

# Spiral Structure and Mass Inflows Barred-Spiral Galaxies

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# Outline

- Bar regions
  - Substructure formation
  - Location of nuclear rings
  - Longevity of dust lanes and ring star formation
- Spiral-arm regions
  - Extent and shape of gaseous arms
  - Gas inflows/outflows driven by spiral arms.

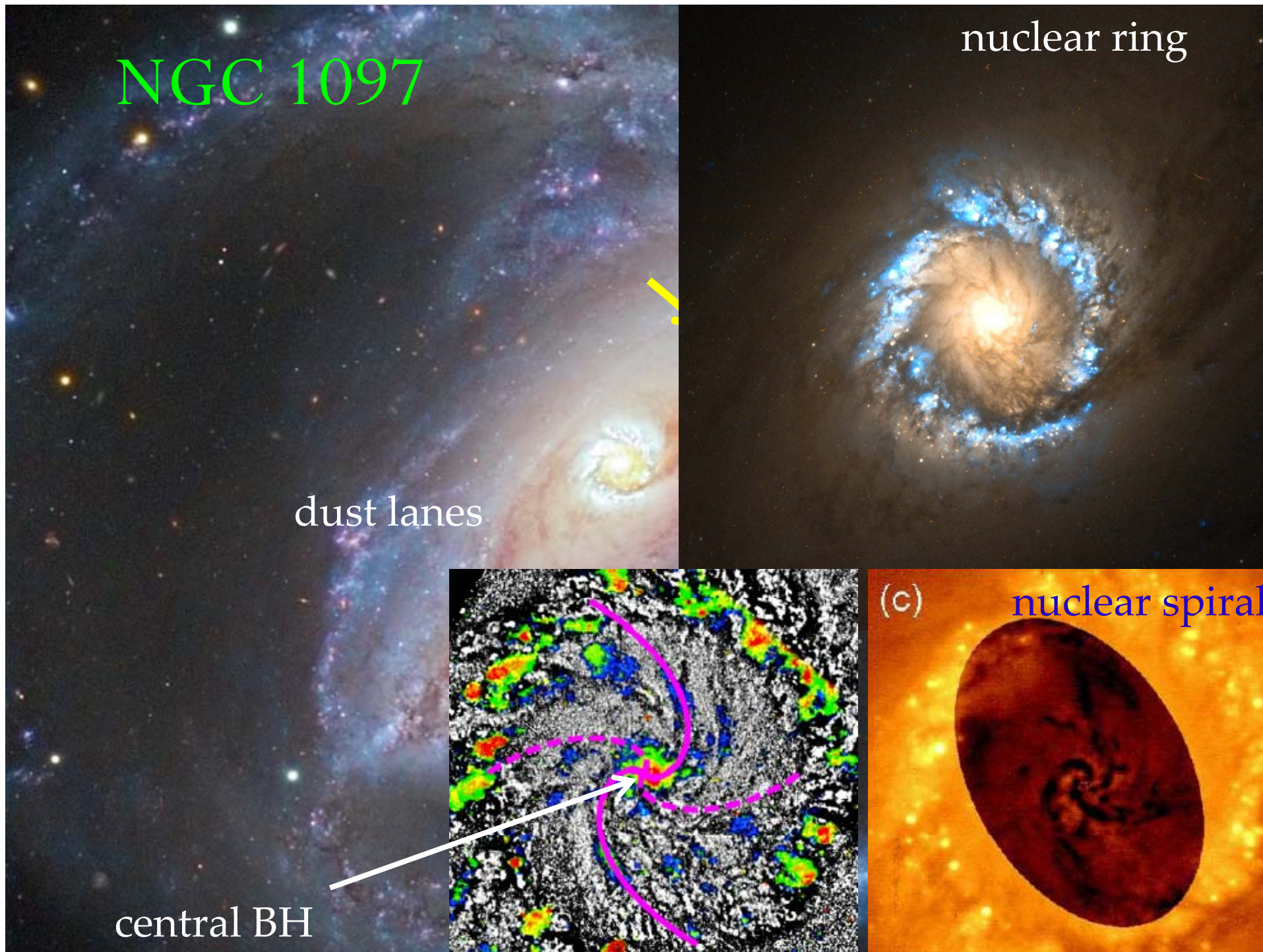
NGC 1097

dust lanes

central BH

nuclear ring

(c) nuclear spirals



- Some galaxies have relatively straight dust lanes, while others have curved ones.



NGC 6951:  $\Delta\alpha=9^\circ$



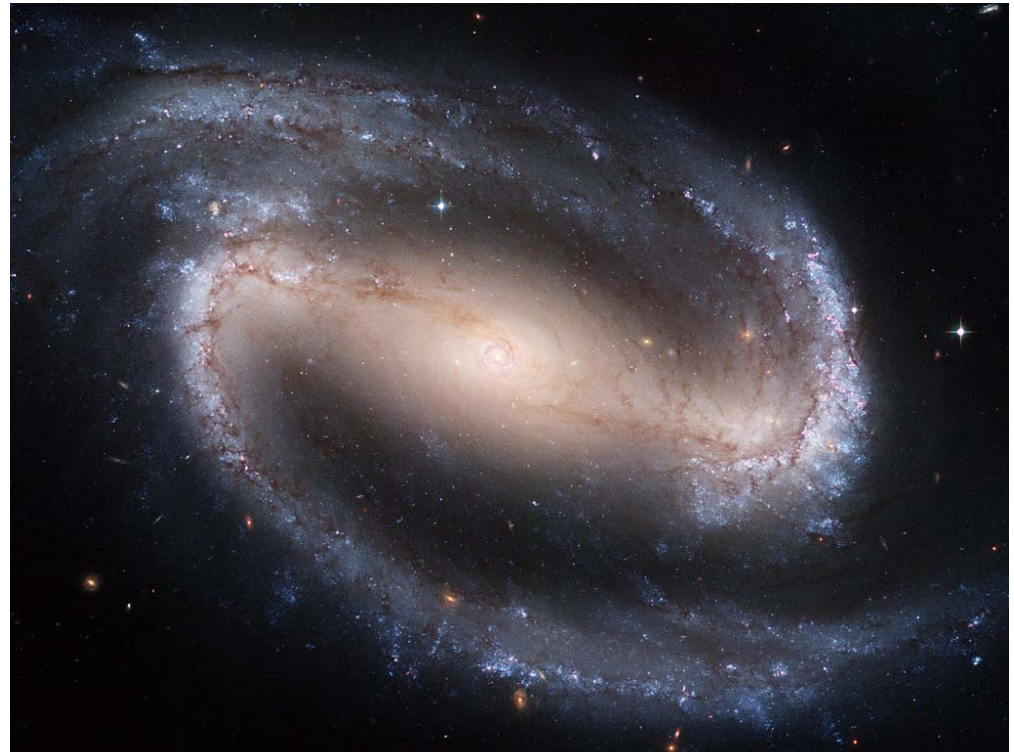
NGC 4321:  $\Delta\alpha=73^\circ$

Comeron et al. (2009)

- Some galaxies have a relatively large nuclear ring, while others have smaller one.



