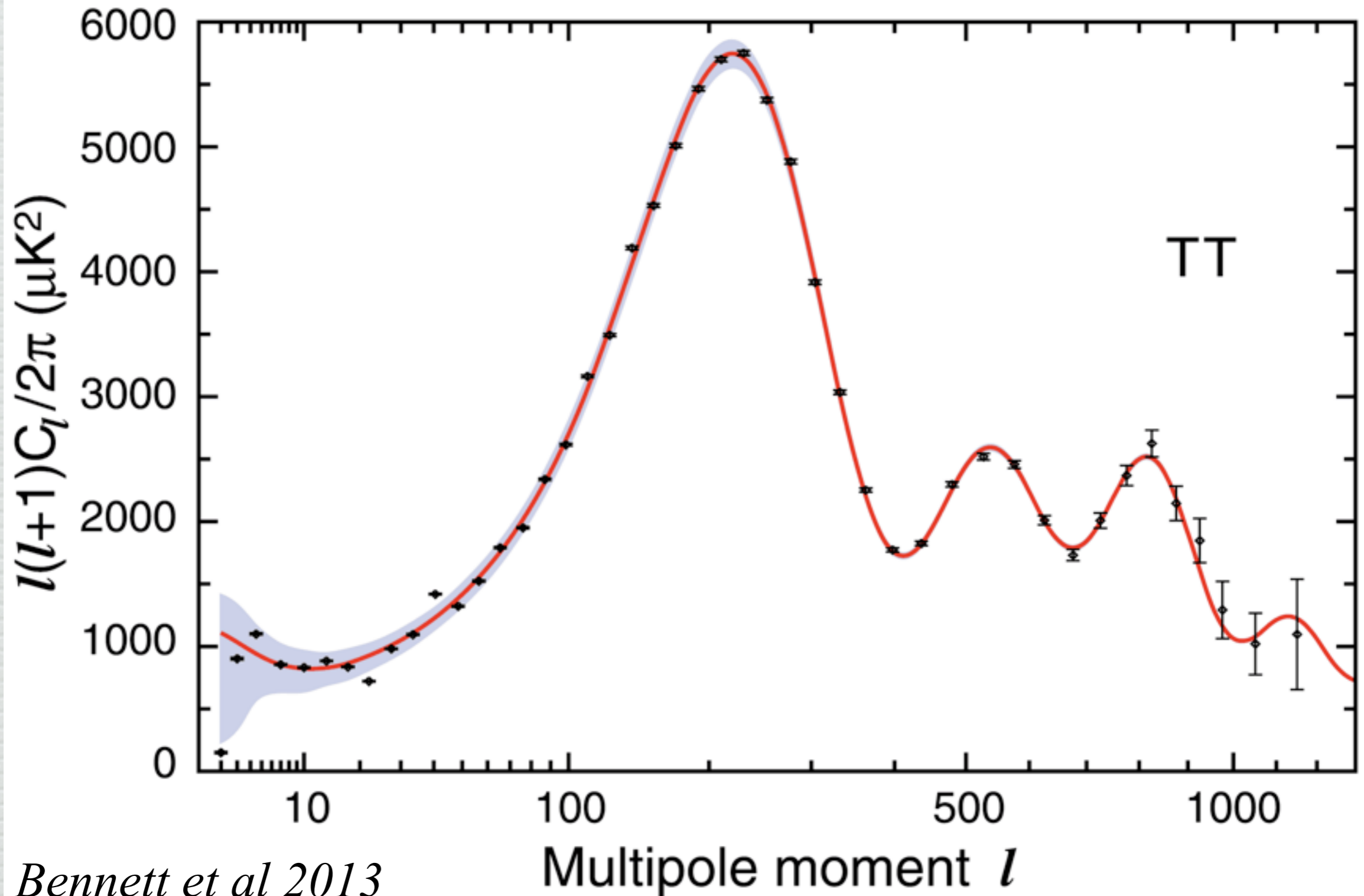


$\sim 180^\circ/\text{Angular scale}$

# January, 2003



# WMAP (2003-2012)



Bennett et al 2013



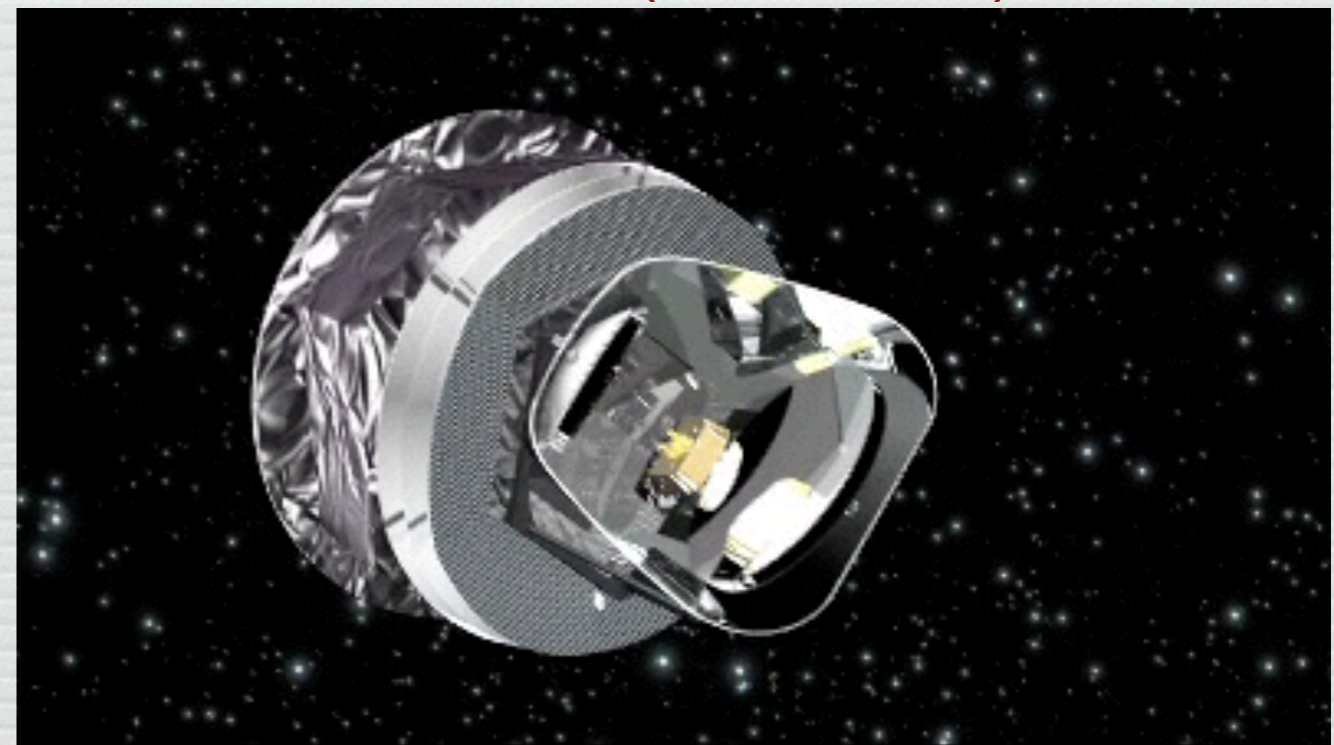
# Planck: Launched 2009

- Nominal mission: 14 Months  
(extended  $\sim 2x$ , plus a “warm extension” for LFI)

*Planck launch, 14 May 2009*

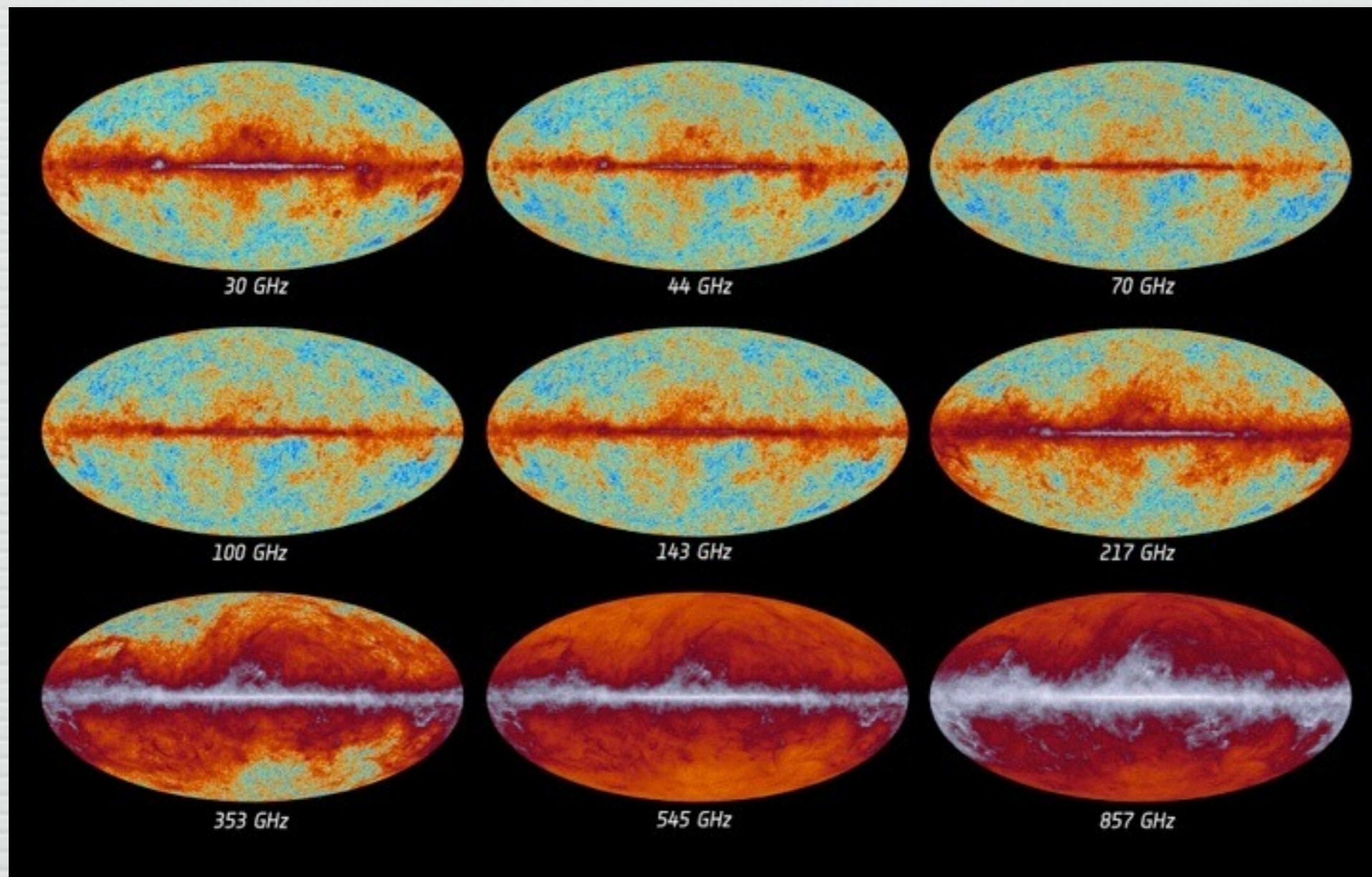


*Planck in orbit (animation)*



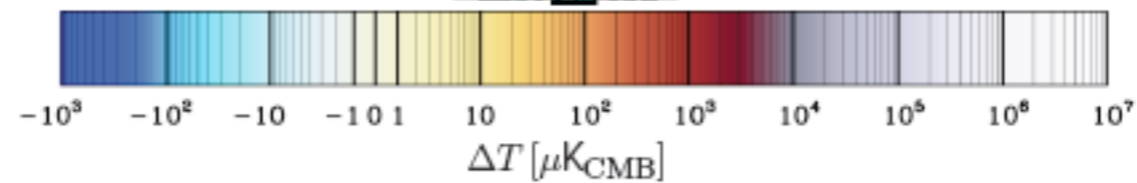
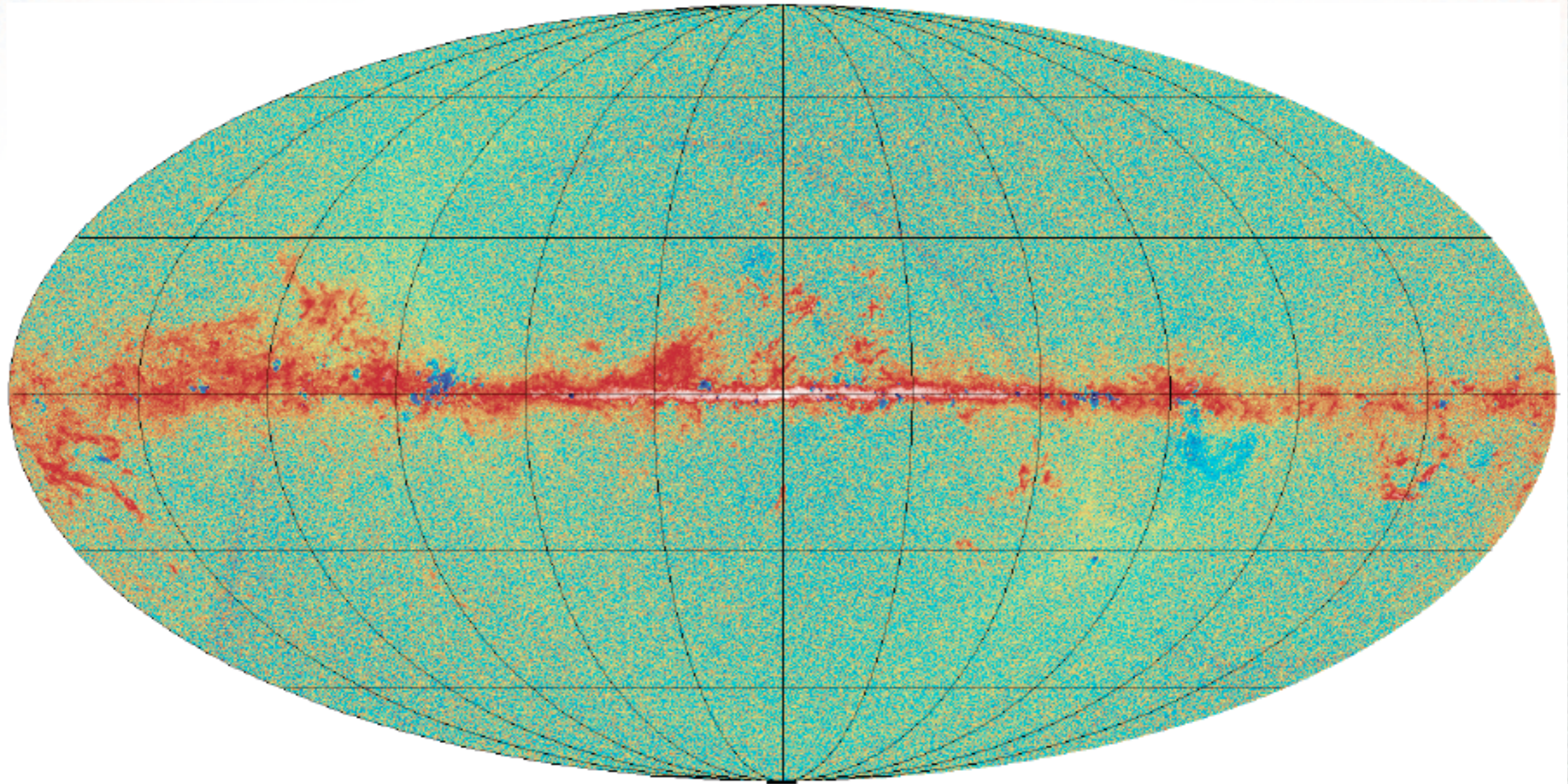
# Frequency Maps

- Raw data: ~500 trillion samples over 15 months
- Maps: ~50 million pixels over 9 frequencies



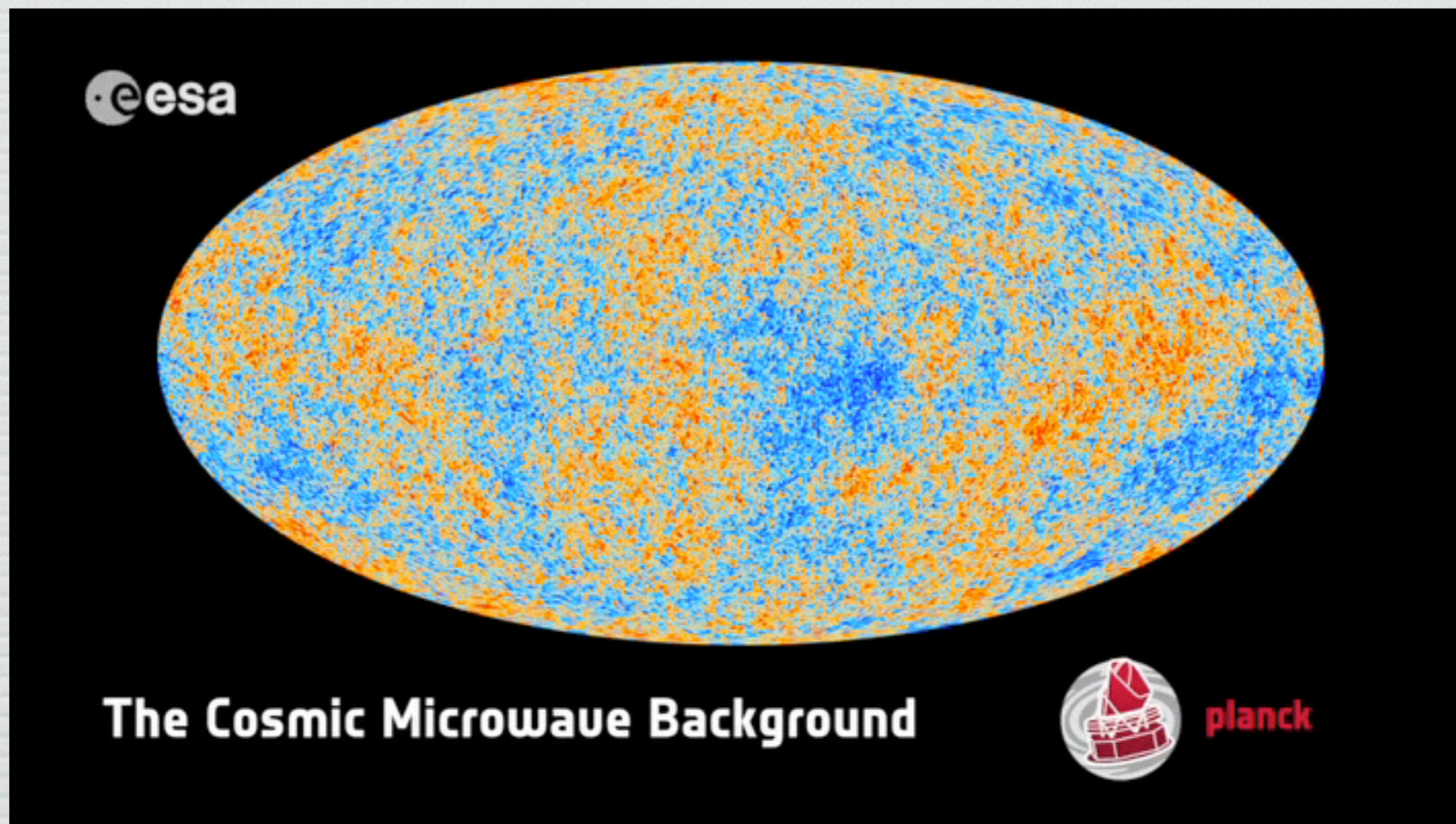
# Map consistency

- 100 GHz – 70 GHz. Red is mostly CO, blue is mostly free-free. CMB is gone!



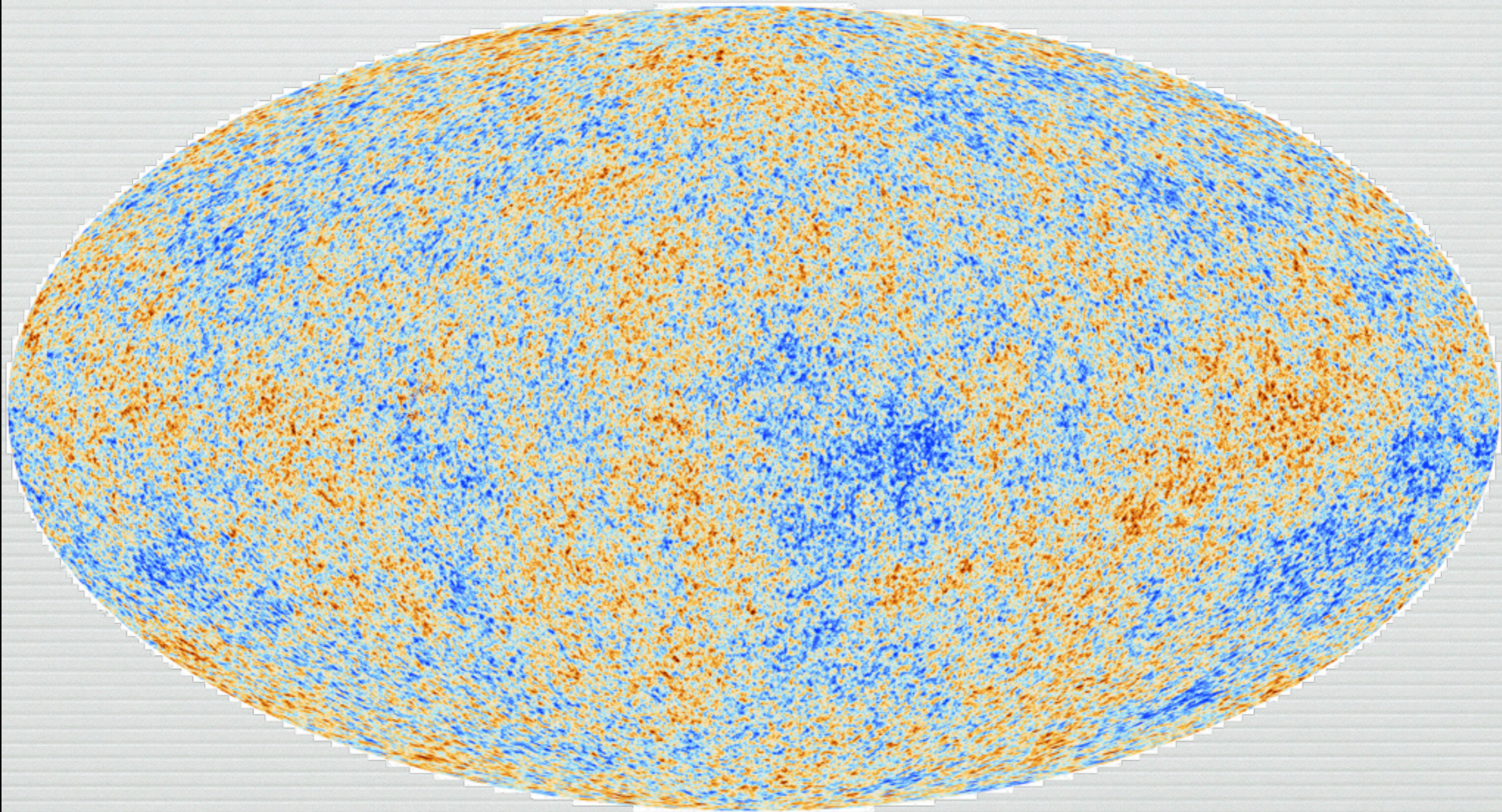
# Component Separation

- Emission at any frequency is the sum of the CMB and astrophysical sources along the line of sight.
- *Planck* observes in 9 bands over 30–850 GHz to disentangle cosmology from astrophysics



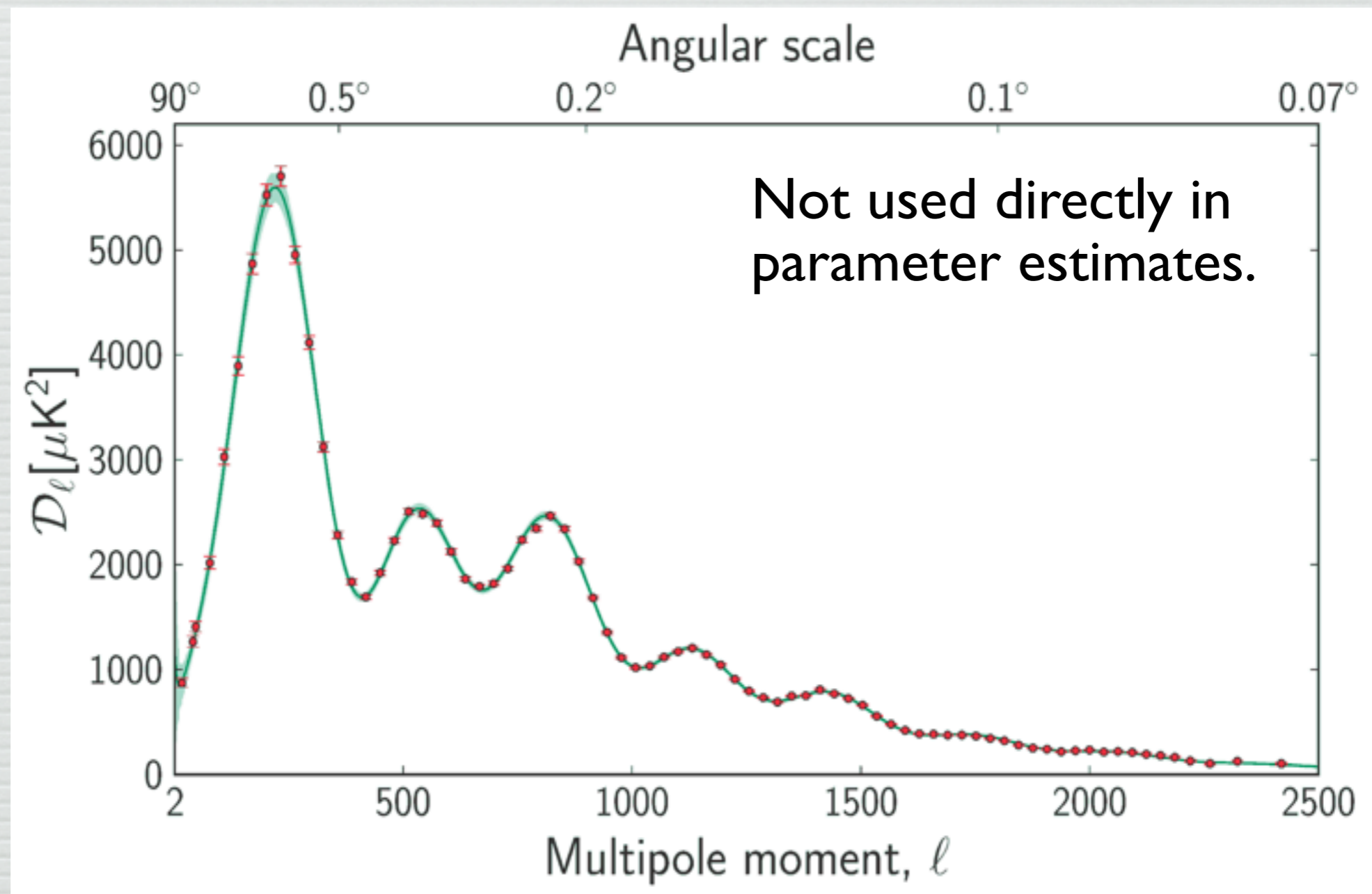
# Planck (2013)

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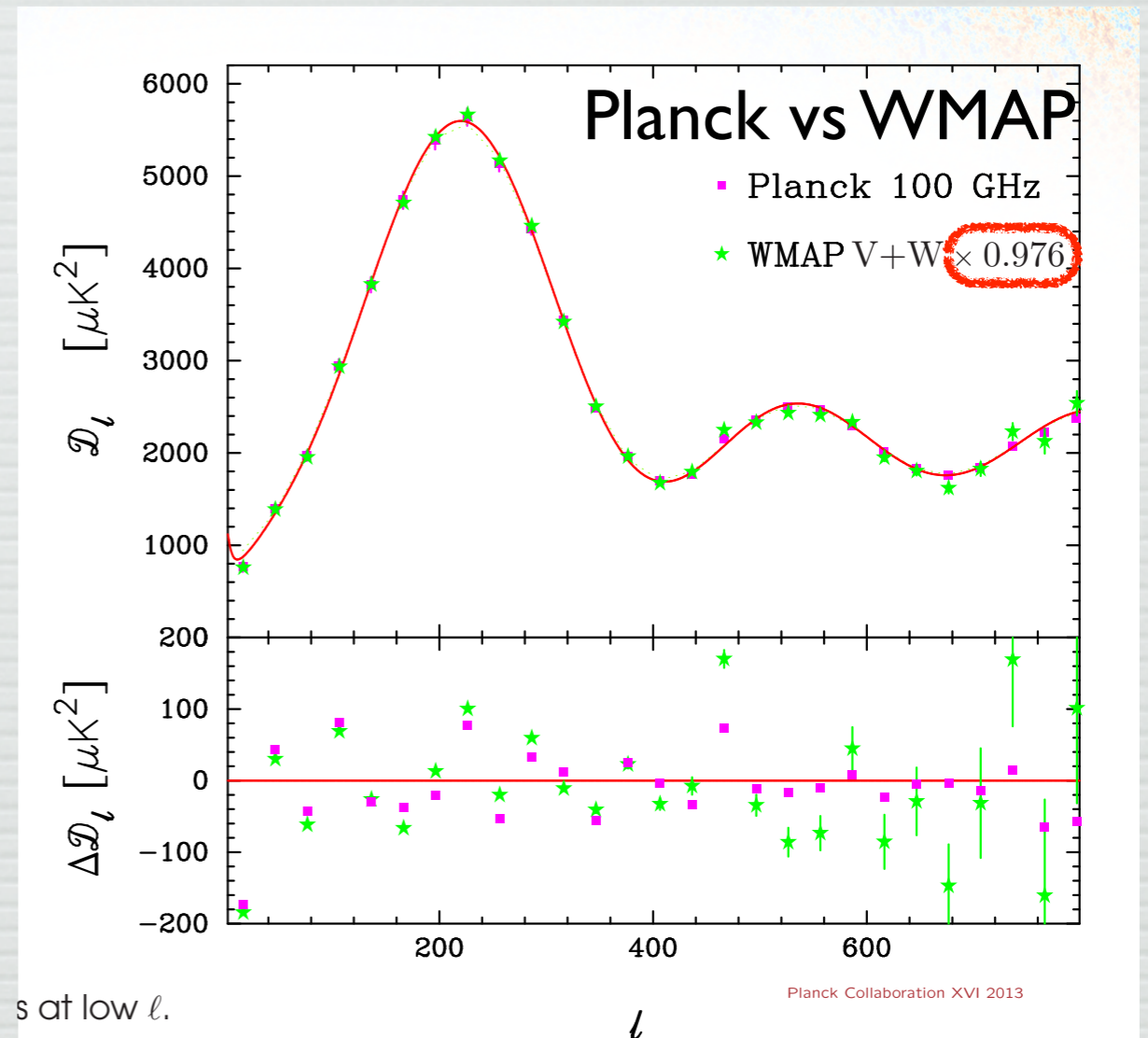
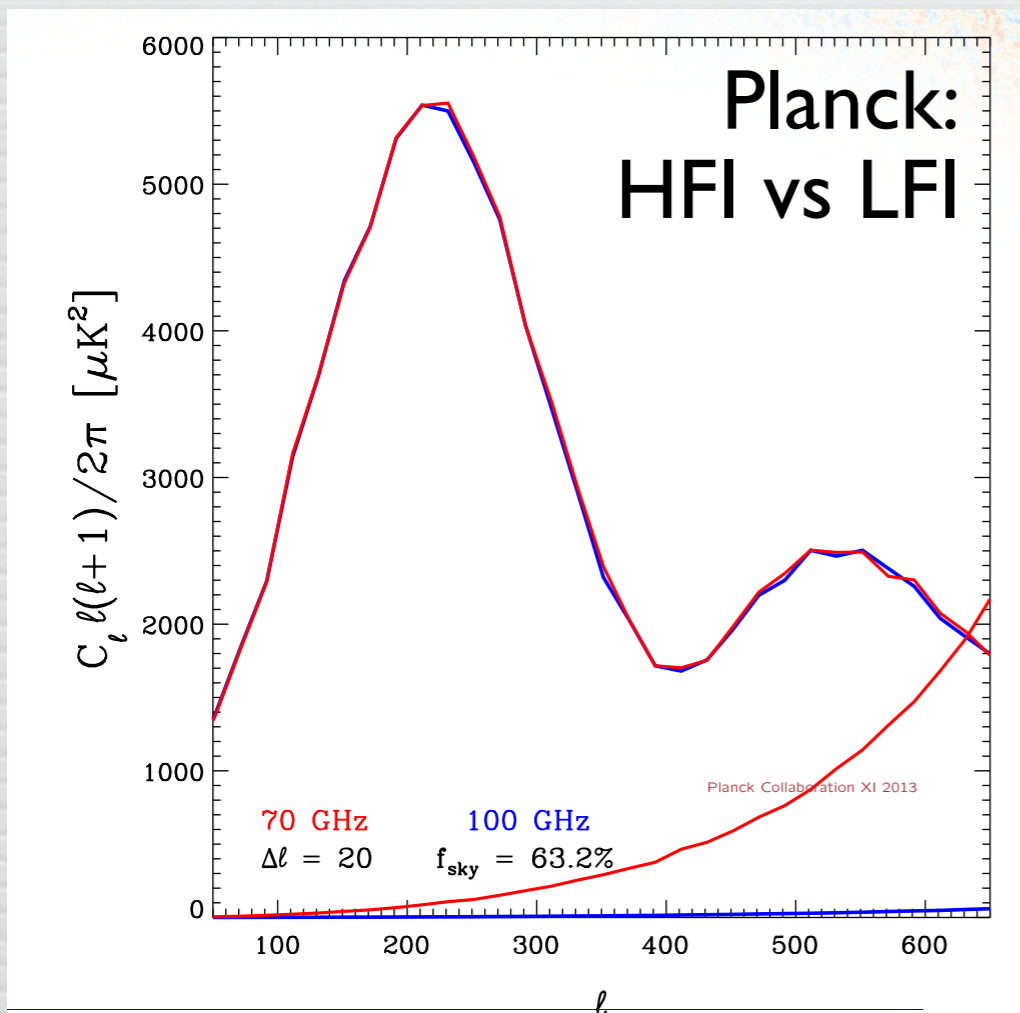
# Planck (2013)

- From  $\sim 50$  million pixels to  $\sim 2500$  multipoles



# Power spectrum consistency

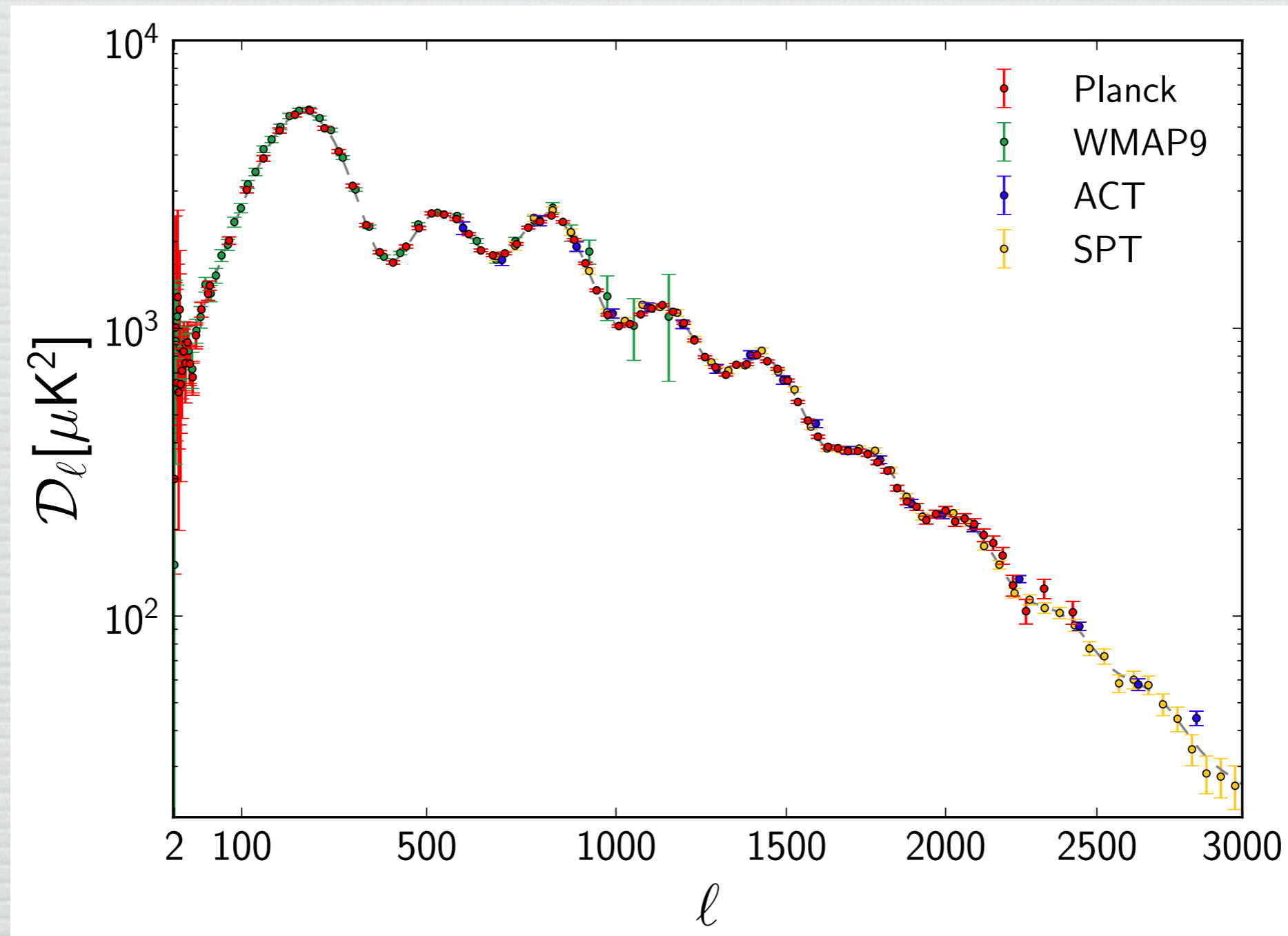
- Excellent agreement between HFI & LFI
- few x 0.1% through the first peak



- Evidence of a  $\sim 2.5\%$  recalibration between WMAP & Planck?

# Spectra

Planck Collaboration: The *Planck* mission



**Fig. 25.** Measured angular power spectra of *Planck*, WMAP9, ACT, and SPT. The model plotted is *Planck*'s best-fit model including *Planck* temperature, WMAP polarization, ACT, and SPT (the model is labelled [Planck+WP+HighL] in Planck Collaboration XVI (2013)). Error bars include cosmic variance. The horizontal axis is  $\ell^{0.8}$ .

# Cosmological Parameters

## □ Planck + WWP

from 2500 points to ~6 parameters

### ■ ~directly measured

$$\Omega_b h^2 = 0.02205 \pm 0.00028$$

$$\Omega_c h^2 = 0.1199 \pm 0.0027$$

$$n_s = 0.960 \pm 0.007$$

$$\tau = 0.089 \pm 0.014$$

$$10^9 A_s = 2.20 \pm 0.06$$

$$100 \theta_{MC} = 1.04131 \pm 0.00063$$

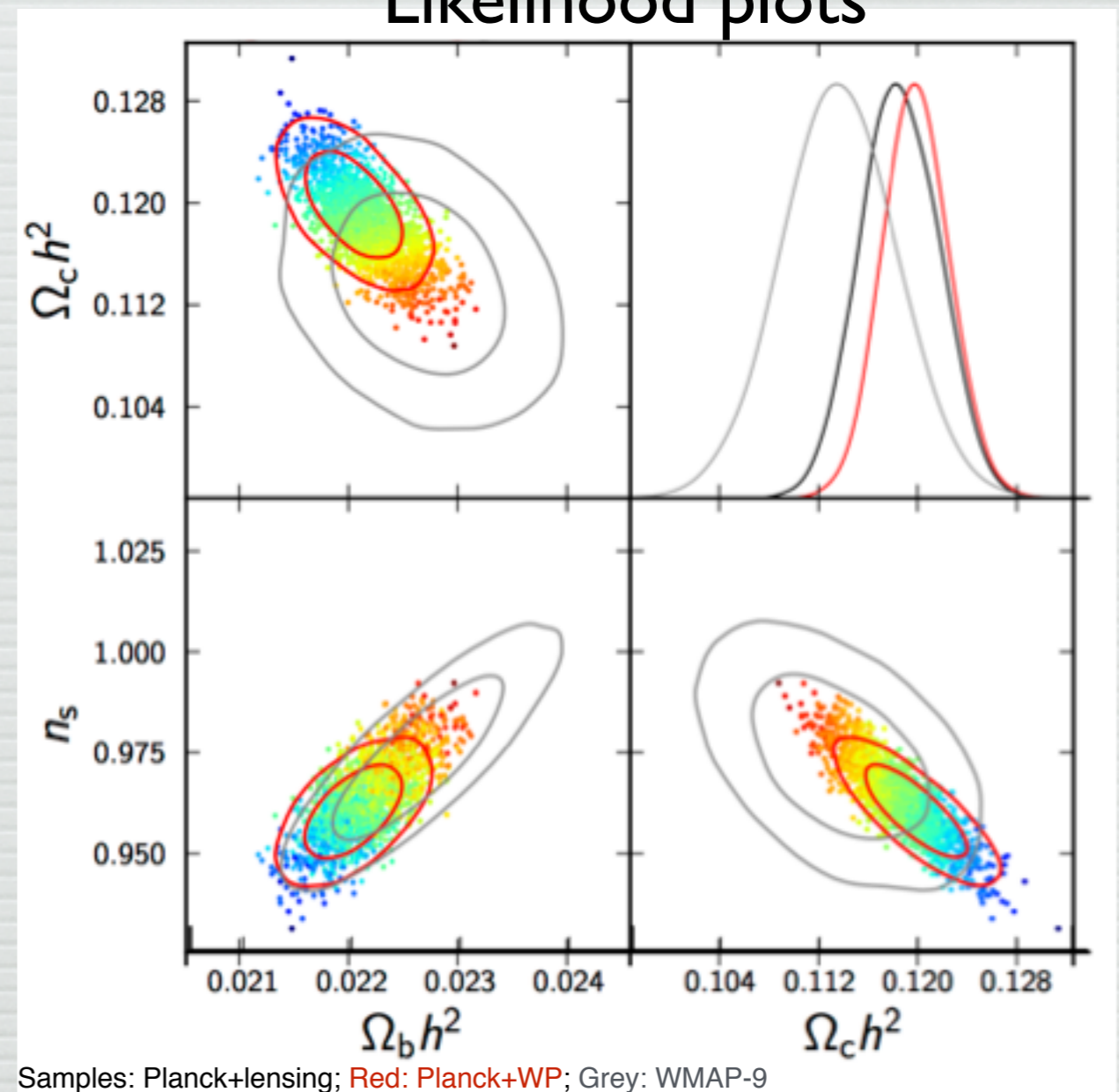
### ■ derived (e.g.)