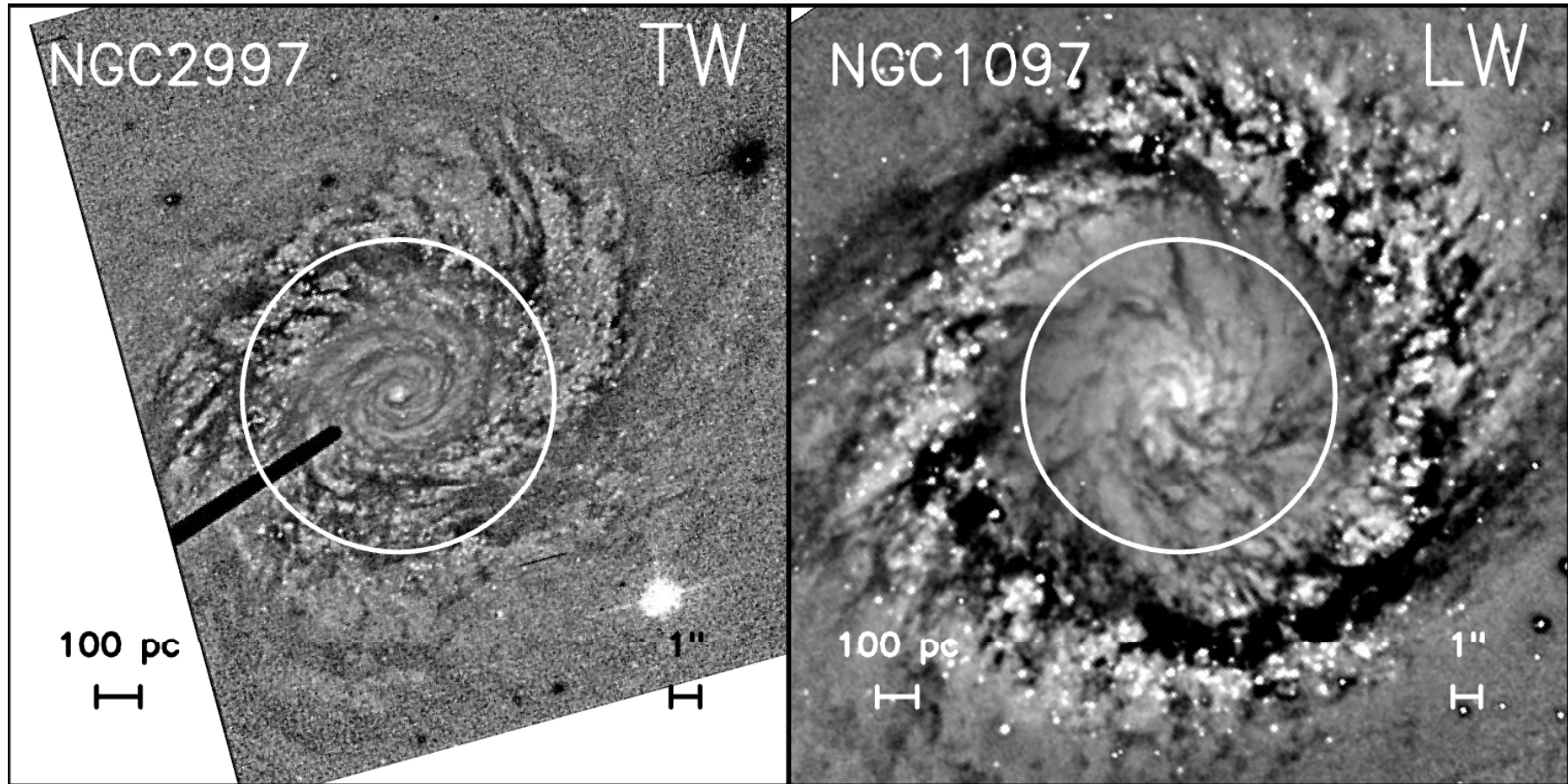
NGC 1343:  $1.2\text{kpc} \times 0.9\text{kpc}$



NGC 1300:  $0.3\text{kpc} \times 0.2\text{kpc}$

Mazzuca et al. (2009)

- Some galaxies have tightly wound nuclear spirals, while others have loosely wound ones.



Peeples & Martini (2006)

# Nuclear Rings

- Regarding nuclear rings, it has been widely accepted that rings form via **resonant interactions** of the gas with the bar potential.
  - This notion was driven by the fact that observed nuclear rings are located near the **inner Lindblad resonances** (e.g., **Combes & Gerin 1985; Knapen et al. 1995; Comeron et al. 2010**).
- Yet, there is no convincing theoretical argument.
  - Bar torque is very weak near the ILRs.
  - Resonance is a secular process, occurring over a very long time scale.
  - Resonance tends to disperse the material, rather than gathering it (e.g., gaps in planetary rings and the asteroid belt).

# Bar Model

- A normal galaxy with flat rotation at  $v_c \sim 200$  km/s in outer parts

- $M_{\text{BH}} = 4 \times 10^7 M_{\odot}$

- Bar : **a Ferrers ellipsoid**

$$\rho = \begin{cases} \rho_{\text{bar}} (1 - g^2)^n & \text{for } g < 1, \\ 0 & \text{elsewhere,} \end{cases}$$

$$g^2 = y^2/a^2 + (x^2 + z^2)/b^2$$

- $n=1$  (central density concentration)

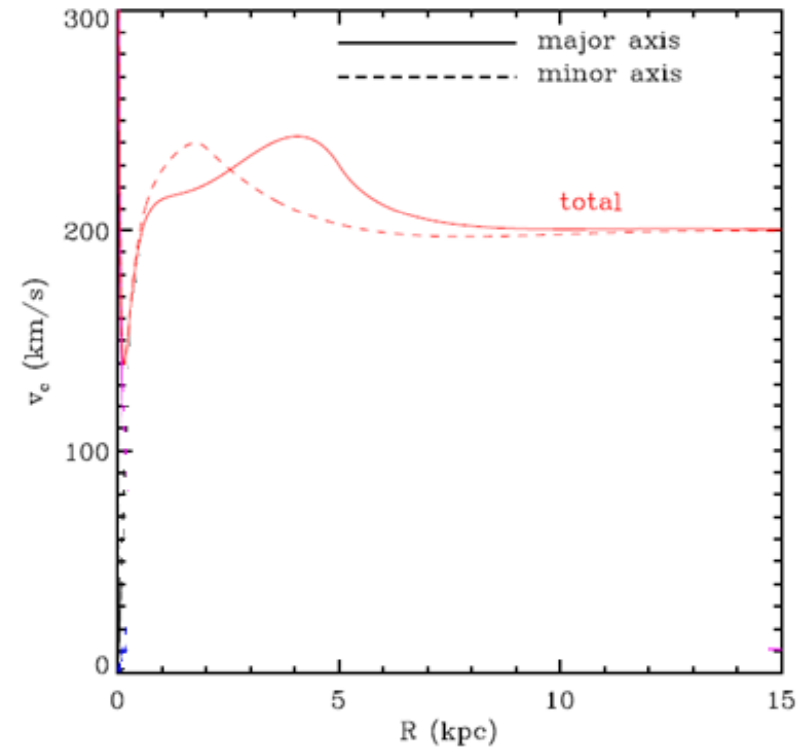
- Semi-major axis  $a=5$  kpc

- Aspect ratio  $R=a/b = 1.5 - 3.5$

- Bar mass  $f_{\text{bar}} =$

$$M_{\text{bar}} / (M_{\text{bar}} + M_{\text{bulge}}) = 8\% - 60\%$$

- $\Omega_b = 33$  km/s/kpc ( $R_{\text{CO}}=6$  kpc)