$$H_0 = 67.3 \pm 1.2 \text{ km/s/Mpc}$$

$$\Omega_\Lambda = 0.685 \pm 0.017$$

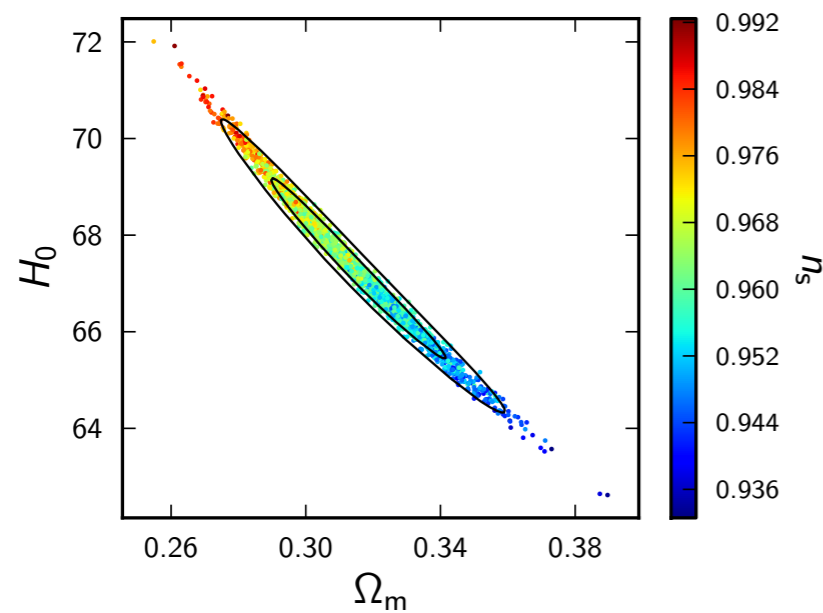
$$\sigma_8 = 0.829 \pm 0.012$$

## Likelihood plots

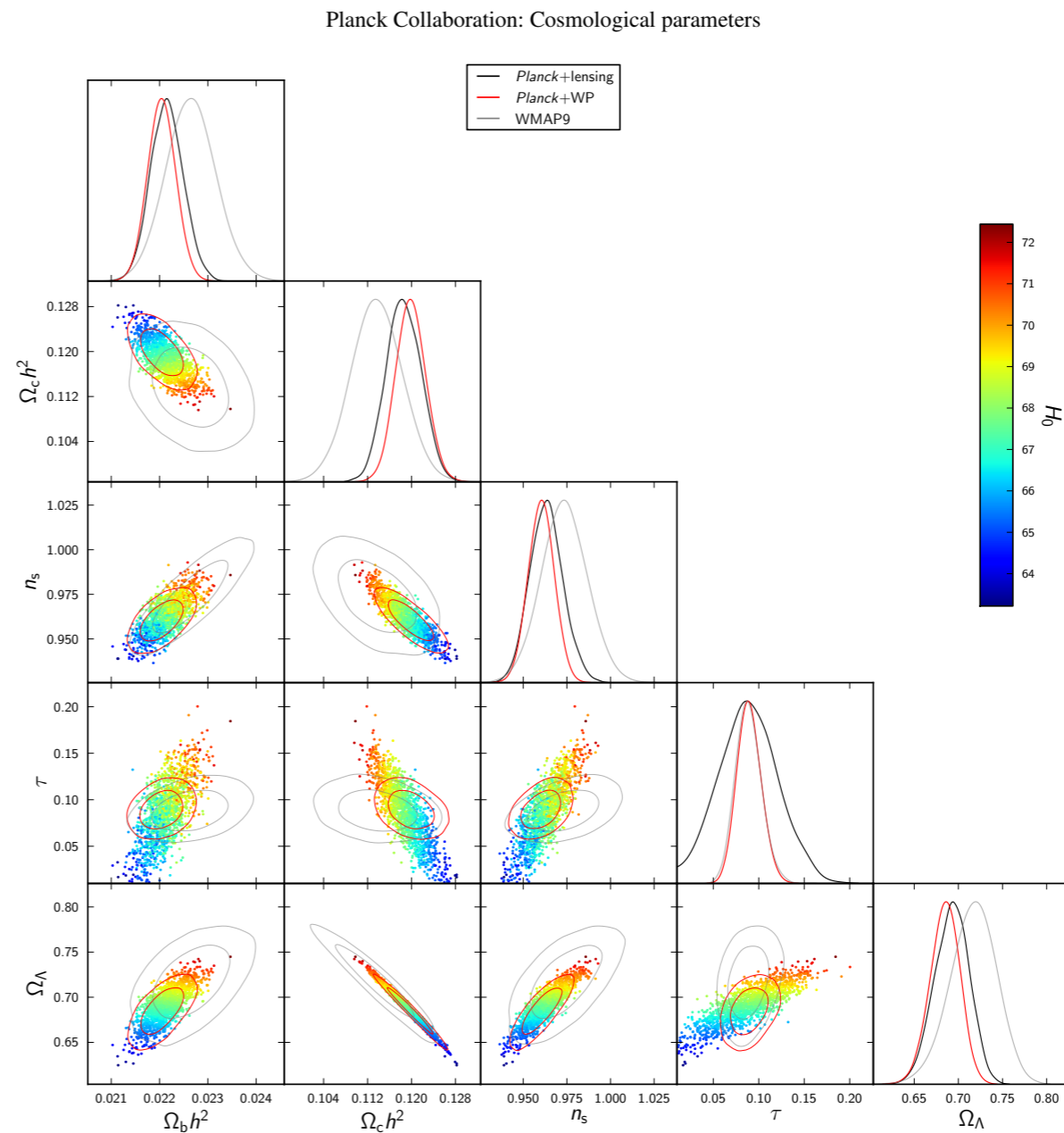


### ■ $\Sigma m_\nu < 0.23 \text{ eV}$ (95%), $N_{\nu, \text{eff}} = 3.30 \pm 0.27$ (68%) [with caveats]

# Planck Params



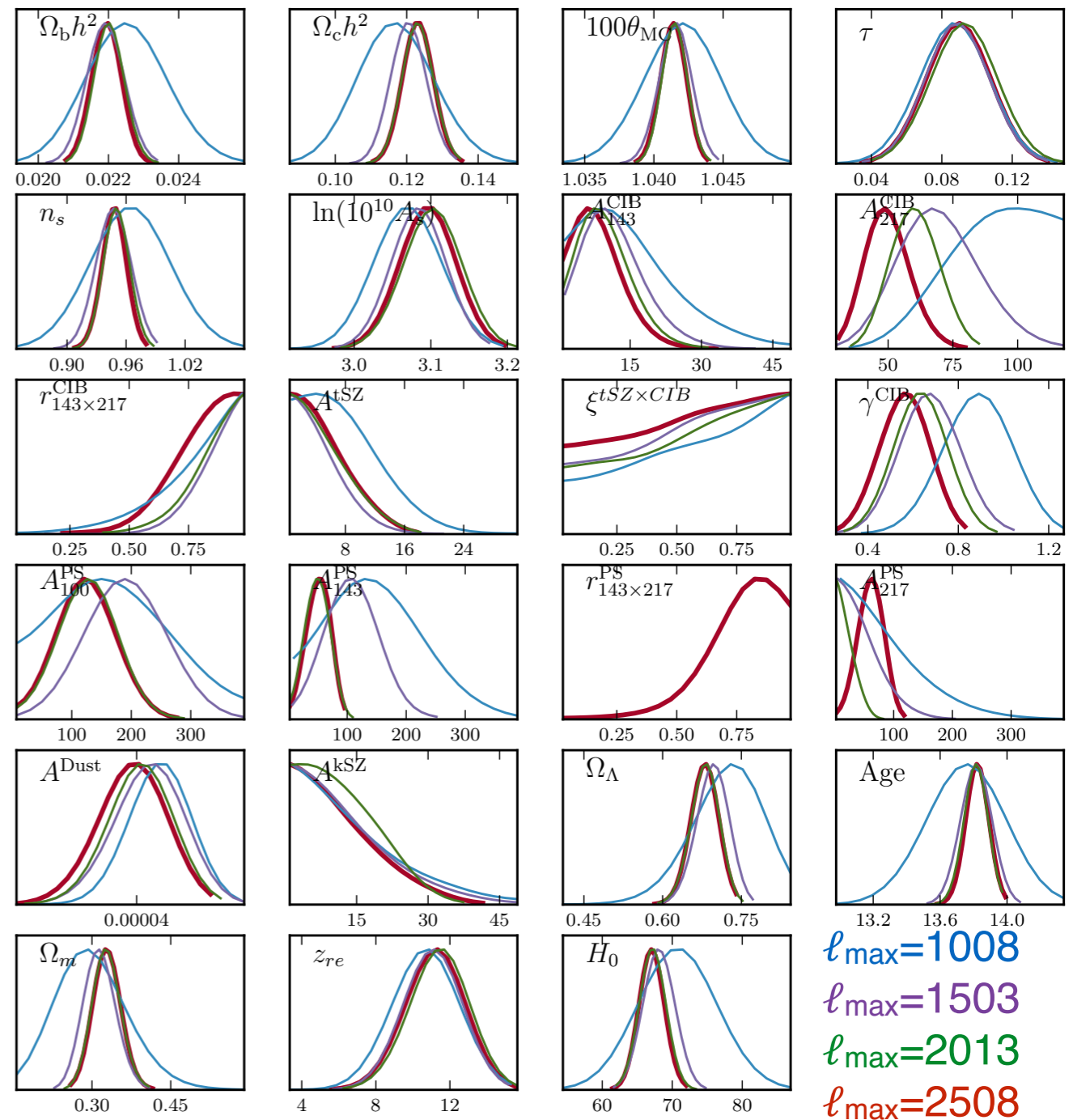
**Fig. 3.** Constraints in the  $\Omega_m$ - $H_0$  plane. Points show samples from the *Planck*-only posterior, coloured by the corresponding value of the spectral index  $n_s$ . The contours (68% and 95%) show the improved constraint from *Planck*+lensing+WP. The degeneracy direction is significantly shortened by including WP, but the well-constrained direction of constant  $\Omega_m h^3$  (set by the acoustic scale), is determined almost equally accurately from *Planck* alone.



**Fig. 2.** Comparison of the base  $\Lambda$ CDM model parameters for *Planck*+lensing only (colour-coded samples), and the 68% and 95% constraint contours adding *WMAP* low- $\ell$  polarization (WP; red contours), compared to *WMAP*-9 (Bennett et al. 2012; grey contours).

# Self-consistency of the parameters

- Very weak dependence on which subset of *Planck* data is analysed.
- Robust to
  - changes in  $\ell_{\max}$ 
    - e.g.,  $\ell \sim 1800$  cooler line
  - inclusion of channels
    - 217 GHz is a minor outlier, but inclusion affects parameters by a small fraction of a sigma

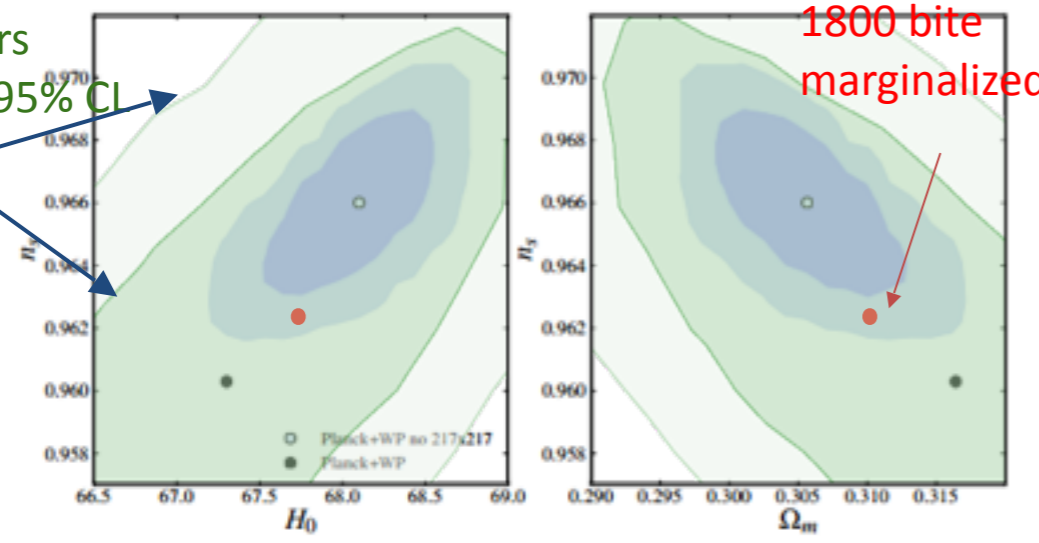


$\ell_{\max}=1008$   
 $\ell_{\max}=1503$   
 $\ell_{\max}=2013$   
 $\ell_{\max}=2508$

Planck+WP parameter posteriors @ 68 & 95% CI

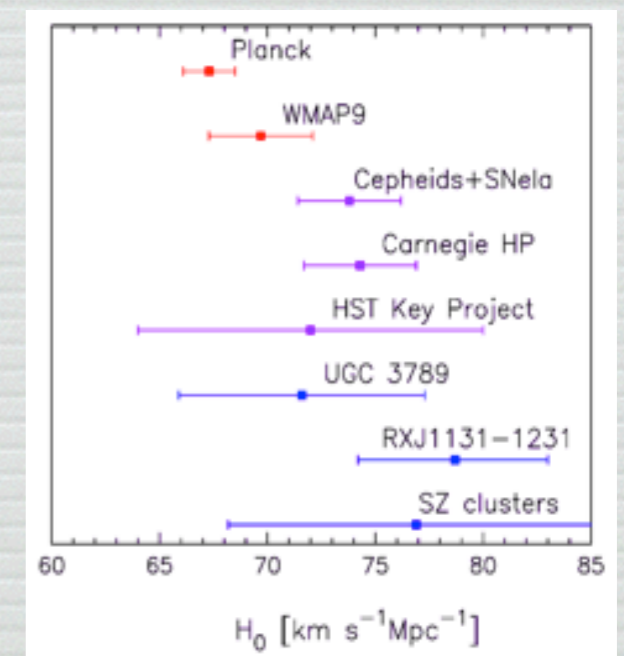
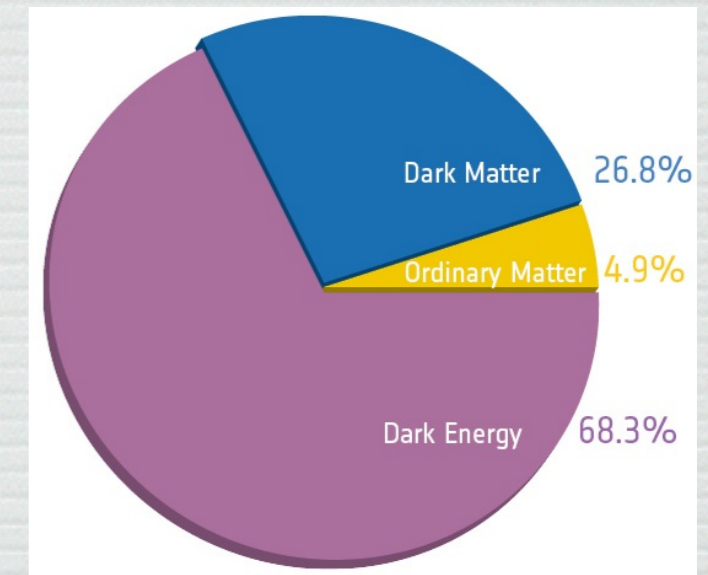
Spergel, Flauger & Hlozek 2013

Planck+WP with 1800 bite marginalized over



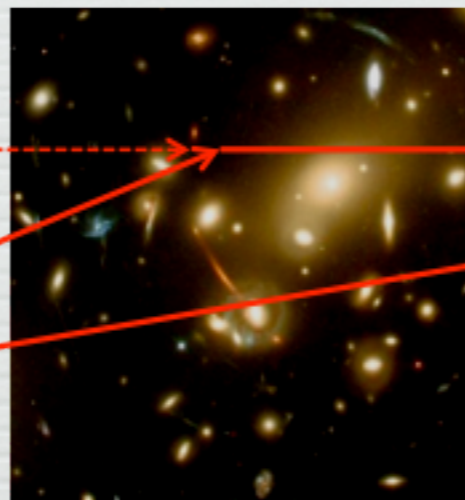
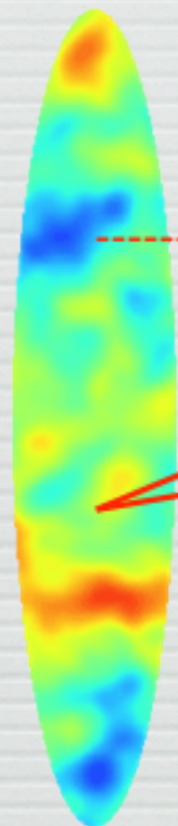
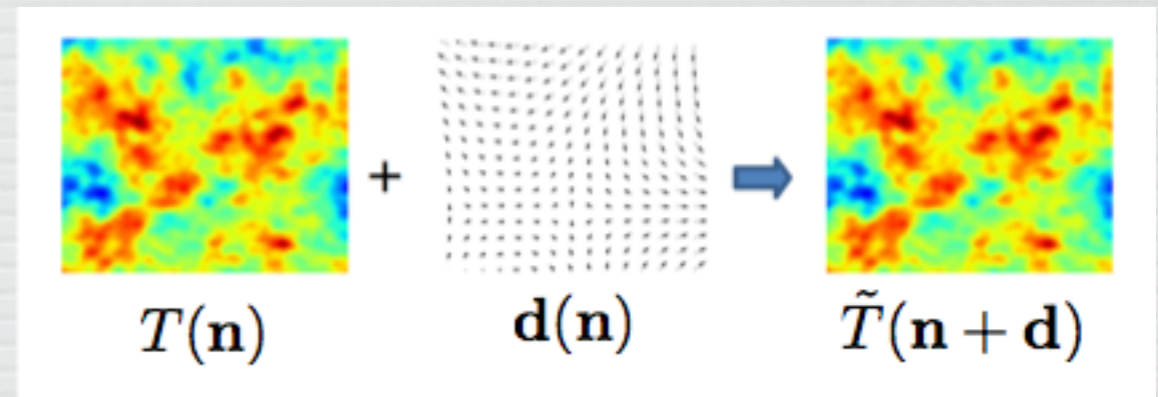
# The new old Universe

- Big picture: no qualitative changes
- Quantitatively:
  - Planck's higher resolution allows a better measurement of the damping physics at small scales
    - slightly slower expansion rate, slightly older universe
    - slightly less dark energy, more dark matter
  - Cosmological parameters not “directly measured” by *Planck*; details depend on the models considered [“priors”]
    - In particular, there are some tensions with other measurements of  $H_0$



# Gravitational lensing

$$\frac{\ell^2}{4} C_\ell^{dd} = \int_0^{\eta_*} d\eta \underbrace{W^2(\eta)}_{\text{geometry}} \underbrace{P\left(k = \frac{\ell + 1/2}{d_A(\eta)}, \eta\right)}_{\text{matter}}$$



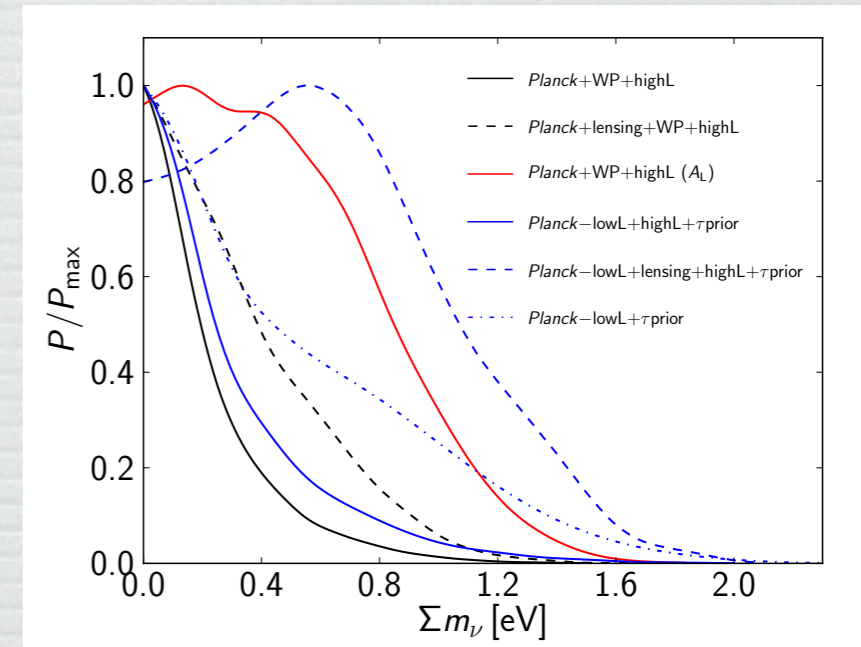
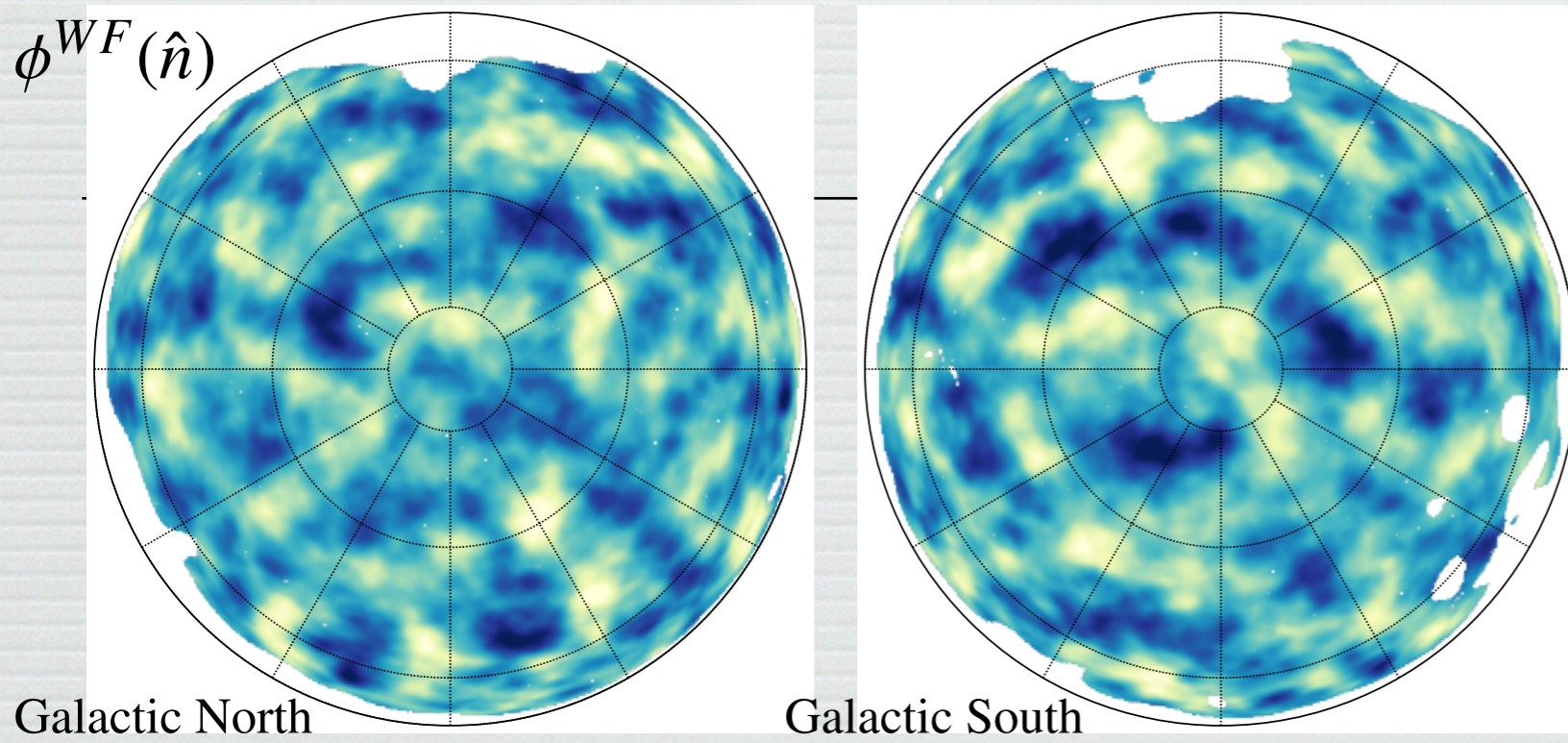
$$\Theta(\hat{n}) = \tilde{\Theta}(\hat{n} + \nabla\phi)$$

Lensed      Unlensed      Deflection Field

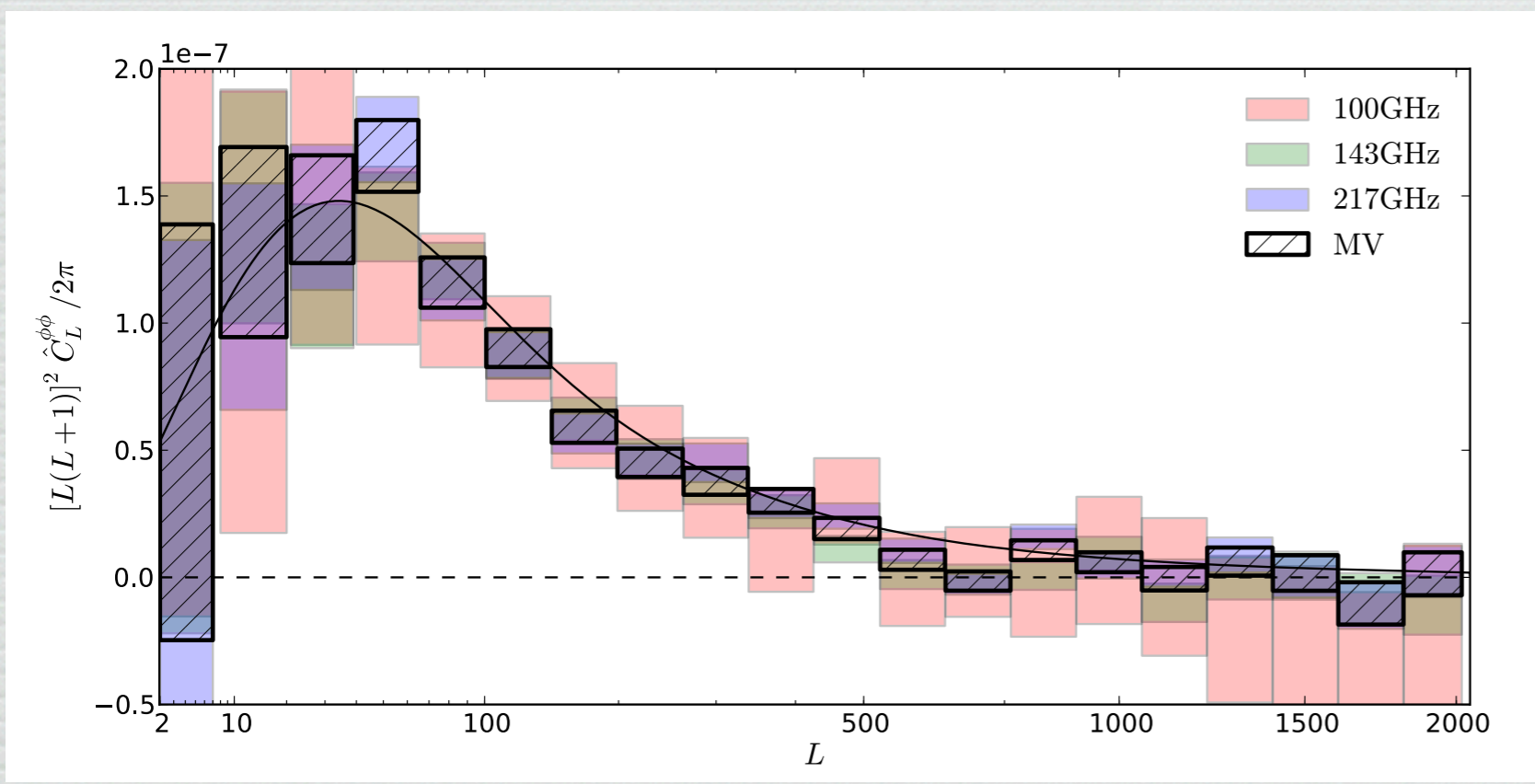
- *Planck* observes lensing:
  - non-Gaussianity
  - on the power spectrum (smoothing)

- correlations with the IR background

# Lensing



**Fig. 26.** Marginalized posterior distributions for  $\Sigma m_\nu$  in flat models from CMB data. We show results for *Planck*+WP+highL without (solid black) and with (red) marginalization over  $A_L$ , showing how the posterior is significantly broadened by removing the lensing information from the temperature anisotropy power spectrum. The effect of replacing the low- $\ell$  temperature and (*WMAP*) polarization data with a  $\tau$  prior is shown in solid blue (*Planck*-lowL+highL+ $\tau$ prior) and of further removing the high- $\ell$  data in dot-dashed blue (*Planck*-lowL+ $\tau$ prior). We also show the result of including the lensing likelihood with *Planck*+WP+highL (dashed black) and *Planck*-lowL+highL+ $\tau$ prior (dashed blue).



# non-Gaussianity: $f_{\text{NL}}$

---

□ Heuristically  $\phi = \phi_G + f_{\text{NL}}(\phi_G^2 - \langle \phi_G^2 \rangle)$   
for a Gaussian  $\phi_G$  (e.g., multi-field inflation)

- This is the (spatially) local model for non-Gaussianity
- Induces specific 3-d correlations

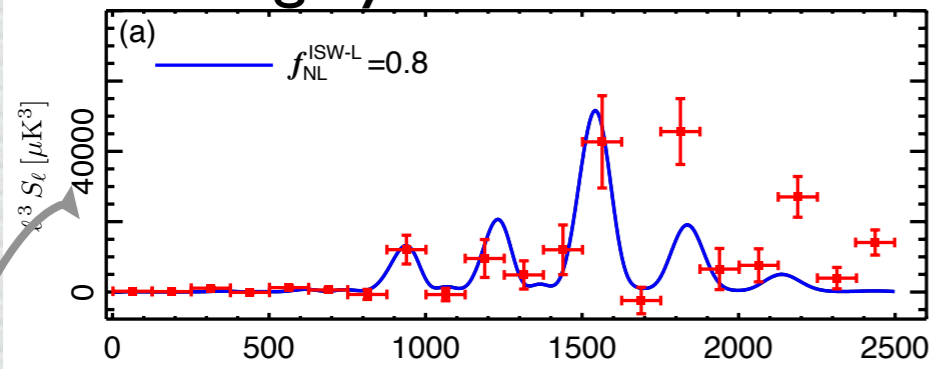
$$\begin{aligned}\langle \phi\phi\phi \rangle &\sim 3f_{\text{NL}} (\langle \phi_G\phi_G\phi_G\phi_G \rangle - \langle \phi_G\phi_G \rangle \langle \phi_G\phi_G \rangle) + O(f_{\text{NL}}^2) \\ &\sim 6f_{\text{NL}} \langle \phi_G\phi_G \rangle \langle \phi_G\phi_G \rangle + O(f_{\text{NL}}^2)\end{aligned}$$

and hence 2-d correlations in the CMB

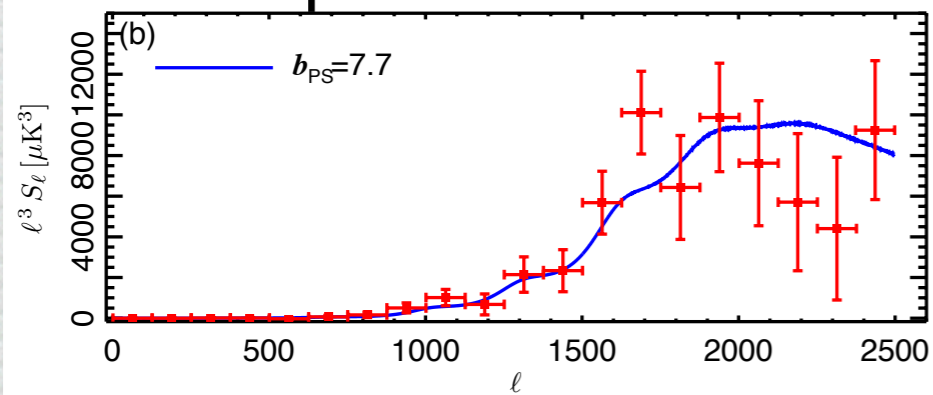
- Corresponds to Fourier bispectrum  $B(k_1, k_2, k_3)$  which peaks in squeezed case  $k_1 \ll k_2 \approx k_3$ 
  - modulate small-scale structure by large-scale modes
    - cf. galaxy bias
- More generally, consider other shapes (e.g., equilateral) motivated by specific theories

# Non-Gaussianity

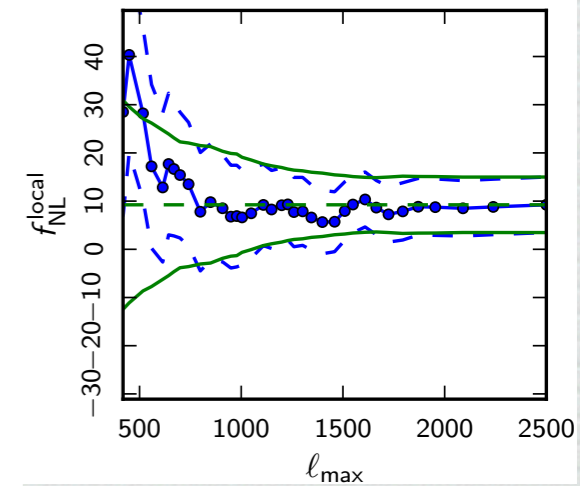
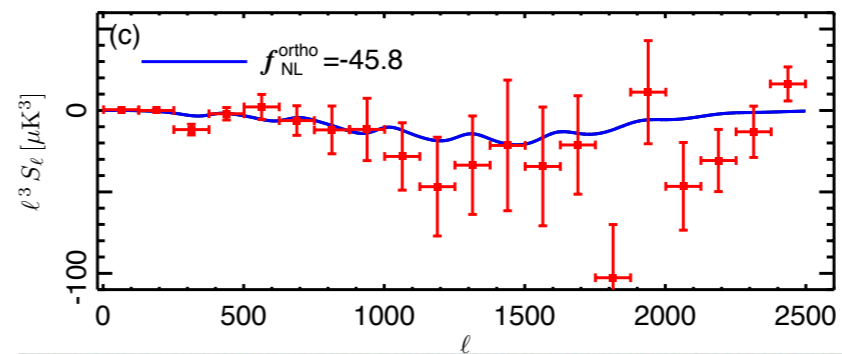
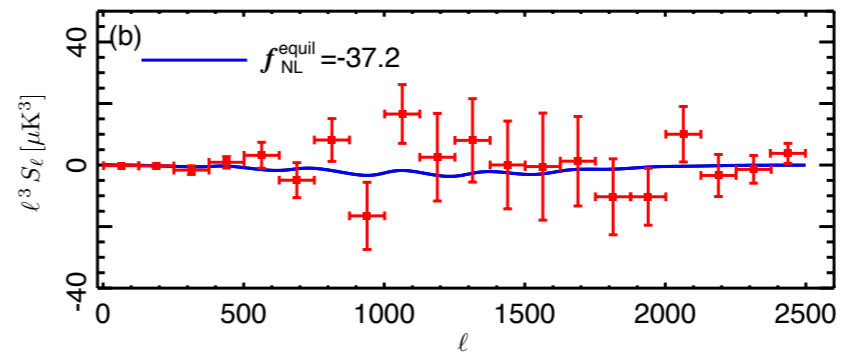
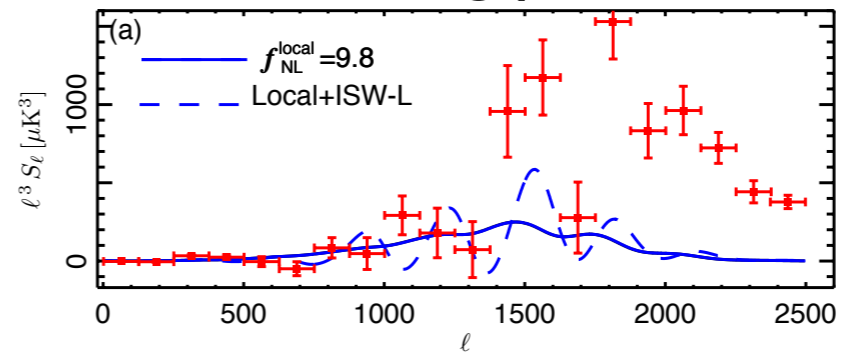
We see lensing by cosmic structures



...and point sources...



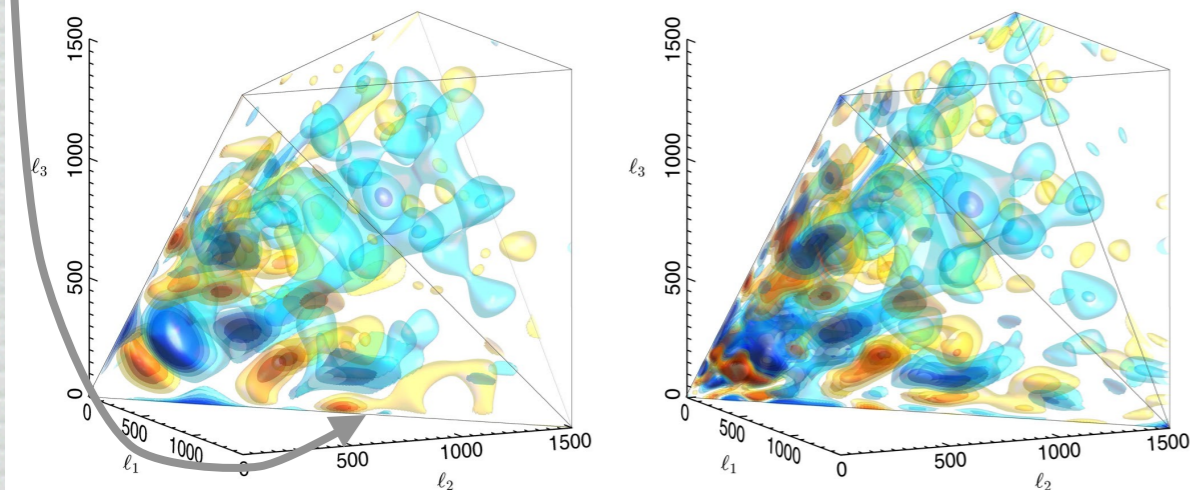
...but nothing primordial



$$f_{NL}^{local} = 2.7 \pm 5.8$$

$$f_{NL}^{equil} = -42 \pm 75$$

$$f_{NL}^{ortho} = -25 \pm 39$$



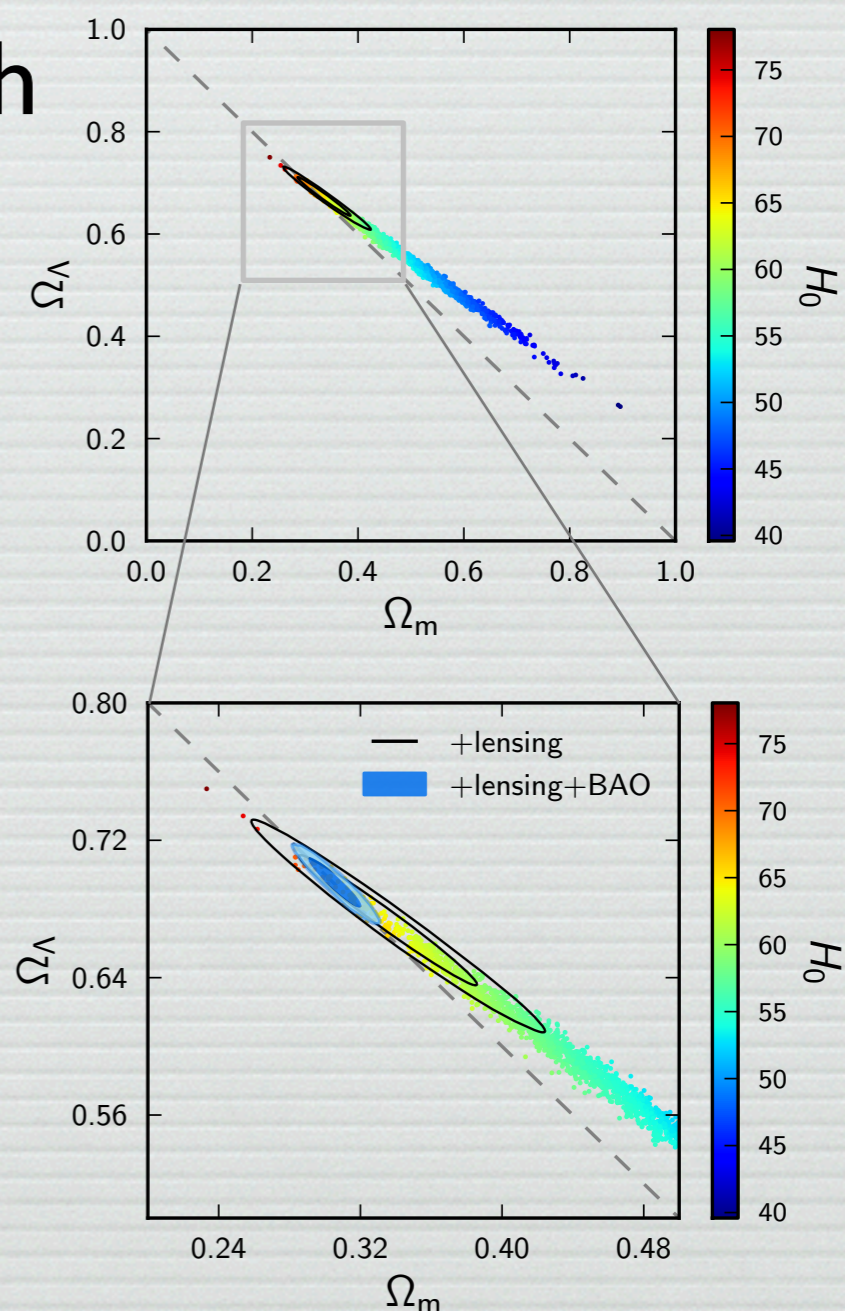
# Fundamental (?) Physics: Inflation

---

- Early period of exponential expansion
  - makes the Universe geometrically flat
    - Prediction: flat Universe ( $\Omega_k=0$ ) ✓
  - takes a “causally connected” region and makes it larger than the observable Universe
    - Prediction: nearly uniform temperature ✓
  - produces fluctuations (quantum randomness on astrophysical scales!)
    - slope of initial power spectrum  $\Rightarrow$  shape of  $C_\ell$
    - Prediction:  $n_s$  a little less than 1 ✓
      - also: nearly Gaussian fluctuations ✓
    - Prediction: gravitational radiation background ?