$$f_{\text{bar}} = 30\%$$

$$R = 2.5,$$

$$M_{\text{BH}} = 4 \times 10^7 M_{\odot}$$

# Bar Strength

- The most important parameter that controls the properties of bar substructures is the **bar strength**  $Q_b$  defined by

$$Q_b = \frac{F_T}{F_R} \Big|_{\max}$$

where  $F_T$  = tangential force due to a bar

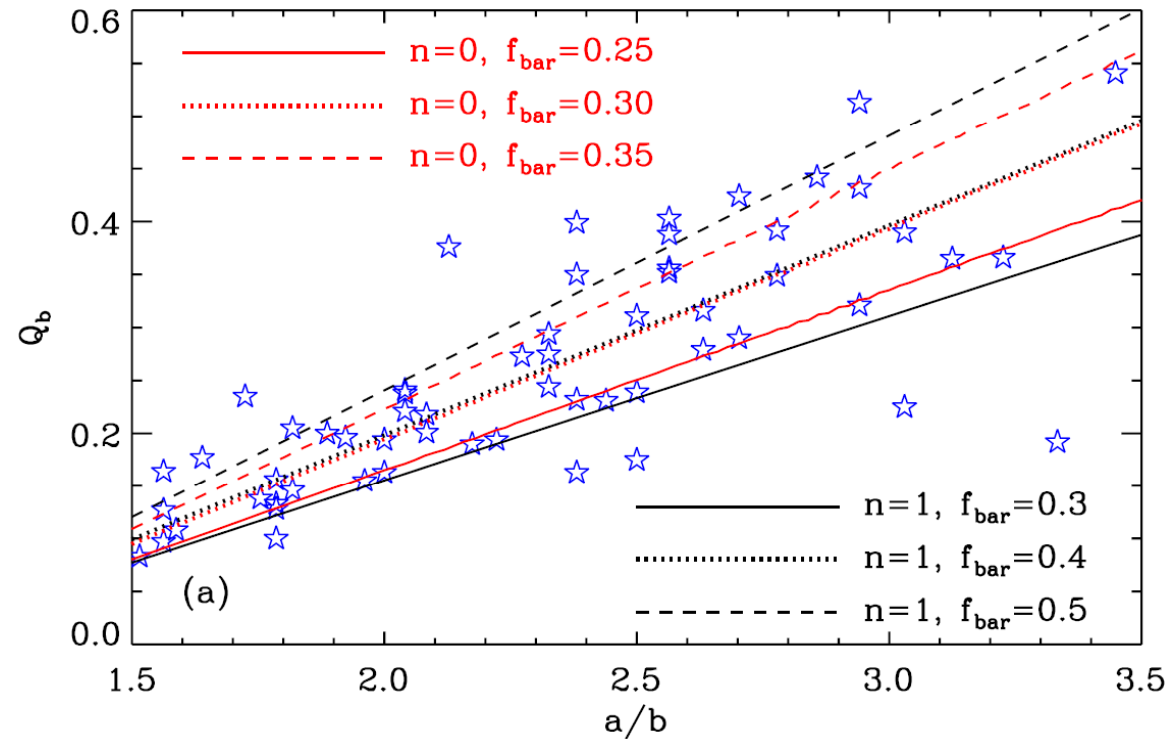
$F_R$  = radial force due to mass distribution

(e.g., Combes & Sanders 1981; Laurikainen & Salo 2002; Block et al. 2004; Laurikainen et al. 2004, 2006; Peeples & Martini 2006; Comeron et al. 2009, 2010)

- For our galaxy models with Ferrers bar,

$$Q_b = \begin{cases} 0.58 f_{\text{bar}}^{0.89} (a/b - 1), & \text{for } n = 0, \\ 0.44 f_{\text{bar}}^{0.87} (a/b - 1), & \text{for } n = 1, \\ 0.38 f_{\text{bar}}^{0.79} (a/b - 1), & \text{for } n = 2 \end{cases}$$

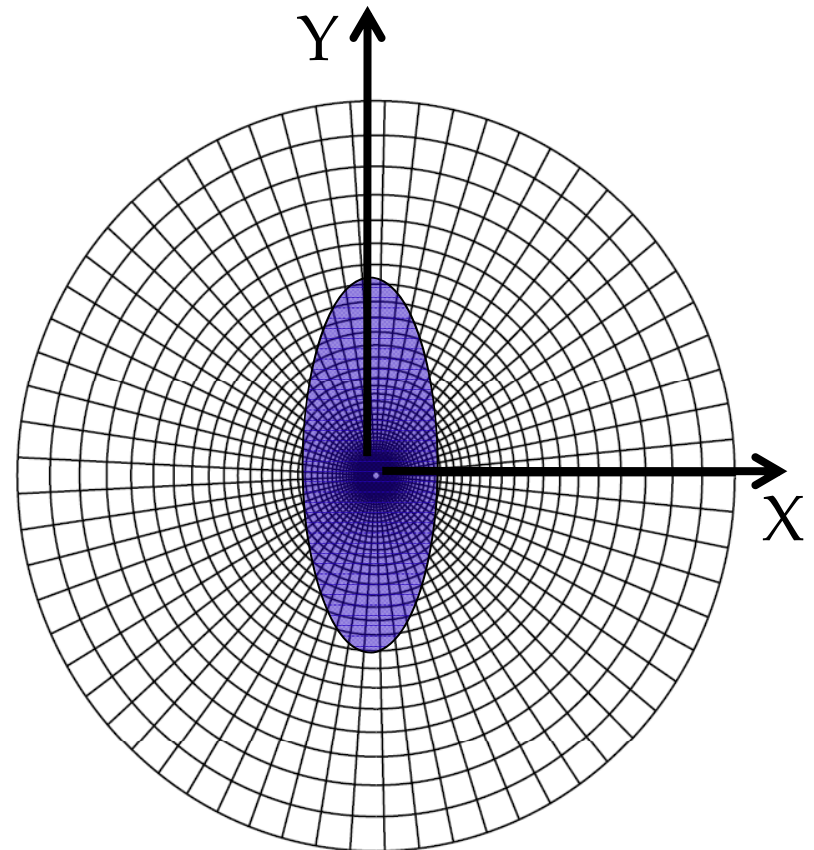
# Bar Strength of Model Galaxies vs. Observations



- The trend of  $Q_b$  becoming larger for a more elongated bar in the observational estimates (Comeron et al. 2010) is consistent with the results of our galaxy models.
  - $f_{\text{bar}} = 0.3\text{--}0.5$  for  $n = 1$
  - $f_{\text{bar}} = 0.25\text{--}0.35$  for  $n = 0$

# Numerical Method

- **CMHOG** Code ( **C**onnection **M**achine **H**igher **O**rders **G**odunov )
  - Grid-based code in cylindrical geometry
- Logarithmically-spaced cylindrical grid with 1024x480 zones
- The bar is oriented along the  $y$ -axis.
- The gaseous disk is self-gravitating and isothermal ( $c_s=10$  km/s) without magnetic fields.
- The ideal HD equations are solved in a frame rotating with the bar.
- No back reaction of the gas to the stellar bar.
- In order to avoid strong transients, the amplitude of the bar potential is slowly increased over  $\sim 200$  Myr.