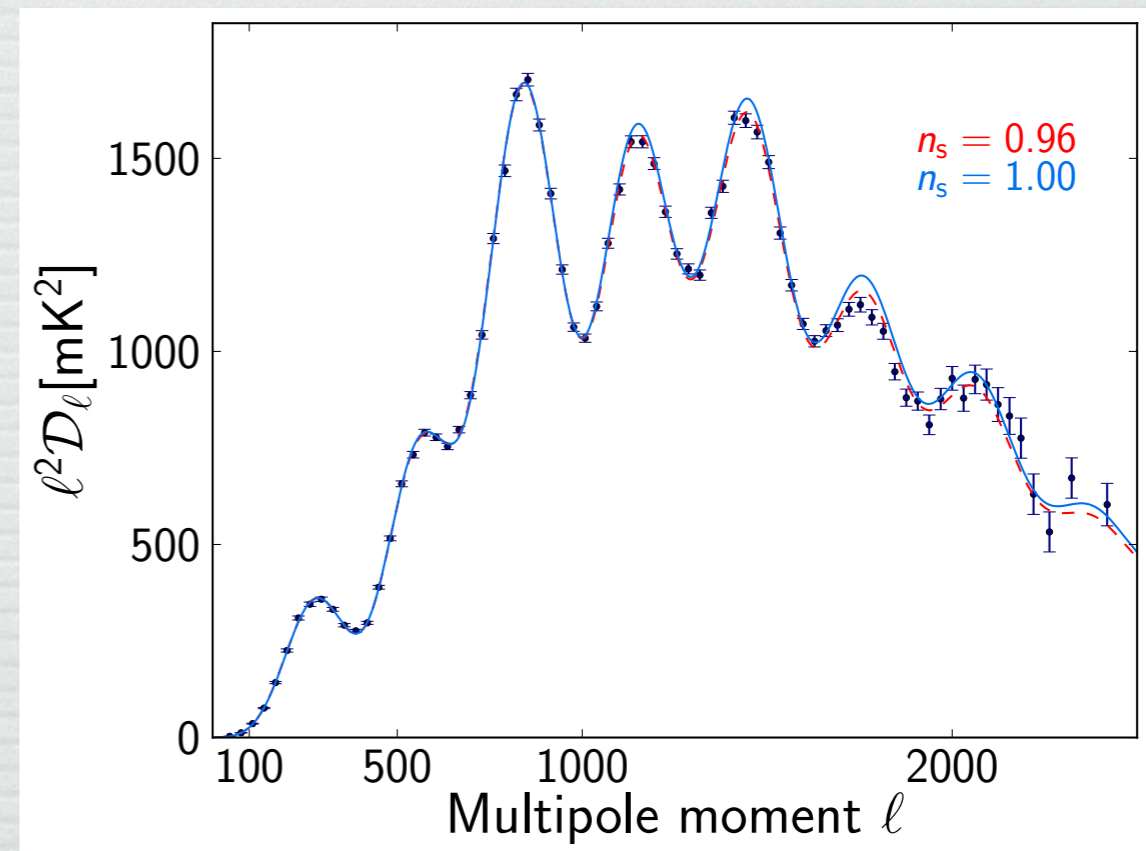
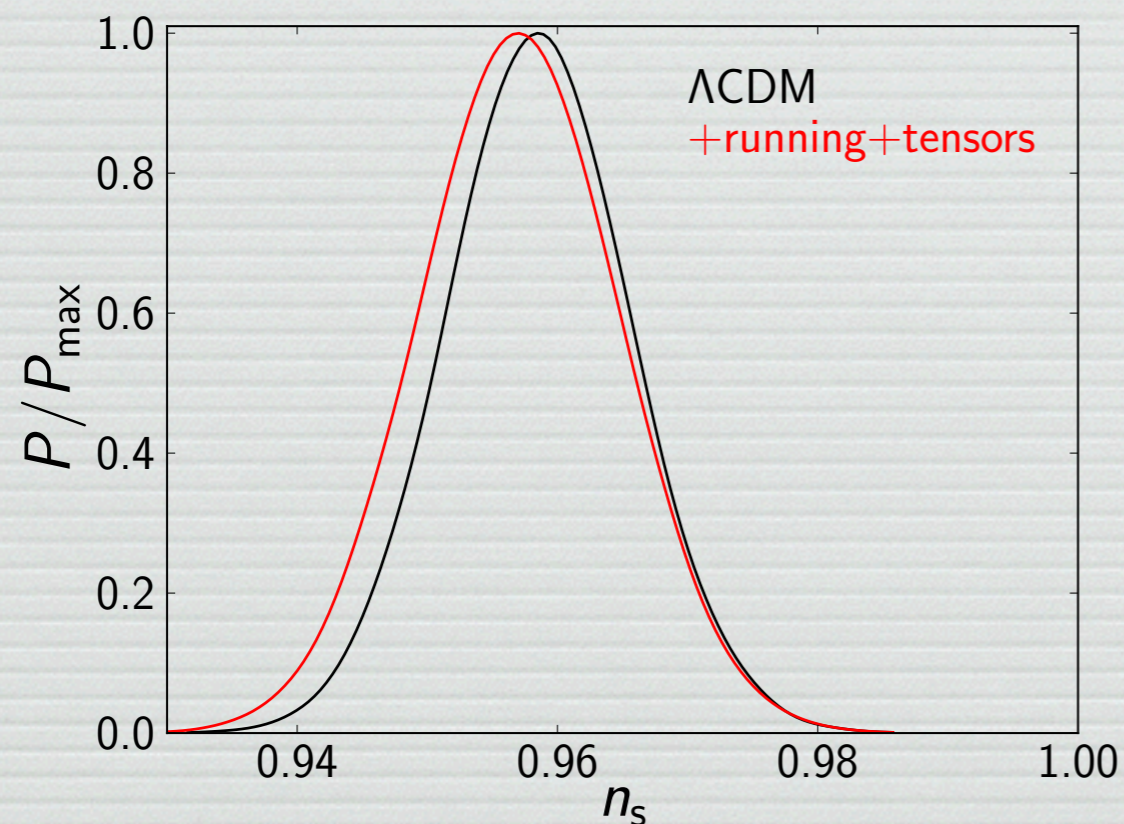
# Inflation: Curvature from the CMB

- With primary CMB alone, cannot determine both  $\Omega_\Lambda$  &  $\Omega_m$  (i.e., curvature)
- *Planck* measures curvature through *lensing*
  - more matter, less dark energy  
⇒ more lensing
    - distorts shape of power spectrum, smears out the small-scale peaks
    - boosts deflection power spectrum
      - about double at  $\Omega_\Lambda=0$
- Even more well-determined when combined with other astrophysical data



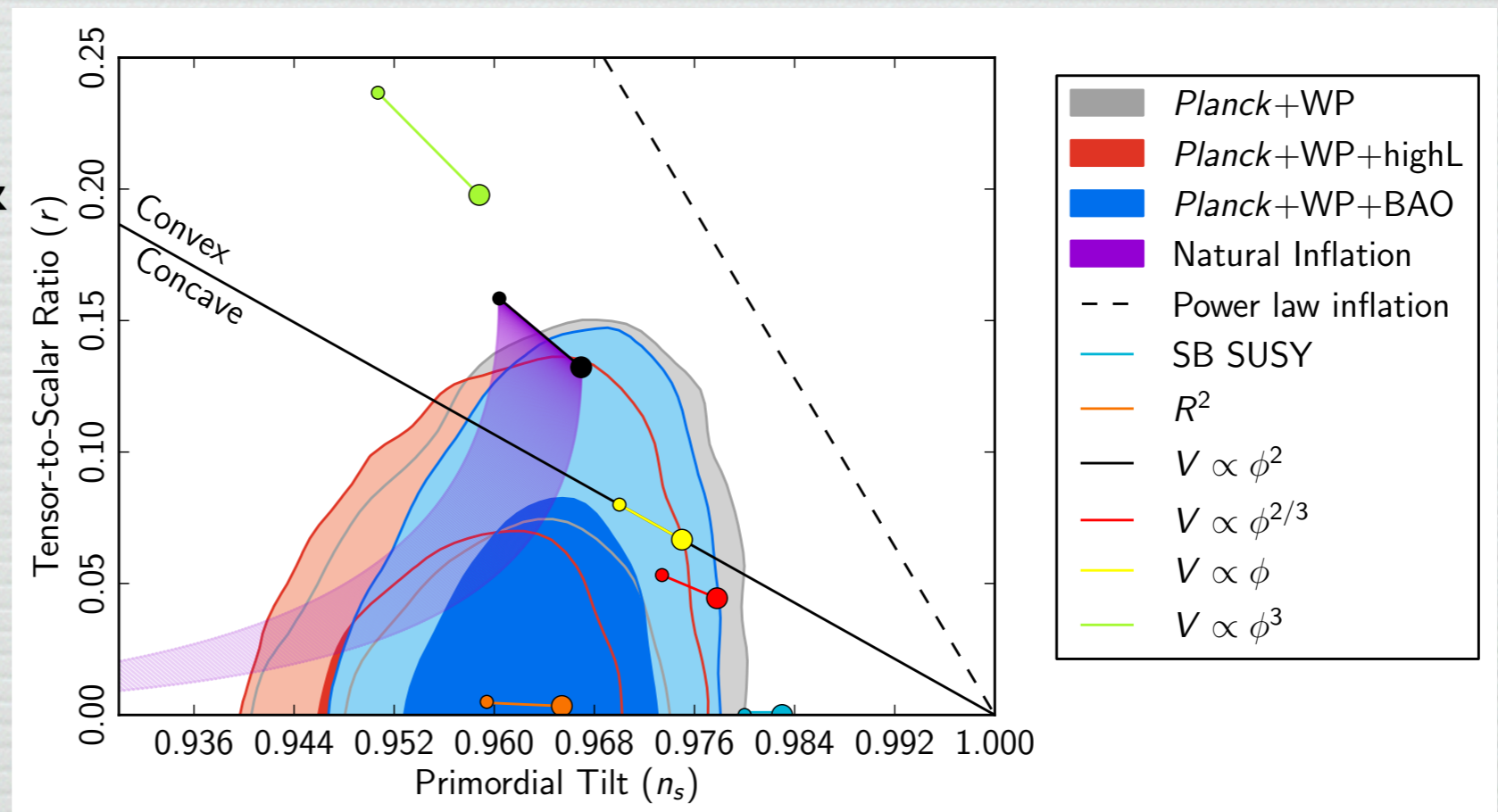
# Inflation: Primordial fluctuations

- $n_s = 0.960 \pm 0.007$
- $>5$  sigma away from  $n_s=1$



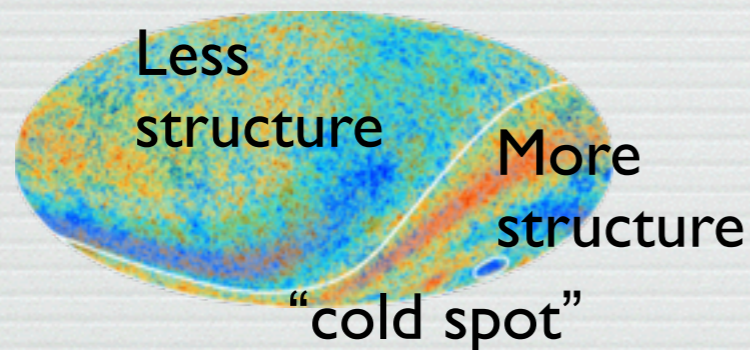
# Inflation: Models

- Simplest models: scalar field  $\phi$  w/very flat potential  $V(\phi)$
- *Planck* constrains specific models of inflation
- More information from the **polarization** of the CMB, which may observe the presence of **gravitational waves** in the early Universe:
  - next year's *Planck* data release
  - next-gen ground & balloon expts (e.g., PolarBear, EBEX, SPIDER,...)



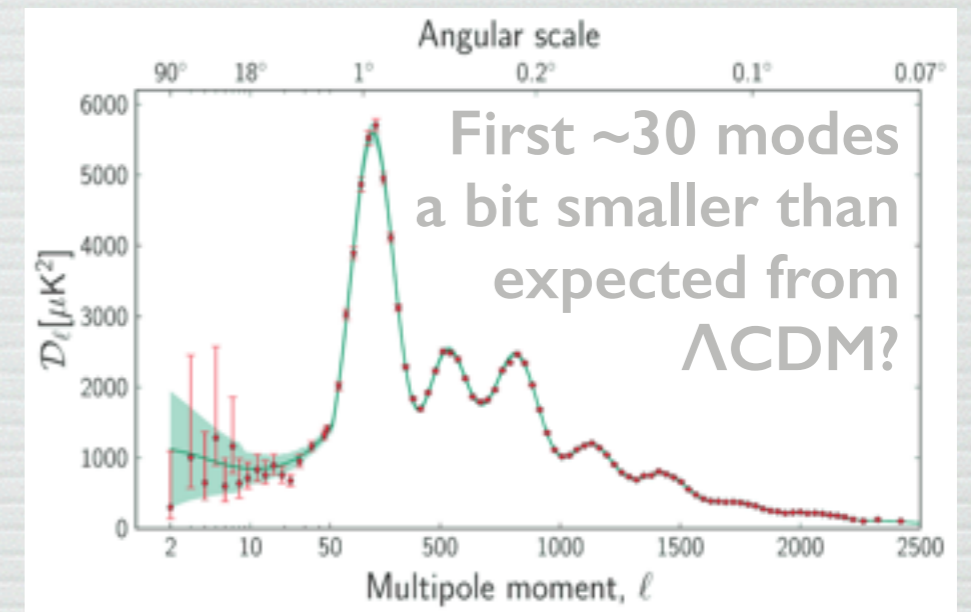
# Consistency of Planck data

- Do the data fit the model?



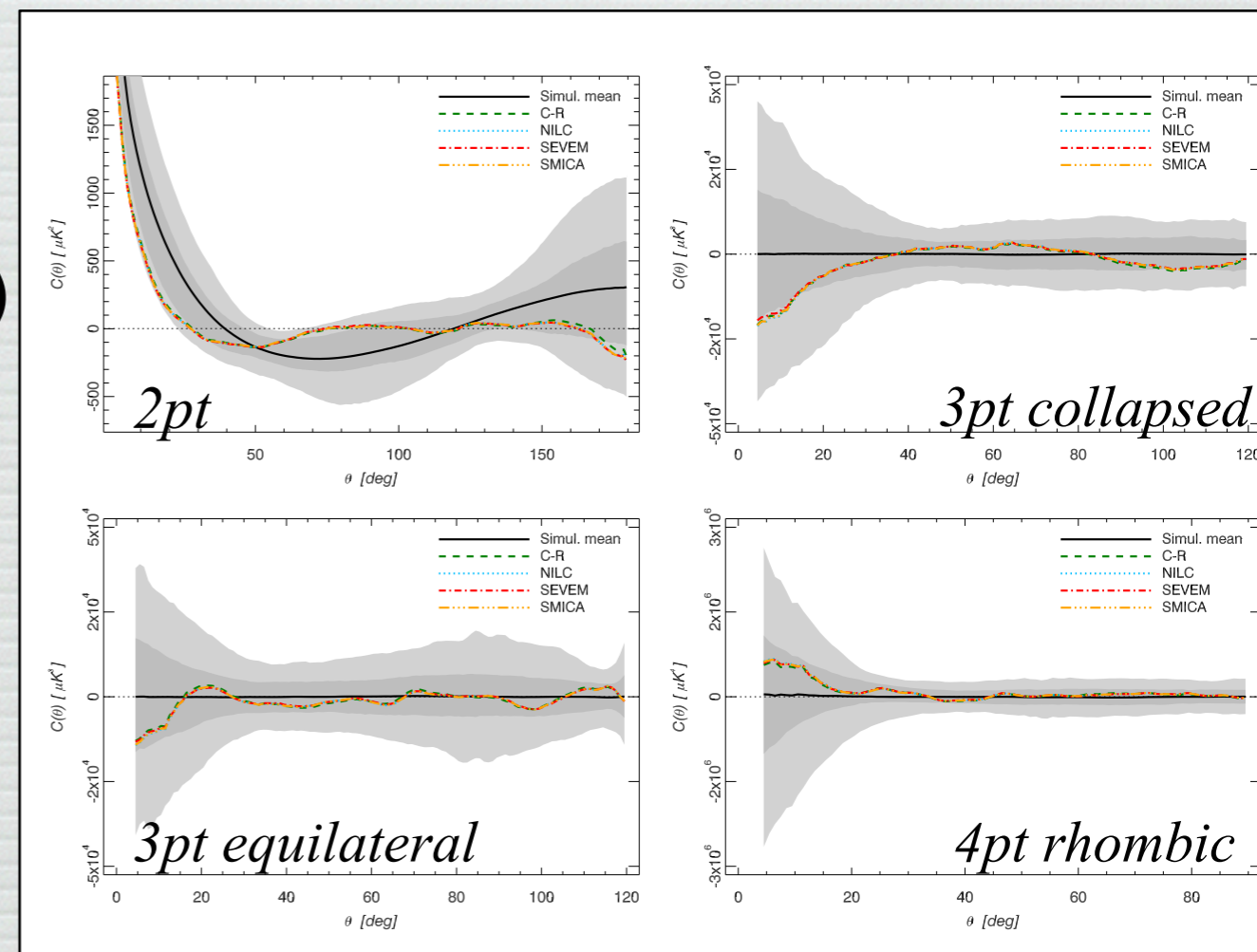
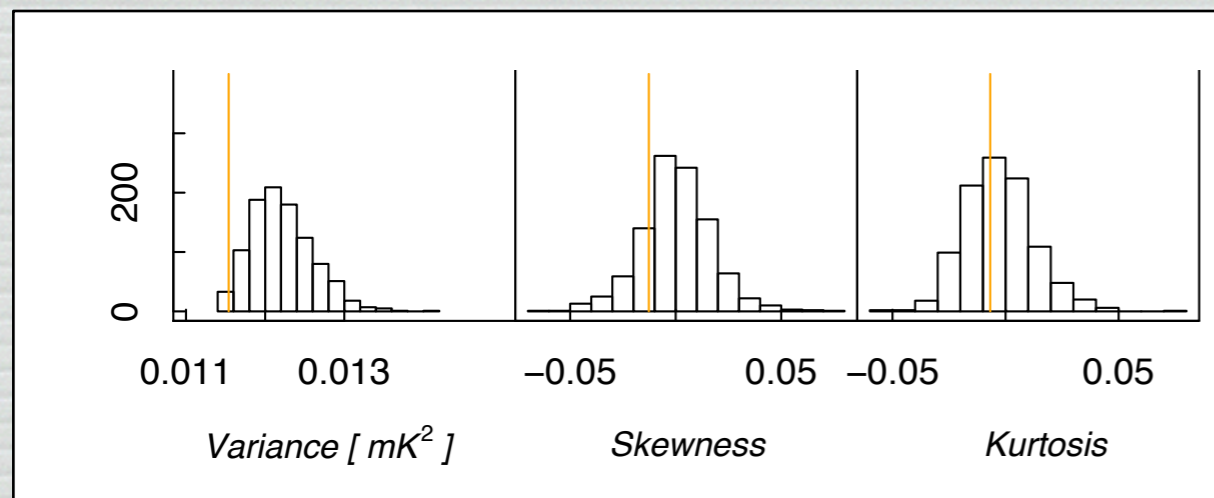
- Do different data agree?

- within *Planck*  $\Delta T/T$ : see above for self-consistency of maps, spectra, parameters
- between *Planck* methods
  - lensing: direct measurement of lensing amplitude  $\sim 1.2$  vs  $1.0$
  - clusters: lower  $\Omega_m$ ,  $\sigma_8$ 
    - at face value, can be [only partially] ameliorated with neutrinos
    - but strong dependence on cluster modelling (e.g., hydrostatic bias)
- Parameter details: e.g., CMB measurements of  $H_0$  a few  $\sigma$  low vs cosmic distance ladder
  - astrophysical measurements seem to be coming down *a posteriori*?