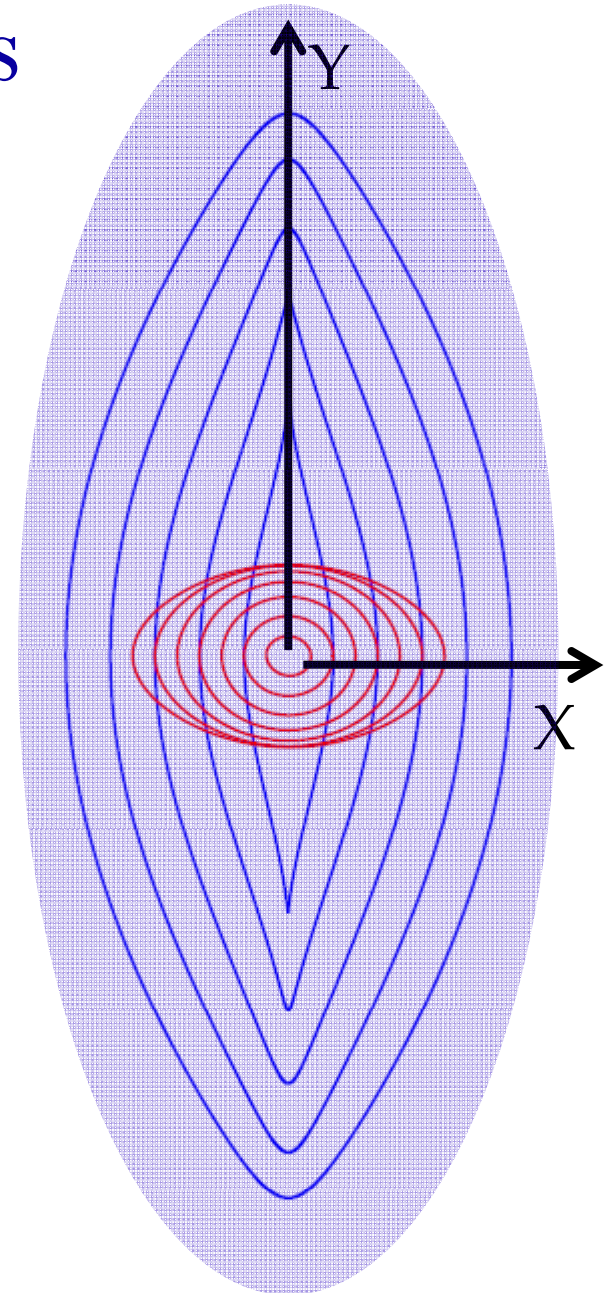
# $x_1$ and $x_2$ Orbits

- In the presence of an non-axisymmetric potential, angular momentum is not conserved, while **Jacobian integral** defined by

$$E_J = \frac{1}{2}|\dot{r}|^2 + \Phi_{\text{eff}}$$

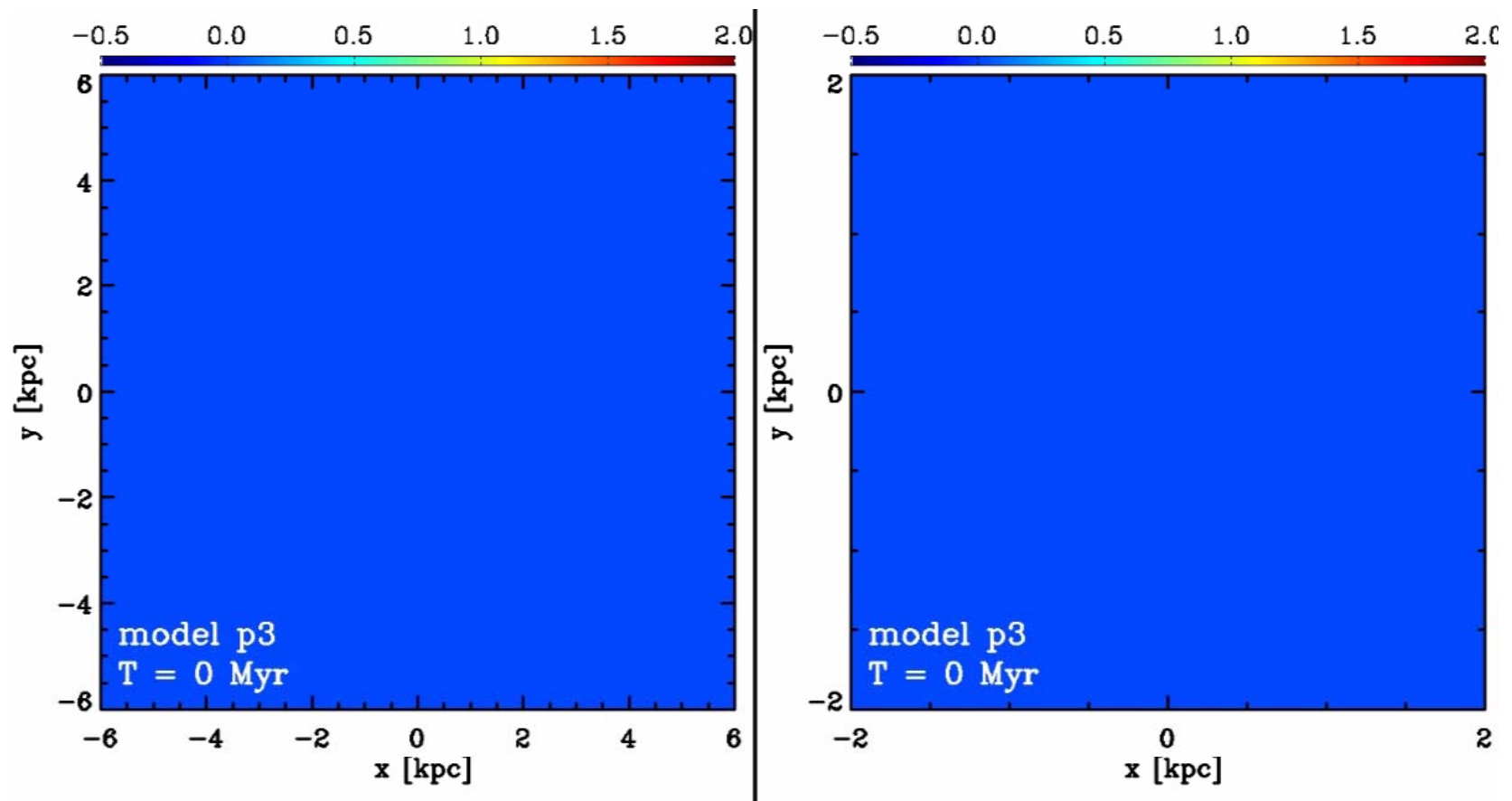
is conserved.

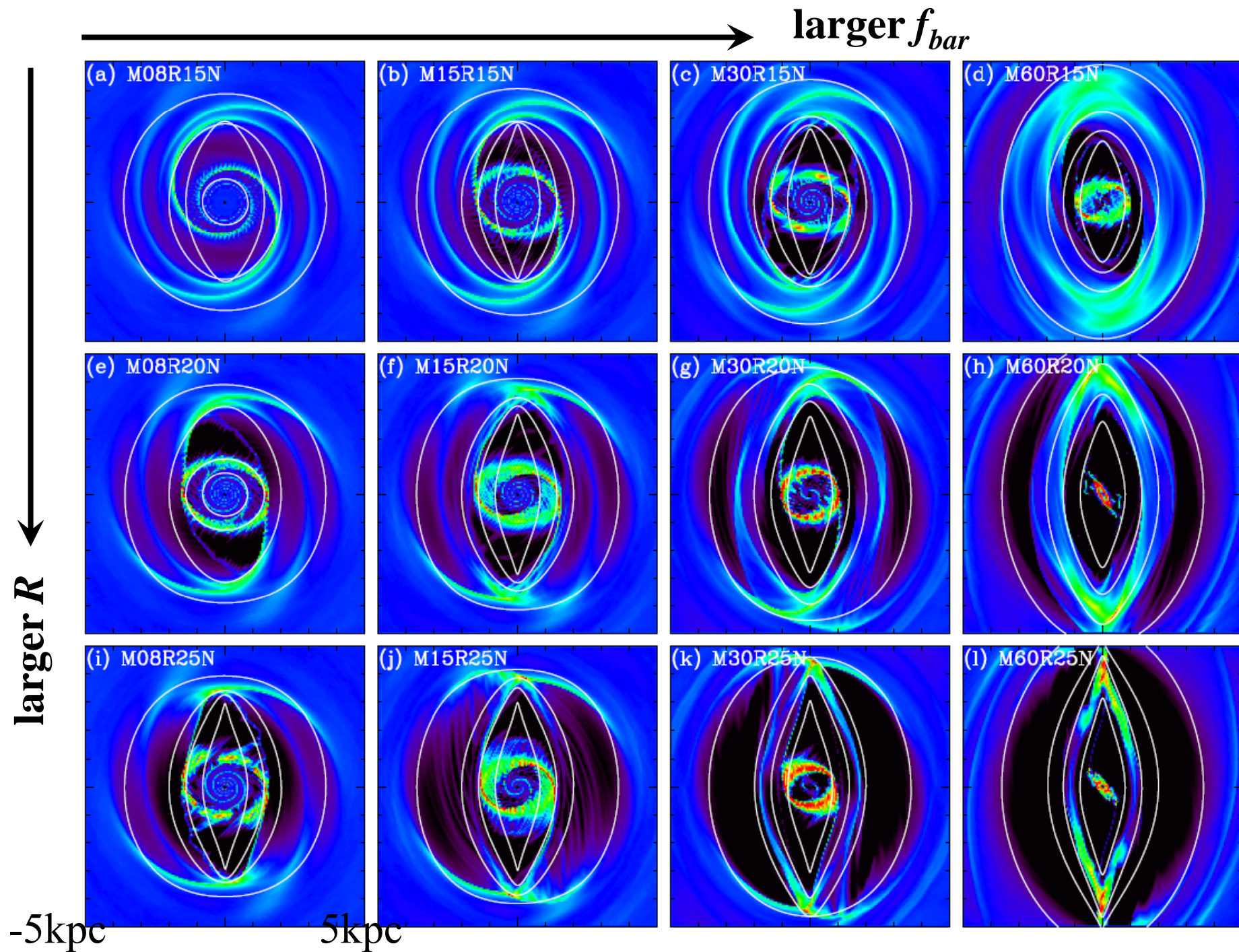
- Two (prograde) closed-orbit families in the rotating frame (**Contopoulos & Papayannopoulos 1980**):
  - **$x_1$  orbits** elongated along the bar major axis
    - Support the bar potential.
    - Associated with dust lanes.
  - **$x_2$  orbits** aligned along the bar minor axis
    - Associated with nuclear rings.



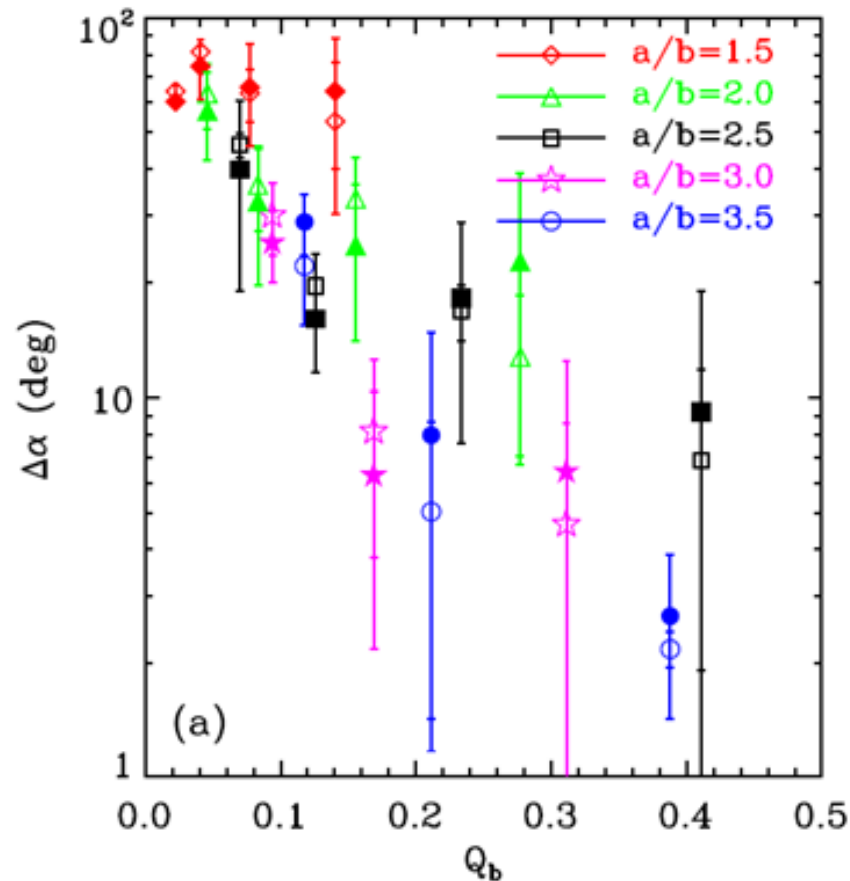
# Model with $Q_b=0.23$

Kim et al. (2012)