# Testing assumptions

- We have been calculating the posterior  $P(\Omega_b h^2, \Omega_c h^2, \theta_{MC}, \tau, n_s, A_s \mid \text{Planck, I})$
- Background information “I”
  - (testable) assumptions:
    - LCDM in general
    - gaussianity, isotropy (+lensing)
    - by some measures, it obeys these assumptions very well

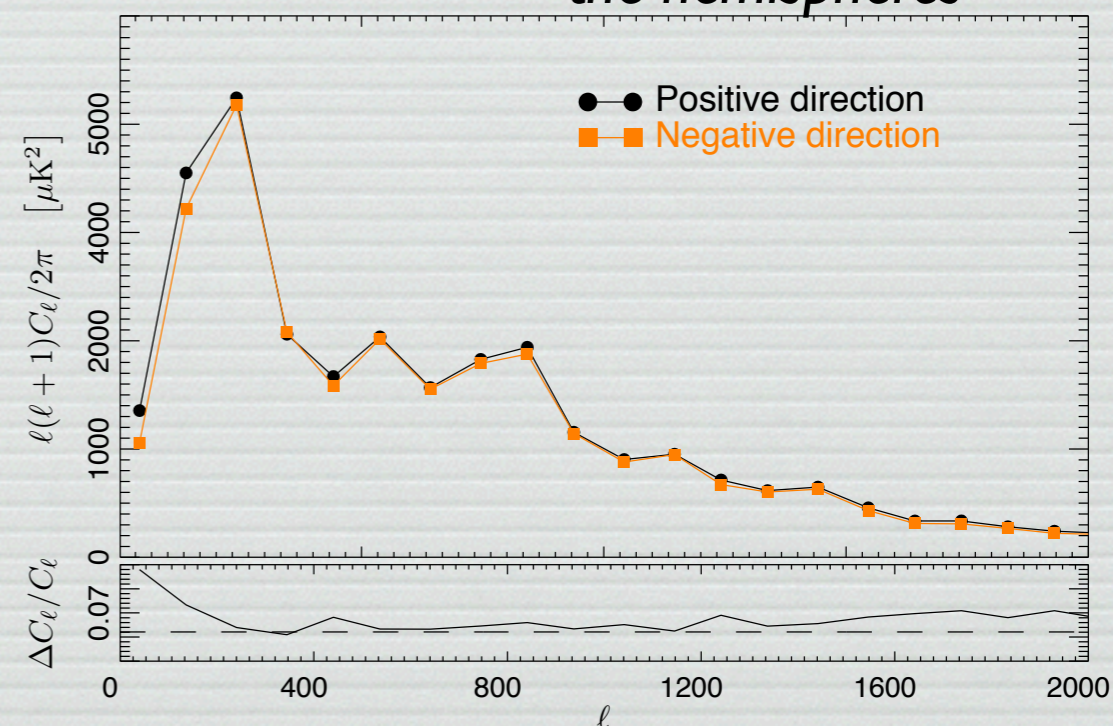
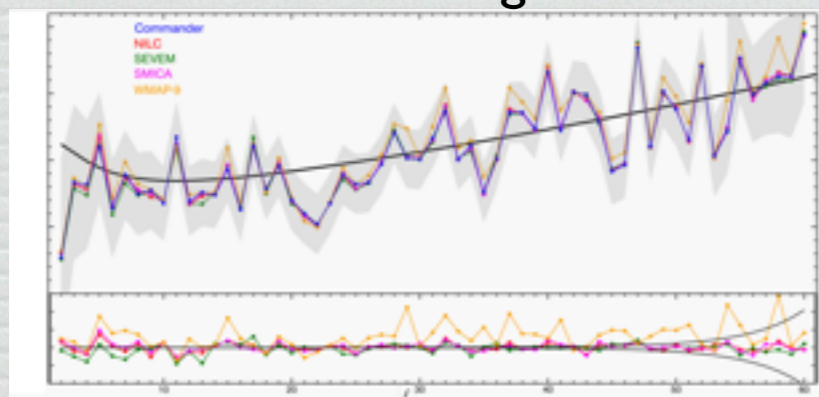


# Large-scale anisotropy

- Hemispherical differences: how can we arrange anisotropy on the scale of the horizon?
  - initial conditions: anisotropic inflation?
  - the large-scale structure of spacetime
    - change the geometry: Bianchi
      - homogeneous + anisotropic spacetimes
    - change the topology

*Small (but statistically significant) difference between the power in the hemispheres*

*Overall low power at large scales*

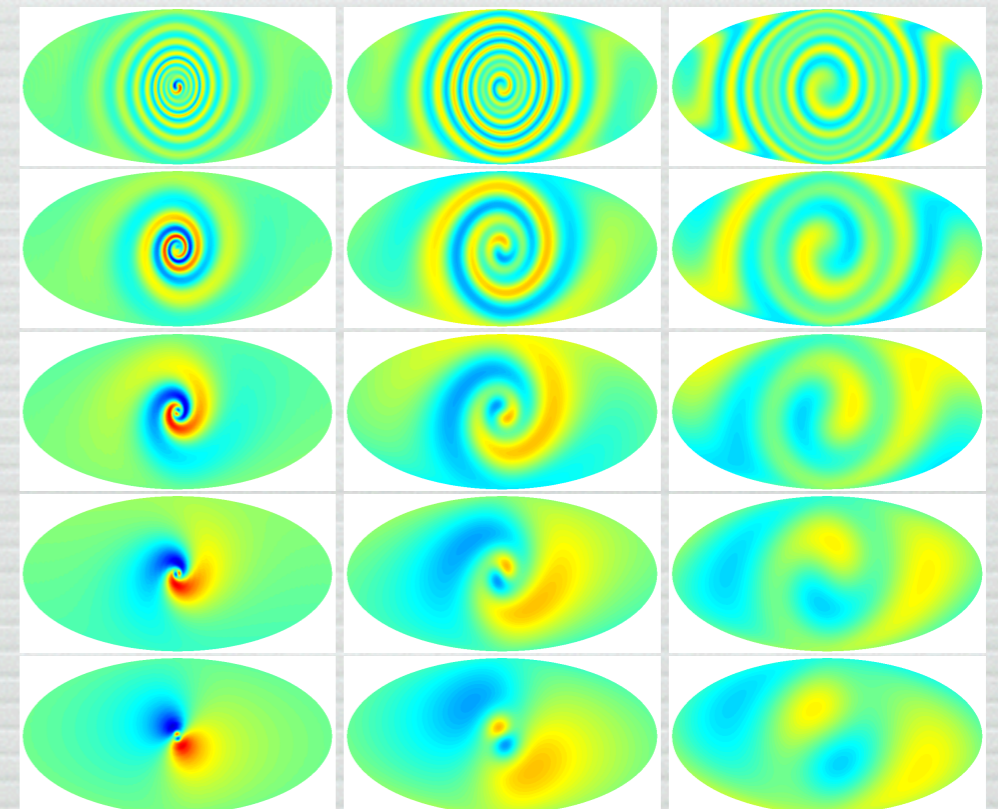


# Bianchi Models

- Homogeneous, anisotropic spaces
- $VII_h$ : global shear and rotation
  - parameter  $h$  relates vorticity  $\omega_i$  to shear  $\sigma_{ij}$ ,  $\Omega_{\text{tot}}$

$$\left(\frac{\omega}{H}\right)_0 = \frac{(1+h)^{1/2}(1+9h)^{1/2}}{6h} \frac{1-\Omega_{\text{tot}}}{\Omega_{\text{tot}}} \sqrt{\left(\frac{\sigma_{12}}{H}\right)_0^2 + \left(\frac{\sigma_{13}}{H}\right)_0^2}$$

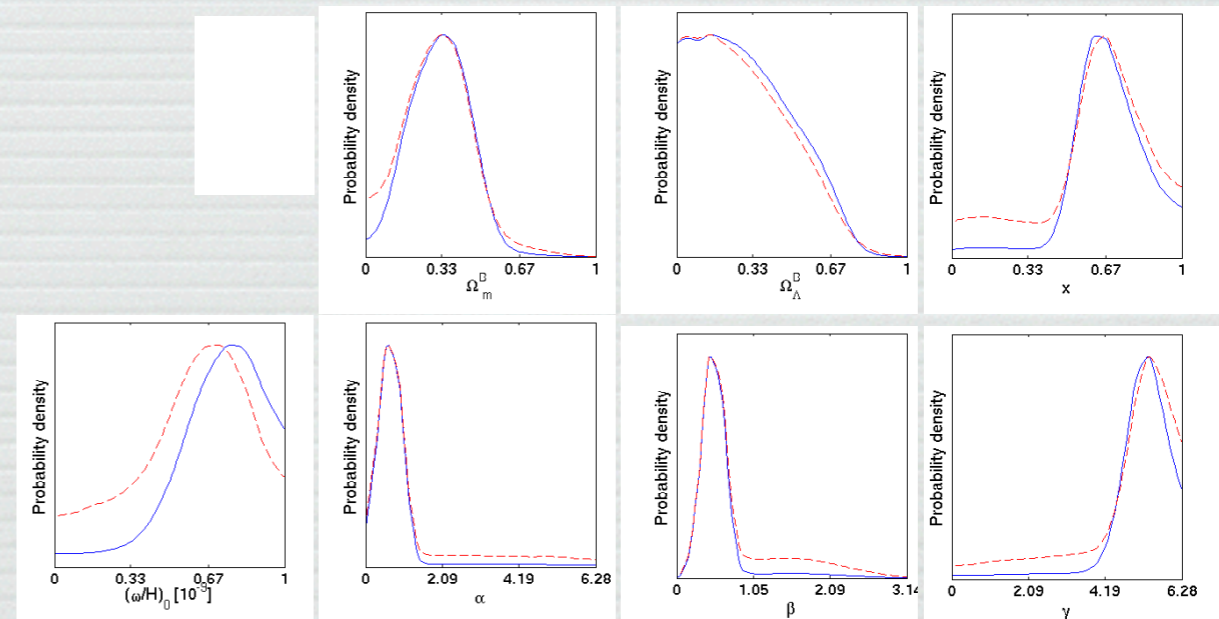
- Focusing induces specific pattern of temperature anisotropy on large scales
- Full likelihood calculation (Gaussian added to deterministic template)
  - consistent cosmology very low likelihood



# Bianchi Models

## Flat-decoupled

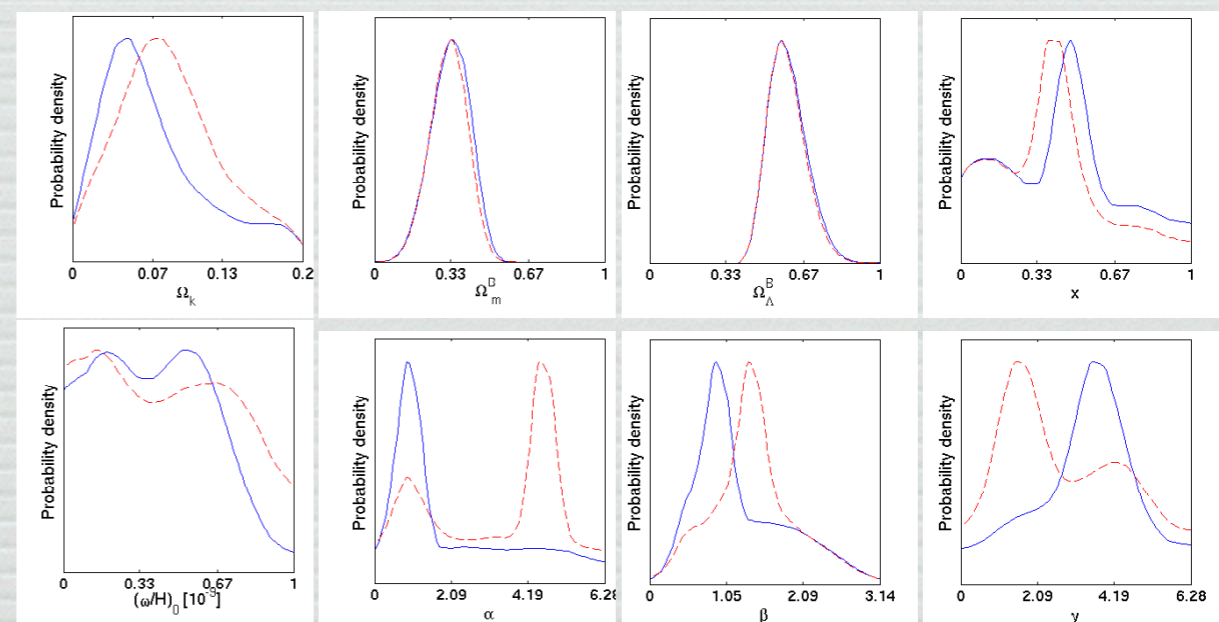
Bianchi Parameter	SMICA		SEVEM	
	MAP	Mean	MAP	Mean
$\Omega_m^B$	0.38	$0.32 \pm 0.12$	0.35	$0.31 \pm 0.15$
$\Omega_\Lambda^B$	0.20	$0.31 \pm 0.20$	0.22	$0.30 \pm 0.20$
$x$	0.63	$0.67 \pm 0.16$	0.66	$0.62 \pm 0.23$
$(\omega/H)_0$	$8.8 \times 10^{-10}$	$(7.1 \pm 1.9) \times 10^{-10}$	$9.4 \times 10^{-10}$	$(5.9 \pm 2.4) \times 10^{-10}$
$\alpha$	$38.8^\circ$	$51.3^\circ \pm 47.9^\circ$	$40.5^\circ$	$77.4^\circ \pm 80.3^\circ$
$\beta$	$28.2^\circ$	$33.7^\circ \pm 19.7^\circ$	$28.4^\circ$	$45.6^\circ \pm 32.7^\circ$
$\gamma$	$309.2^\circ$	$292.2^\circ \pm 51.9^\circ$	$317.0^\circ$	$271.5^\circ \pm 80.7^\circ$



(a) Flat-decoupled-Bianchi model.

## Open-coupled

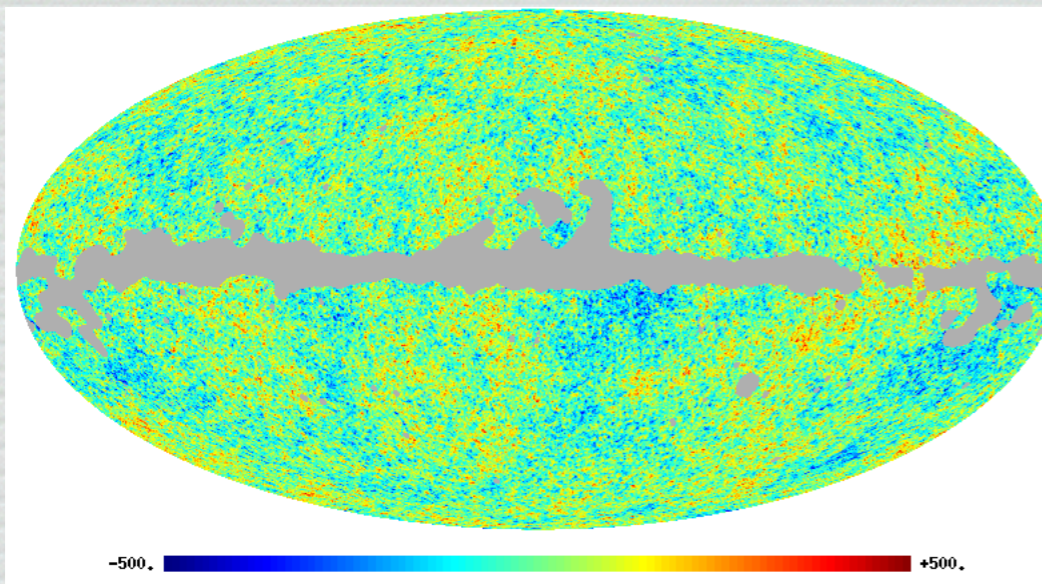
Bianchi Parameter	SMICA		SEVEM	
	MAP	Mean	MAP	Mean
$\Omega_k$	0.05	$0.07 \pm 0.05$	0.09	$0.08 \pm 0.04$
$\Omega_m^B$	0.41	$0.33 \pm 0.07$	0.41	$0.32 \pm 0.07$
$\Omega_\Lambda^B$	0.55	$0.60 \pm 0.07$	0.50	$0.59 \pm 0.07$
$x$	0.46	$0.44 \pm 0.24$	0.38	$0.39 \pm 0.22$
$(\omega/H)_0$	$5.9 \times 10^{-10}$	$(4.0 \pm 2.4) \times 10^{-10}$	$9.3 \times 10^{-10}$	$(4.5 \pm 2.8) \times 10^{-10}$
$\alpha$	$57.4^\circ$	$122.5^\circ \pm 96.0^\circ$	$264.1^\circ$	$188.6^\circ \pm 98.7^\circ$
$\beta$	$54.1^\circ$	$70.8^\circ \pm 35.5^\circ$	$79.6^\circ$	$81.1^\circ \pm 31.7^\circ$
$\gamma$	$202.6^\circ$	$193.5^\circ \pm 77.4^\circ$	$90.6^\circ$	$160.4^\circ \pm 91.1^\circ$



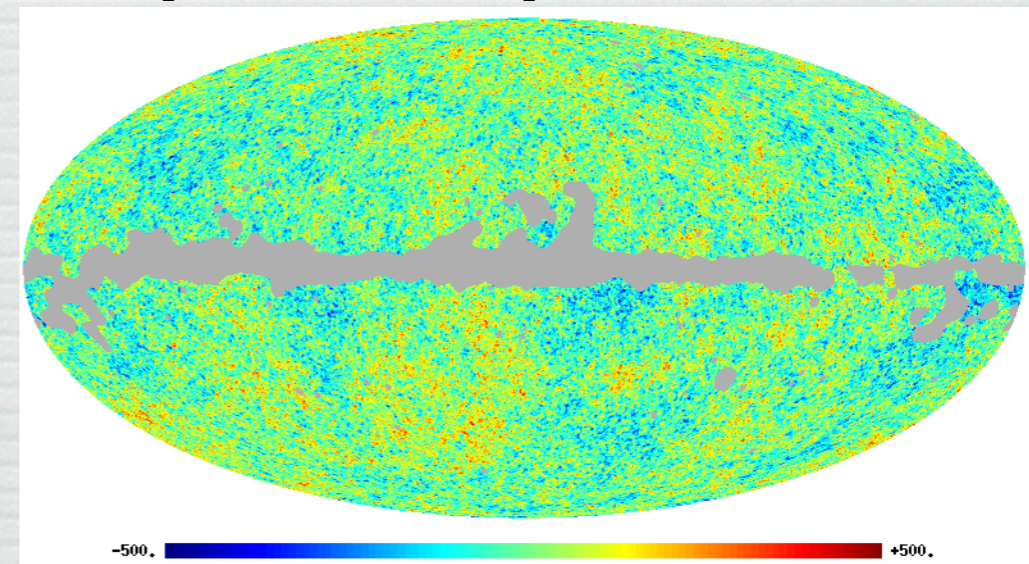
(b) Open-coupled-Bianchi model.