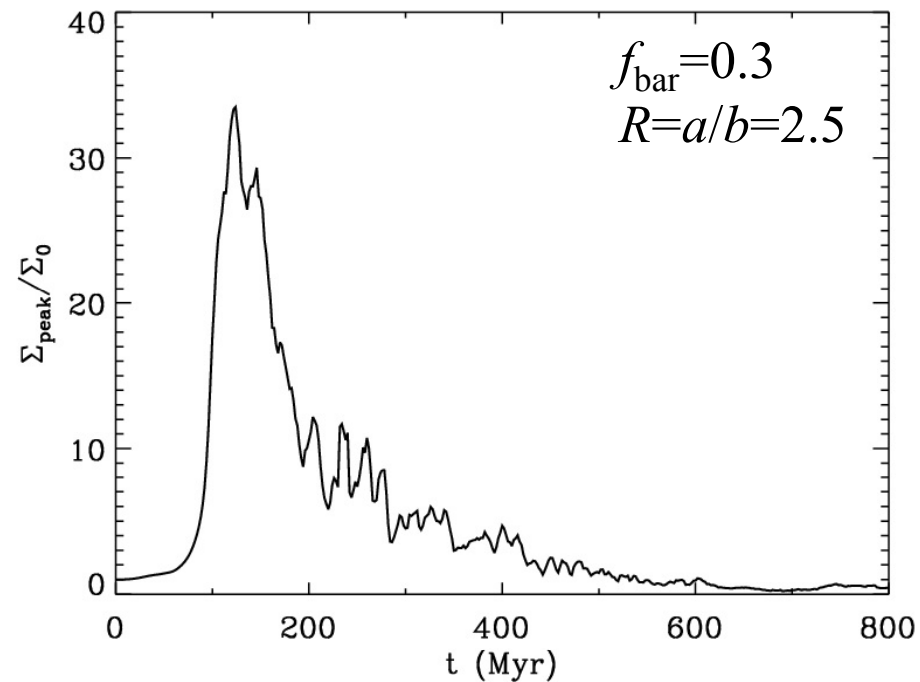
# Curvature $\Delta\alpha$ of Dust Lanes



- Overall, the shape of dust lanes is well described by  $x_1$  orbits.
- A stronger and more elongated bar has more straight dust lanes (Athanasoula 1992; Knapen et al. 2002; Comeron et al. 2009).

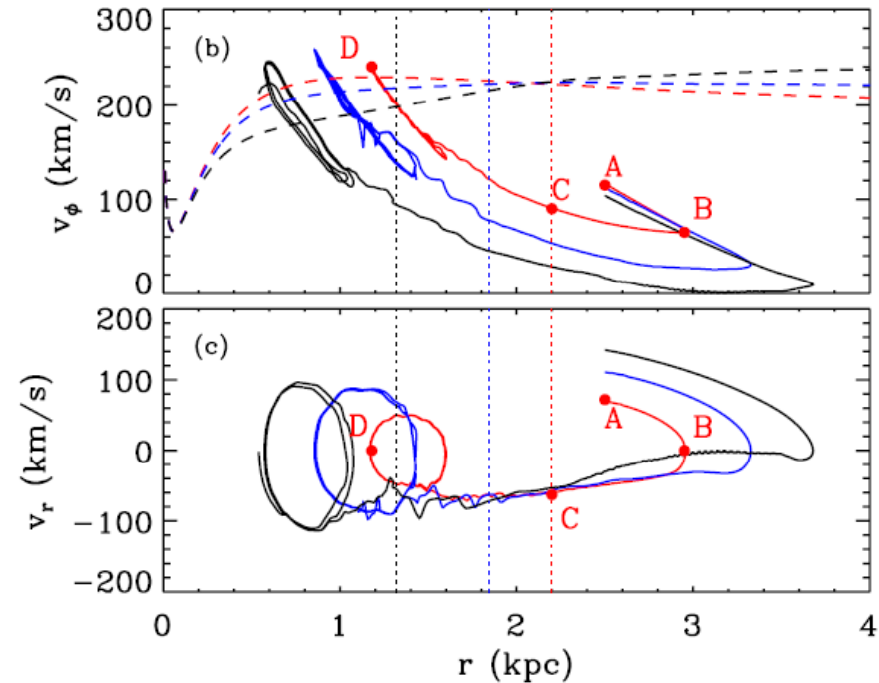
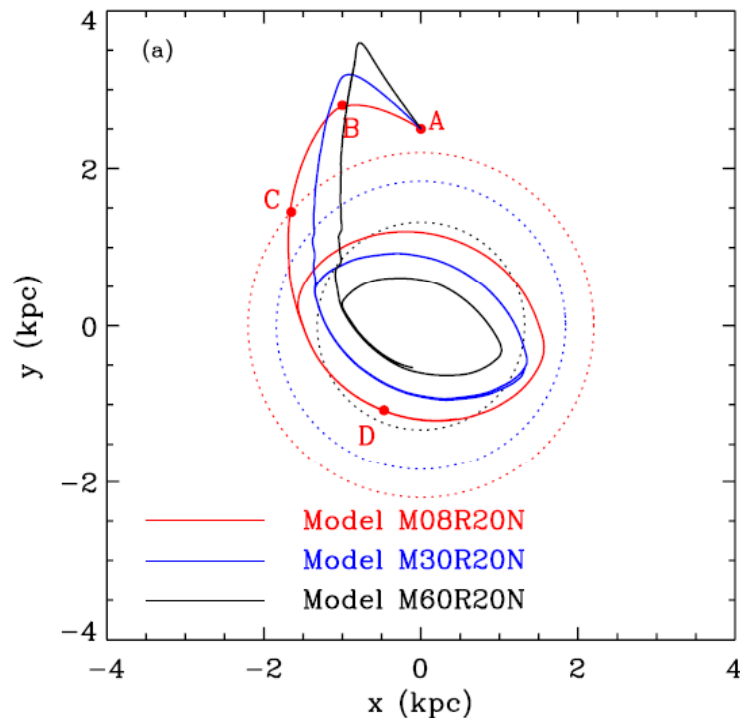
(Average is taken over 250-350 Myr)

# Strength of Dust Lanes



- Dust lanes remain strong only for 100 Myr before the bar potential achieves the full strength.
  - The rapid decline of the strength of dust lanes is primarily due to the fact that the gas only inside the outermost  $x_1$ -orbit can respond strongly to the bar potential to lower its orbits.

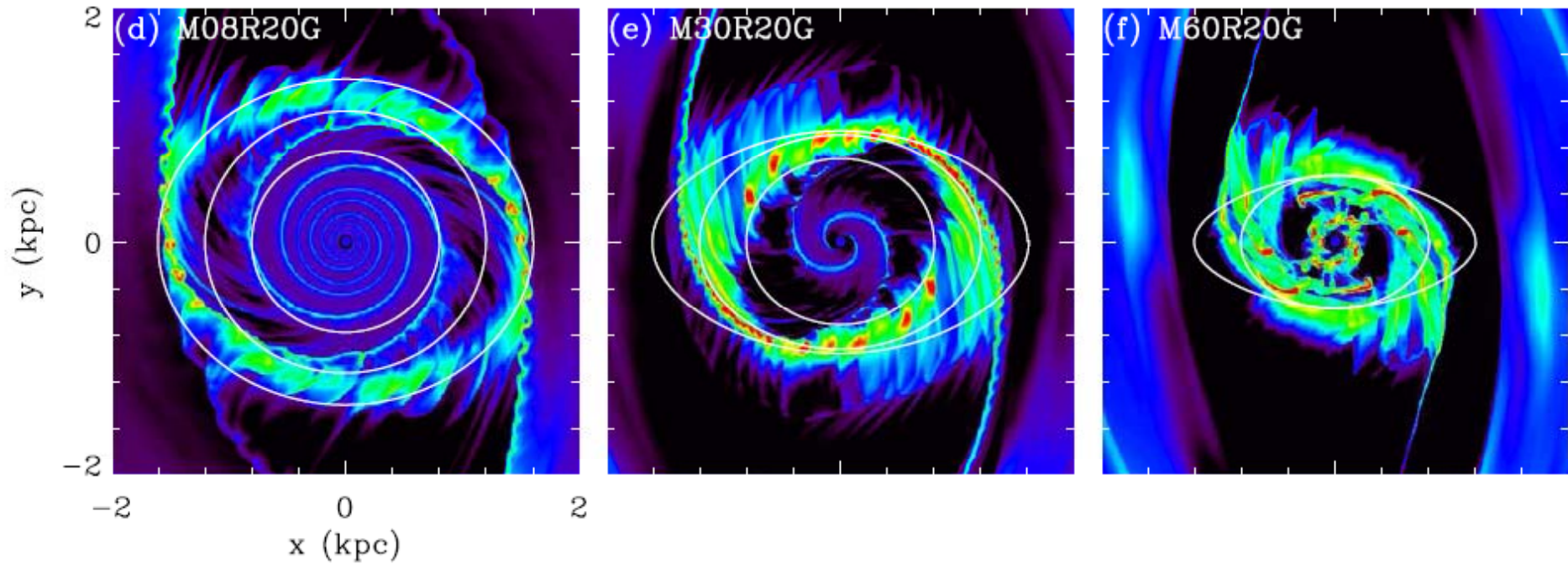
# Ring Formation



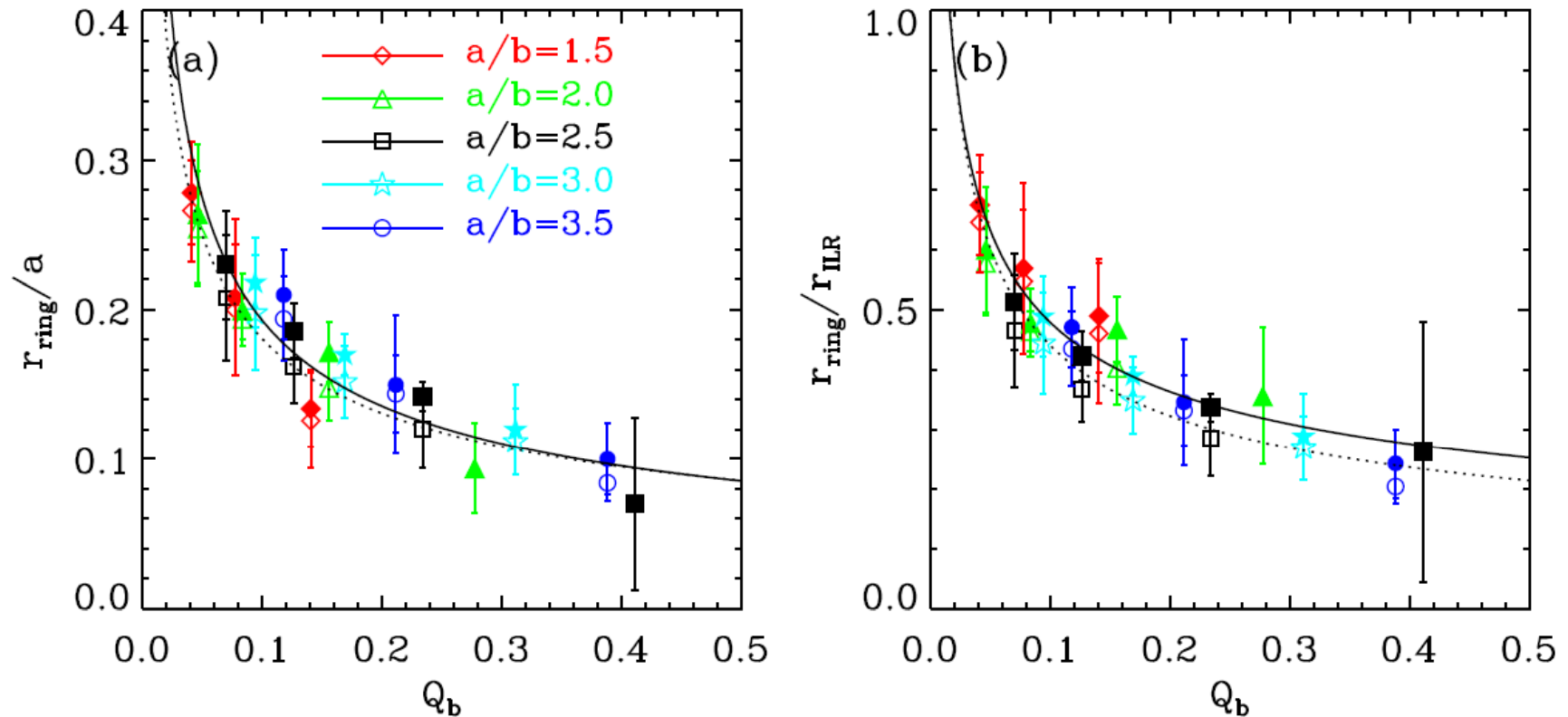
- The inflowing speed is so large that the bar torque cannot stop gas motions across the ILR.
- The inflowing gas keeps moving in and eventually forms a nuclear ring at the location where the centrifugal force balances the external gravitational force.