Flat-coupled:  $\omega_0/H_0 < 8.1 \times 10^{-10}$  (95%)

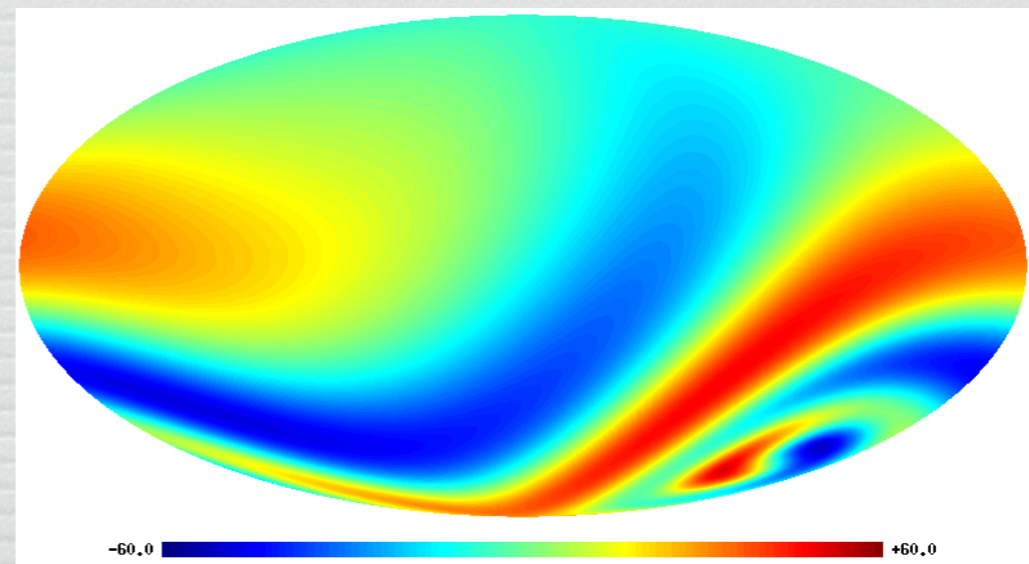
- 
- The Bianchi VII<sub>h</sub> uncoupled “model” accounts for much of the hemispherical asymmetry

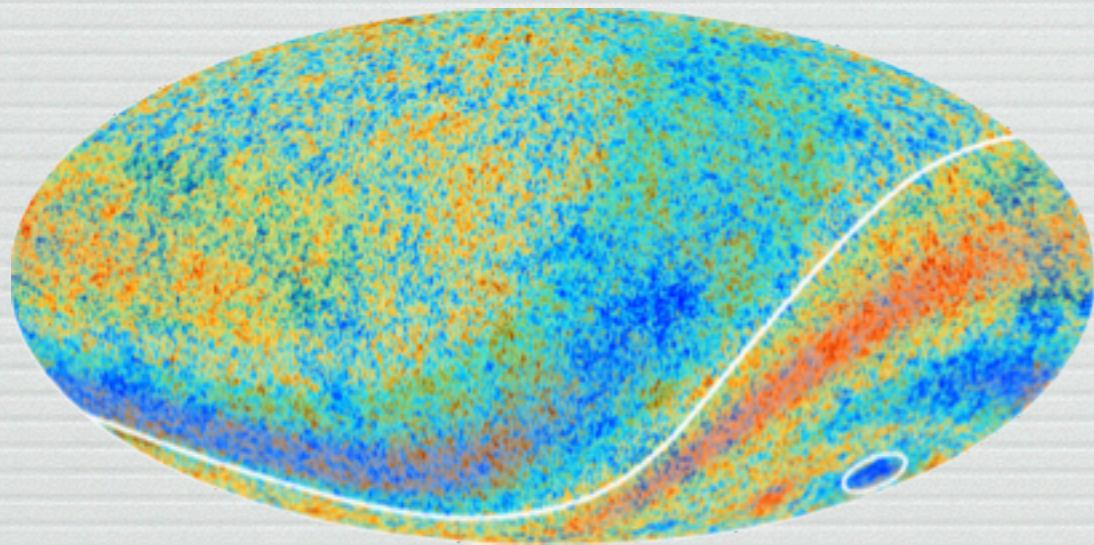


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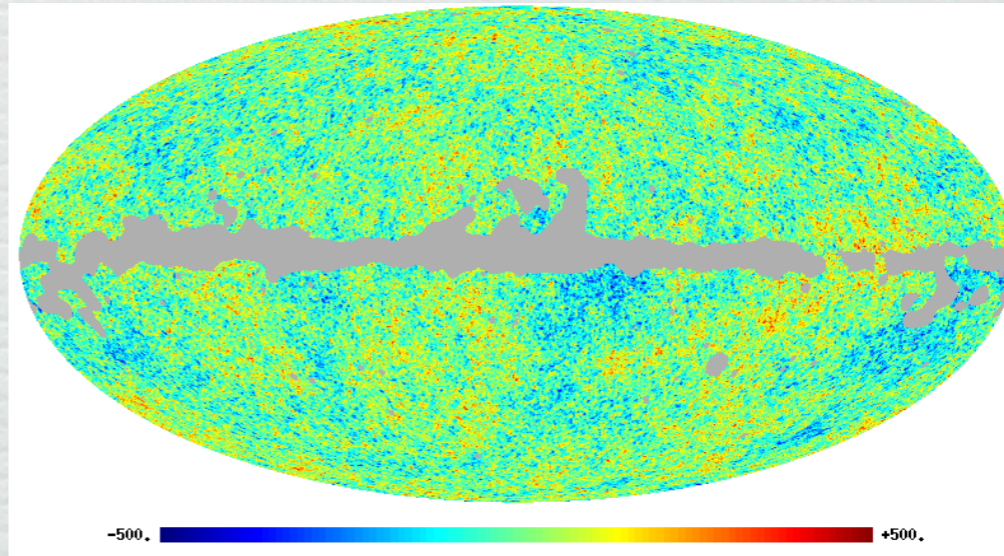


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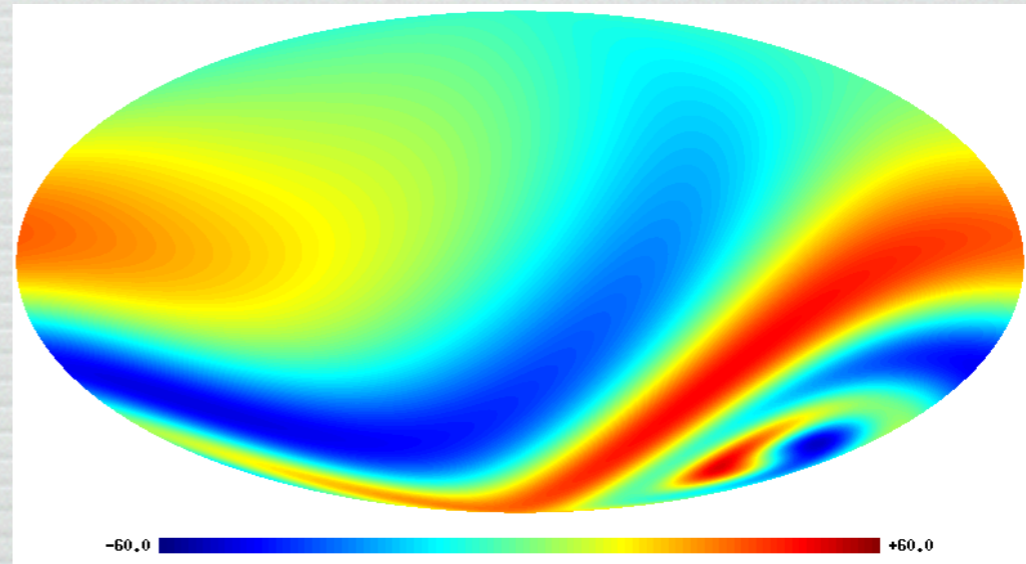




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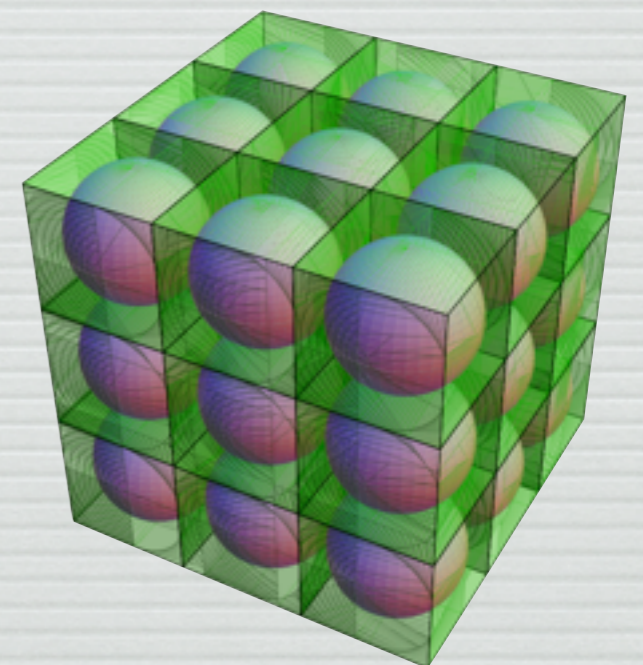
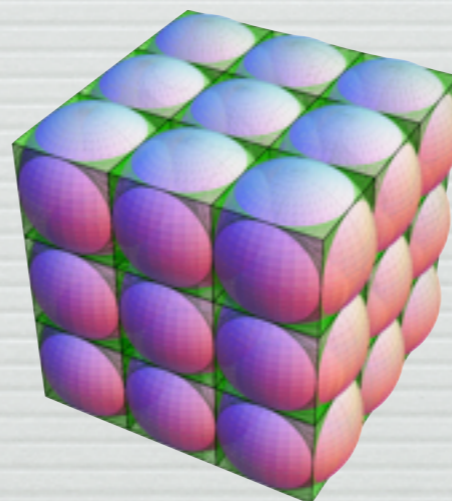
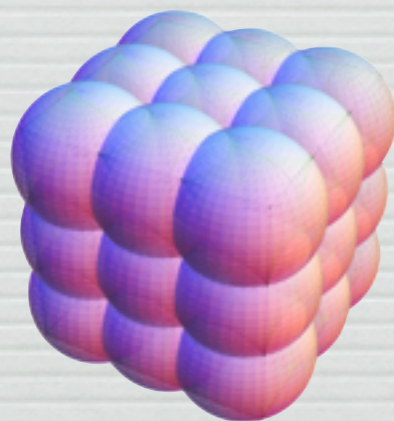
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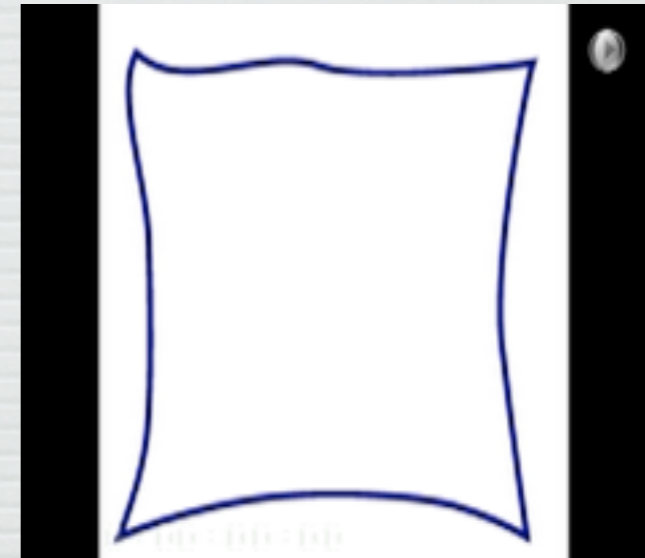
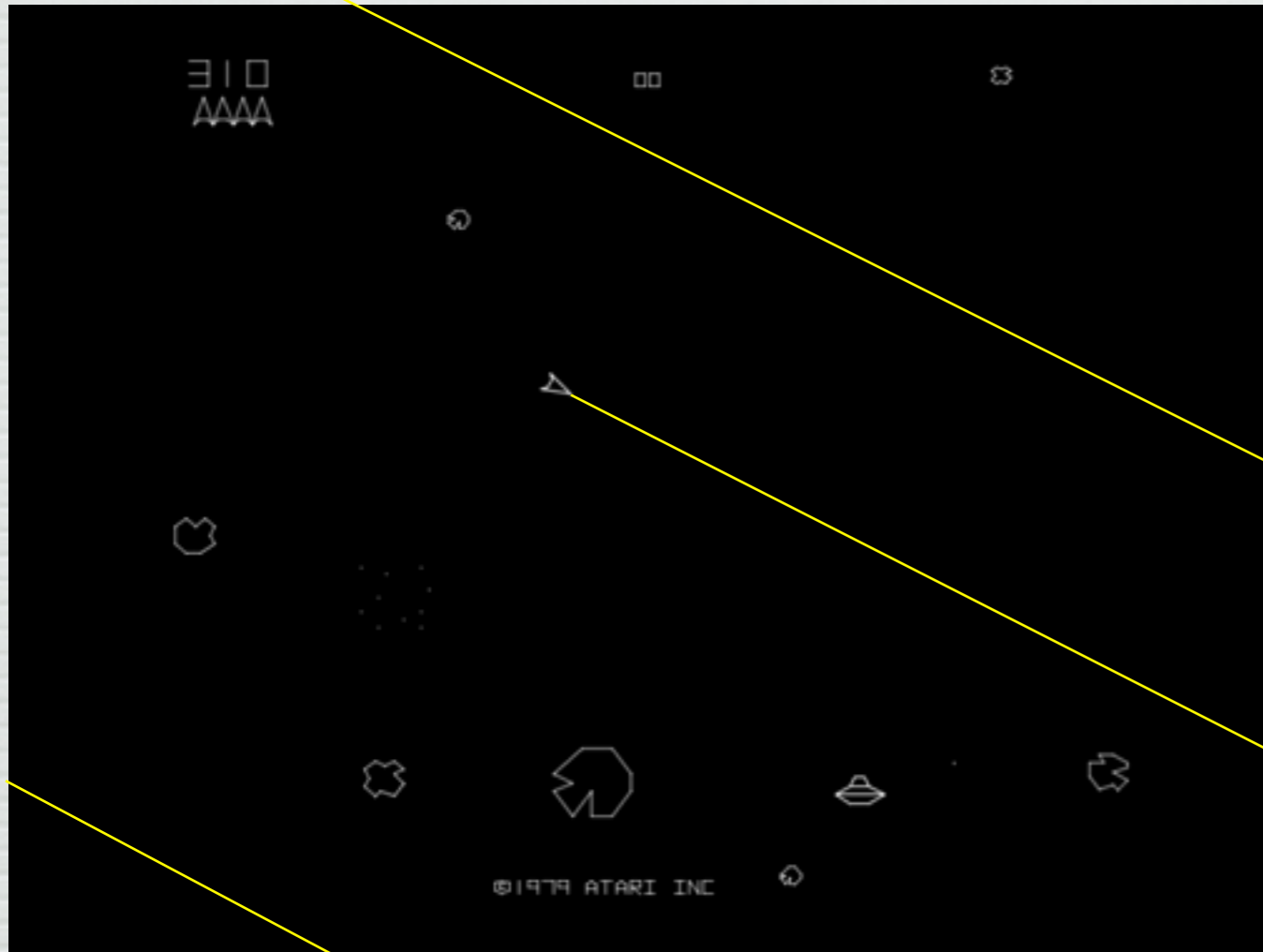
# Fundamental Physics: The shape of the Universe

---

- General relativity determines the **curvature** of the Universe, but not its **topology** (holes and handles)
- Most theories of **quantum gravity** (and quantum cosmology) predict **topological change** on small scales and at early times.
- Does this have cosmological implications?
  - E.G., small universe  $\Rightarrow$  fewer large-scale modes available  $\Rightarrow$  low power on large scales?



# Topology in a flat “universe”

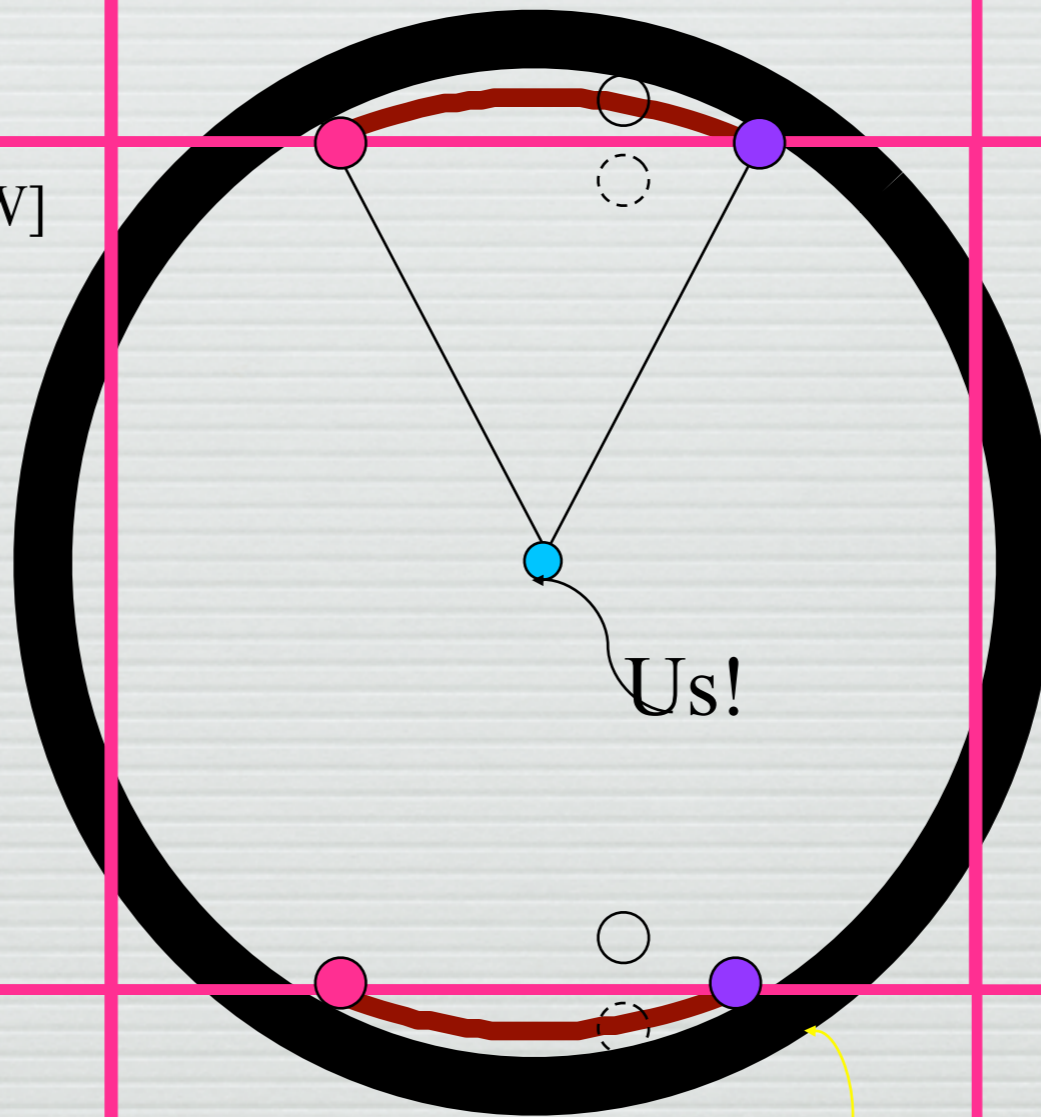


“tiling the plane”

Don't *need* to “embed” the square to have a connected topology.

# Measuring Topology with the CMB

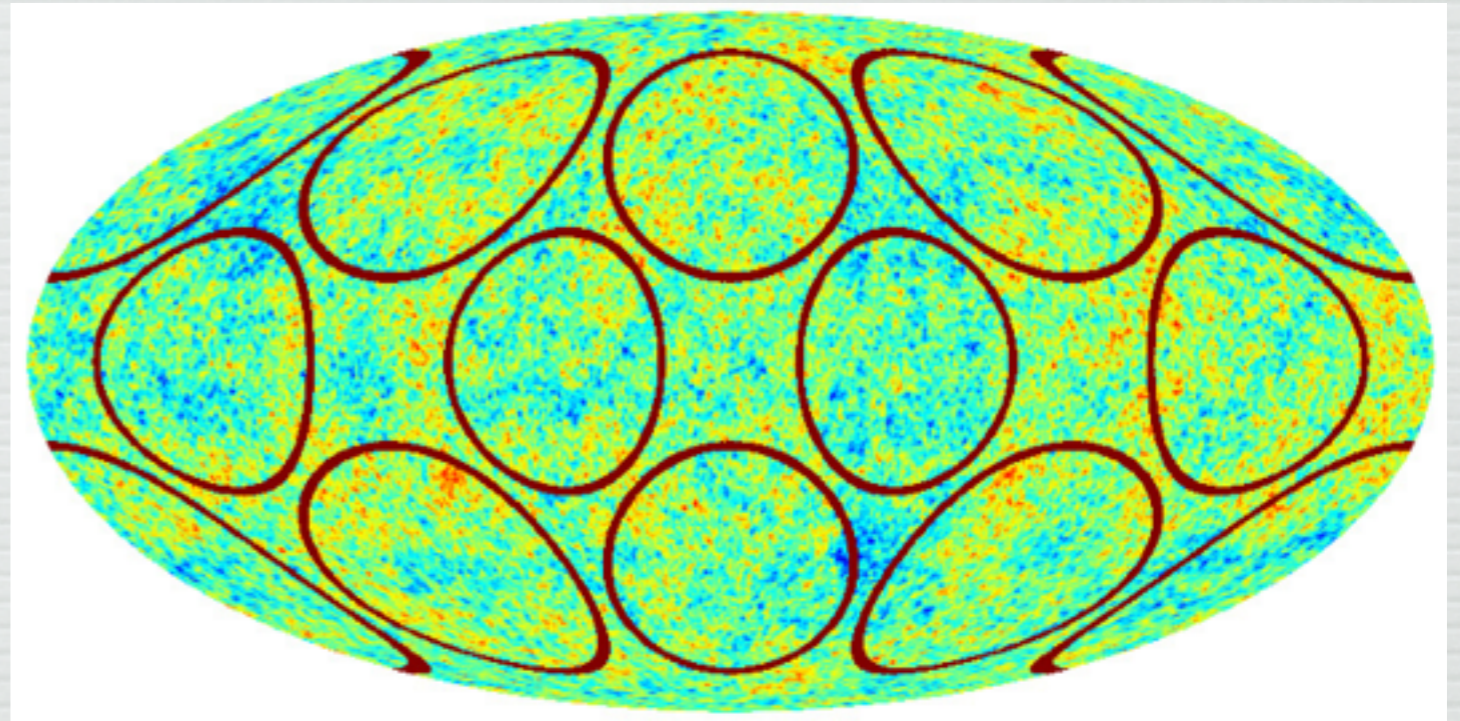
- Perfect correlation [of SW]
- “circles in the sky”
- finite-lag correlation



Last Scattering Surface

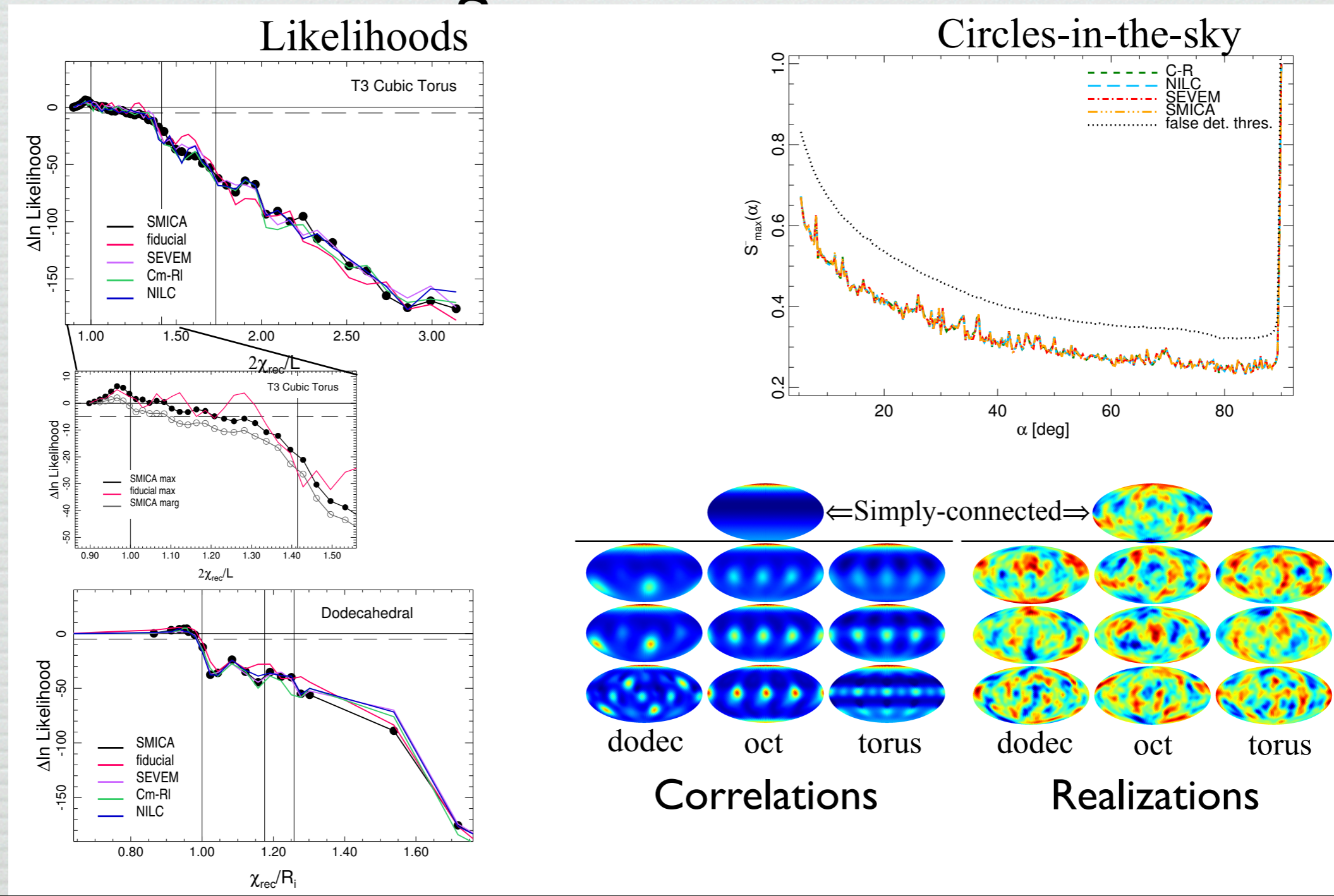
# Topology from Planck

- “Matched circles” in a simulated Universe:
- When *topological scale*  $\approx$  *Horizon scale*, induce anisotropic correlations (and suppress power) on large scales
- More powerful (Bayesian) methods take advantage of full correlation structure
- Alas, not found... but we limit the size of the “fundamental cube” to be greater than the size of the surface we observe with the CMB:
  - side  $L \gtrsim 26$  Gpc (85 billion light years!)



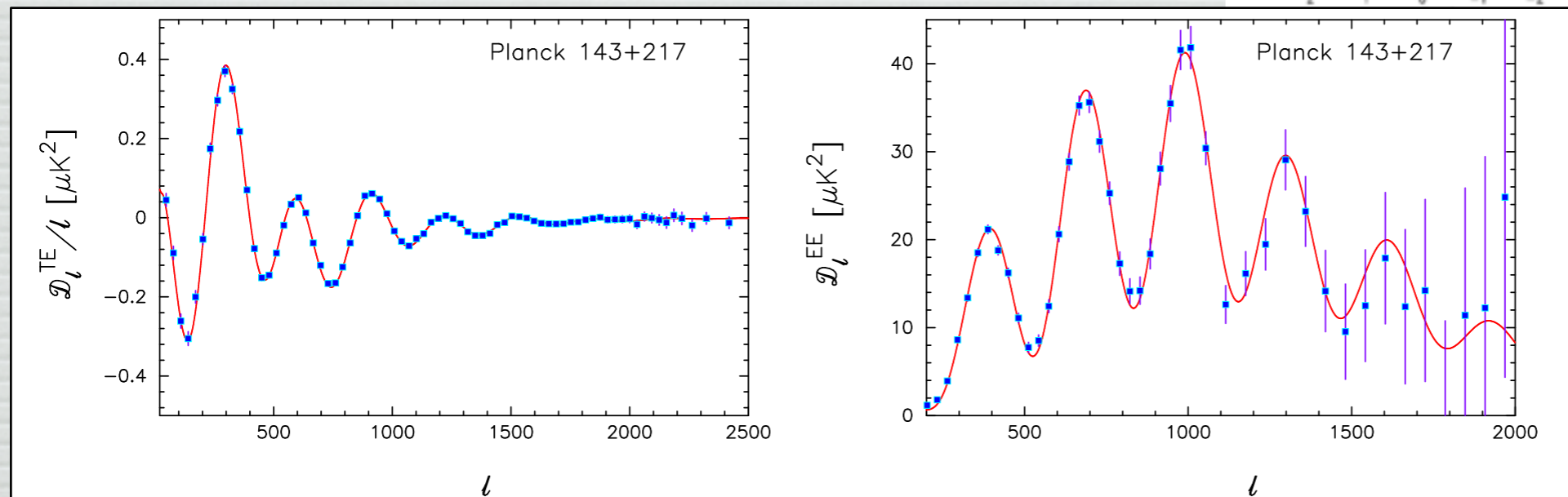
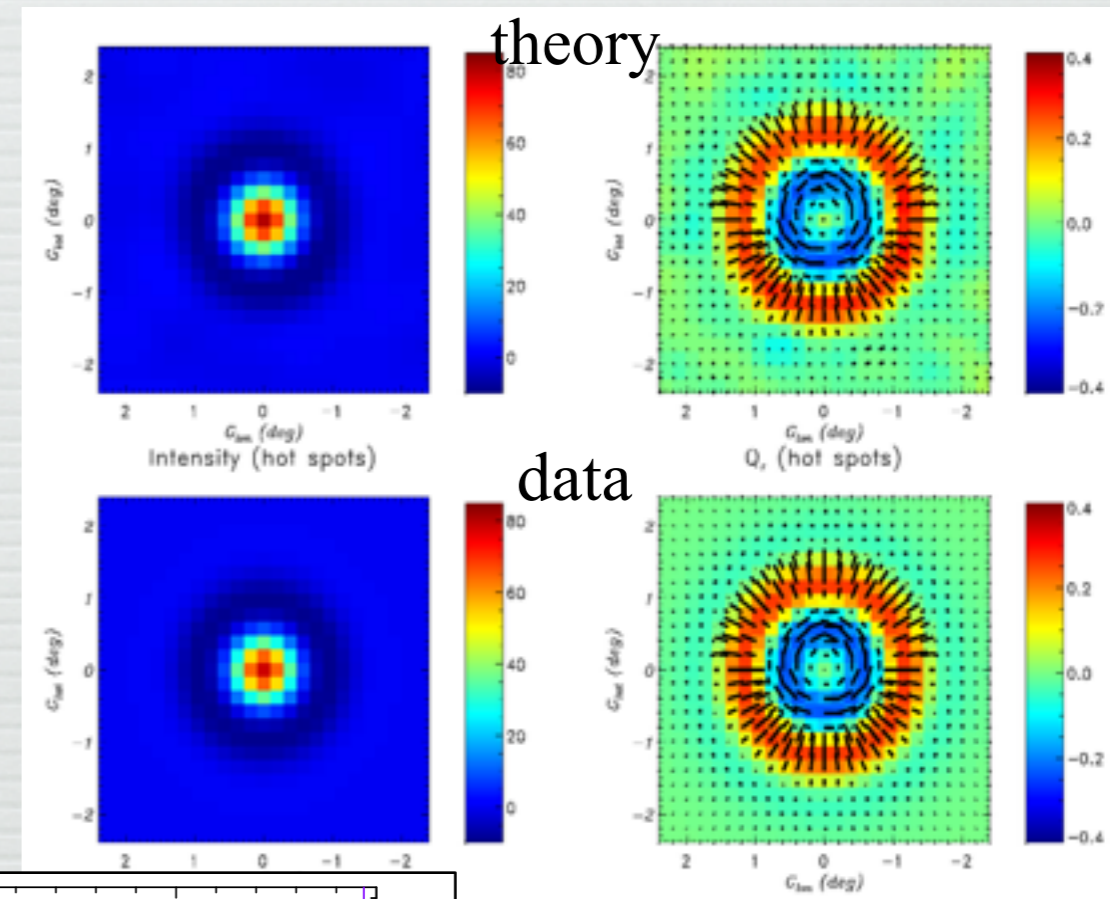
# Topology: results

- No strong evidence for topology on the scale of the last-scattering surface



# Planck 2014-

- Next up: twice as much intensity data (30 vs 15 months) and **polarization**.
- **Preview**: at small/intermediate scales, polarization and intensity correlation exactly as predicted by theory.

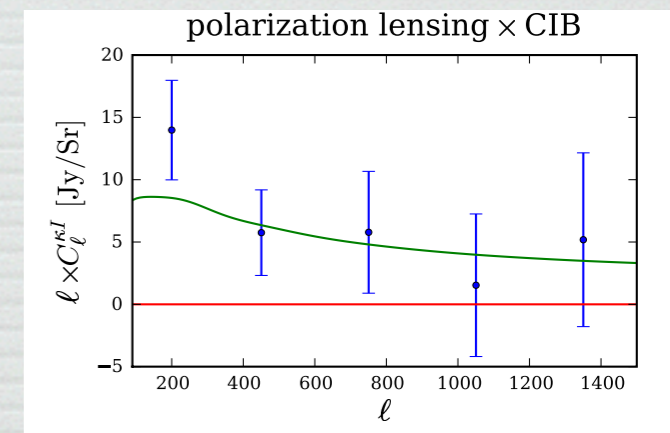


**Fig. 11.** Planck TE (left) and EE spectra (right) computed as described in the text. The red lines show the polarization spectra from the base  $\Lambda$ CDM Planck+WP+highL model, which is fitted to the TT data only.

# Post-Planck

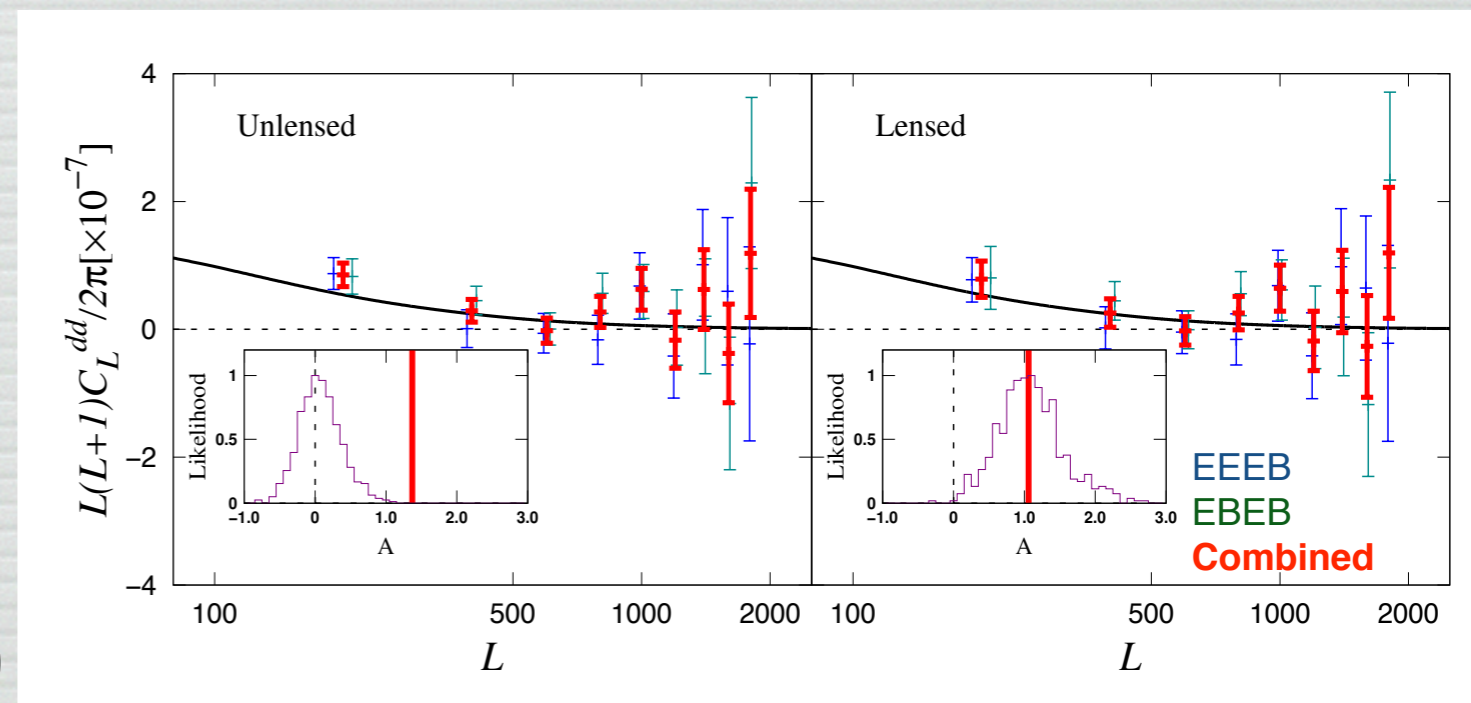
□ Polarization: Starting to get the first results from kilo-pixel CMB detector arrays — sufficient to detect lensing conversion of  $E \rightarrow B$

■ Cross-correlation with large-scale structure (SPTPol: Hanson et al; ACT: Hand et al; Polarbear)



■  $\langle EEEB \rangle$  &  $\langle EBEB \rangle$  (Polarbear)

■ Still no detection of primordial B modes (gravitational radiation)



# Hanson et al, *SPTPOL*, arXiv:1307.5830

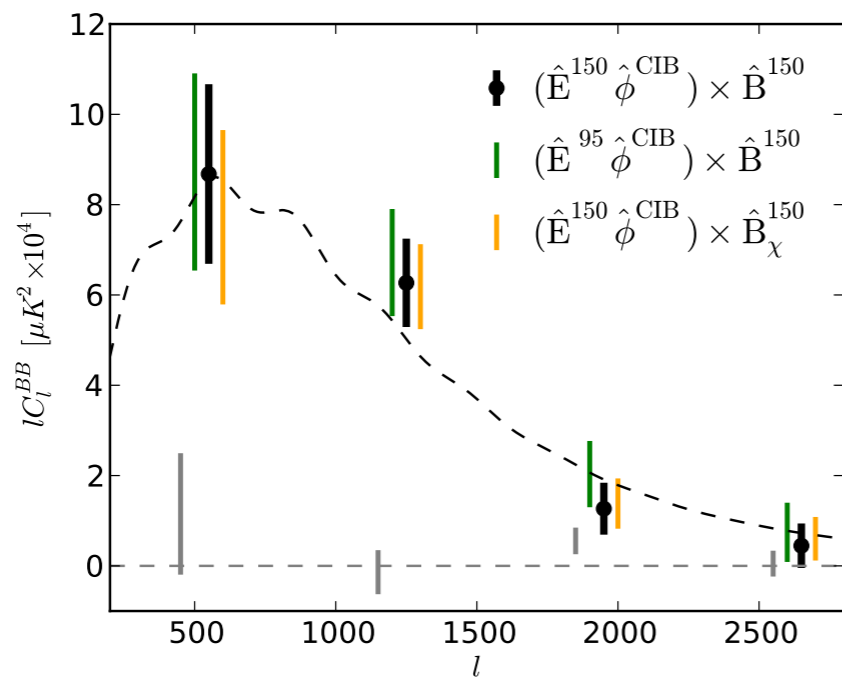


FIG. 2: (Black, center bars): Cross-correlation of the lensing  $B$  modes measured by SPTpol at 150 GHz with lensing  $B$  modes inferred from CIB fluctuations measured by *Herschel* and  $E$  modes measured by SPTpol at 150 GHz; as shown in Fig. 1. (Green, left-offset bars): Same as black, but using  $E$  modes measured at 95 GHz, testing both foreground contamination and instrumental systematics. (Orange, right-offset bars): Same as black, but with  $B$  modes obtained using the  $\chi_B$  procedure described in the text rather than our fiducial Wiener filter. (Gray bars): Curl-mode null test as described in the text. (Dashed black curve): Lensing  $B$ -mode power spectrum in the fiducial cosmological model.

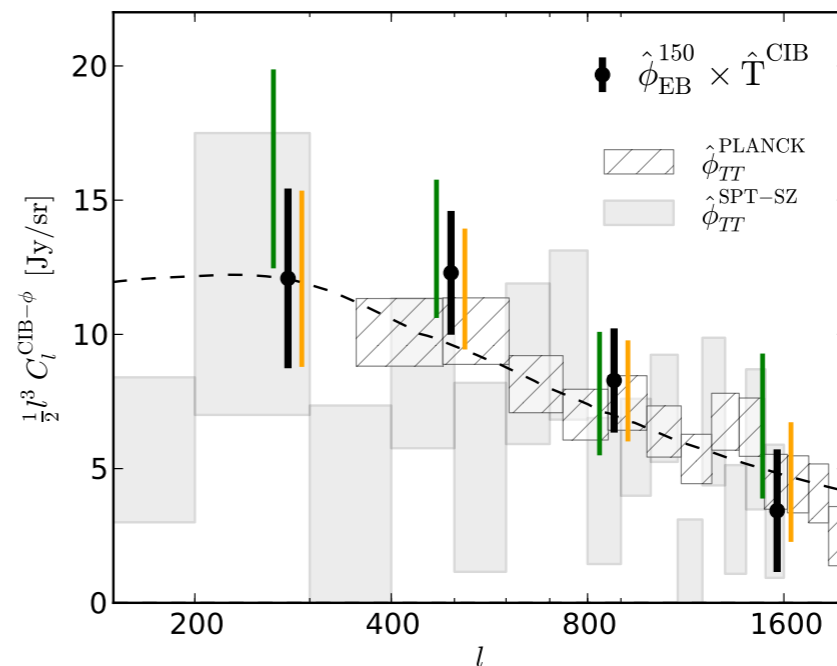


FIG. 3: “Lensing view” of the  $EB\phi$  correlation plotted in Fig. 2, in which we cross-correlate an  $EB$  lens reconstruction from SPTpol data with CIB intensity fluctuations measured by *Herschel*. Left green, center black, and right orange bars are as described in Fig. 2. Previous analyses using temperature-based lens reconstruction from *Planck* [26] and SPT-SZ [22] are shown with boxes. The results of [26] are at a nominal wavelength of  $550 \mu\text{m}$ , which we scale to  $500 \mu\text{m}$  with a factor of 1.22 [37]. The dashed black curve gives our fiducial model for  $C_l^{\text{CIB}-\phi}$  as described in the text.

# Conclusions

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- *Planck* data support a **standard  $\Lambda$ CDM cosmology**
  - flat FRW
  - perturbations:
    - nearly scale-invariant adiabatic
    - Gaussian + linear & nonlinear evolution
  - $\Lambda$ -like acceleration
- Some anomalies/inconsistencies remain (as might be expected)
- **More data** in 2014-15 from *Planck* and other experiments
  - especially polarization

} inflation?

# Extra Stuff

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- Lensing
- Neutrinos
- Bianchi

# Particle physics with the whole Universe

□ Neutrinos are very light  $\Rightarrow$  act like radiation

- affect expansion rate at early times
- affect growth of structure at late times

□ Still relativistic at recombination

□ Improved limit from lensing:  
more mass = less lensing

- $\Sigma m_\nu < 0.66$  eV (95%, *Planck*+WVP+highL)

- $\Sigma m_\nu < 0.23$  eV (+BAO)

- However, adding *Planck* lensing spectrum increases limit to  $<0.85$  eV.

- $N_{\text{eff}} = 3.36 \pm 0.34$  (68%, *Planck*+WVP+highL)

- $N_{\text{eff}} = 3.30 \pm 0.27$  (+BAO)

□ With nominal cluster mass bias, SZ cluster counts prefer non-zero neutrino mass ( $\sim 0.5$  eV).