# Nuclear Rings

larger  $Q_b$

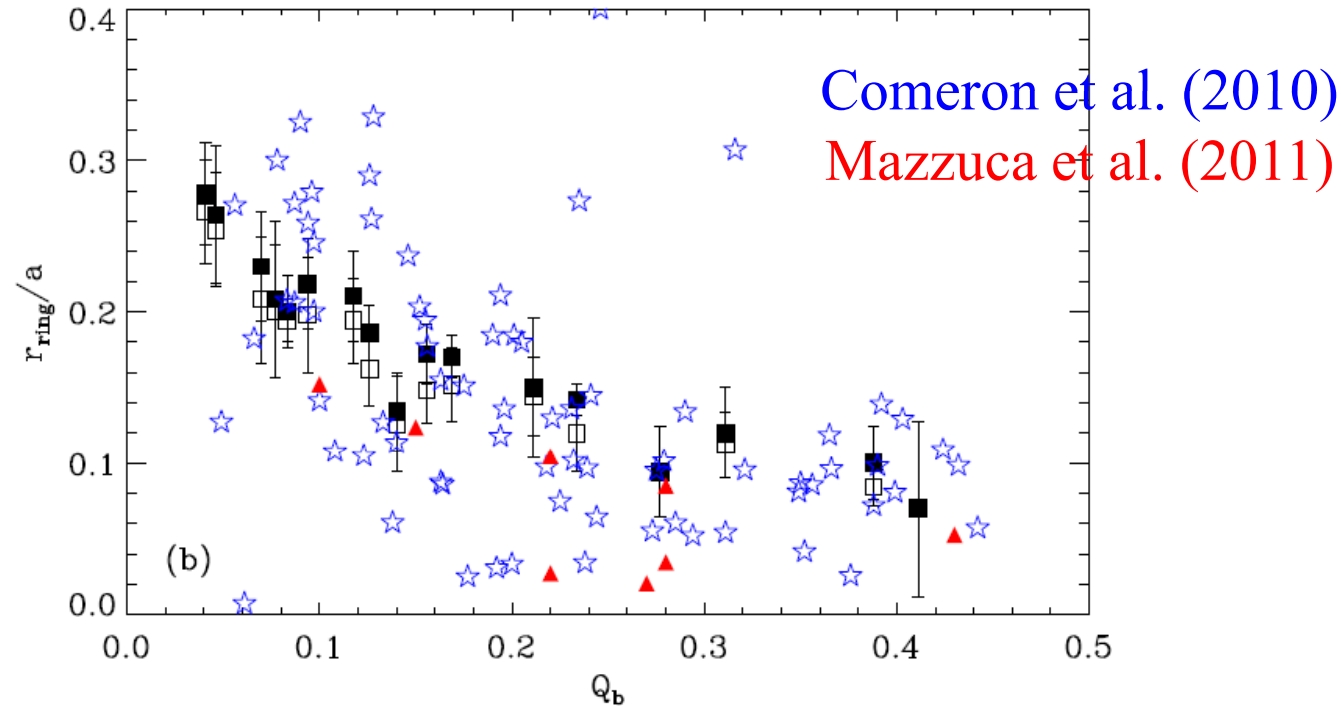


# Ring Size



- The ring position is in general inside the inner Lindblad resonance of the bar potential.
- Rings are smaller in models with a stronger bar.

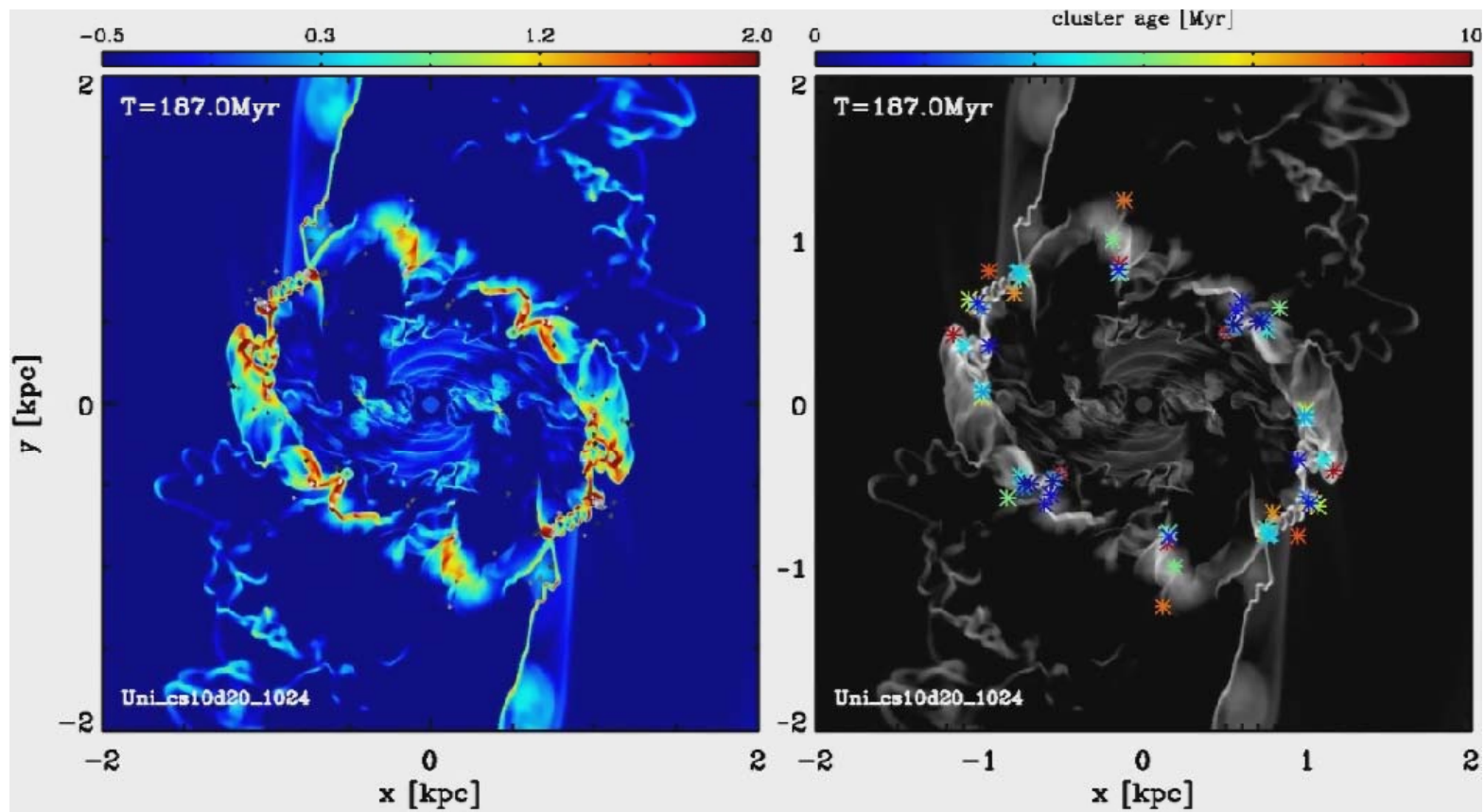
# Comparison With Observed Ring Sizes



- Both observational and numerical results show that stronger bars can possess smaller rings.
- For  $Q_b < 0.15$ , the agreement between observational and numerical results is quite good.
- For  $Q_b > 0.15$ , the ring size in our models corresponds roughly to the upper envelope of the observational results.

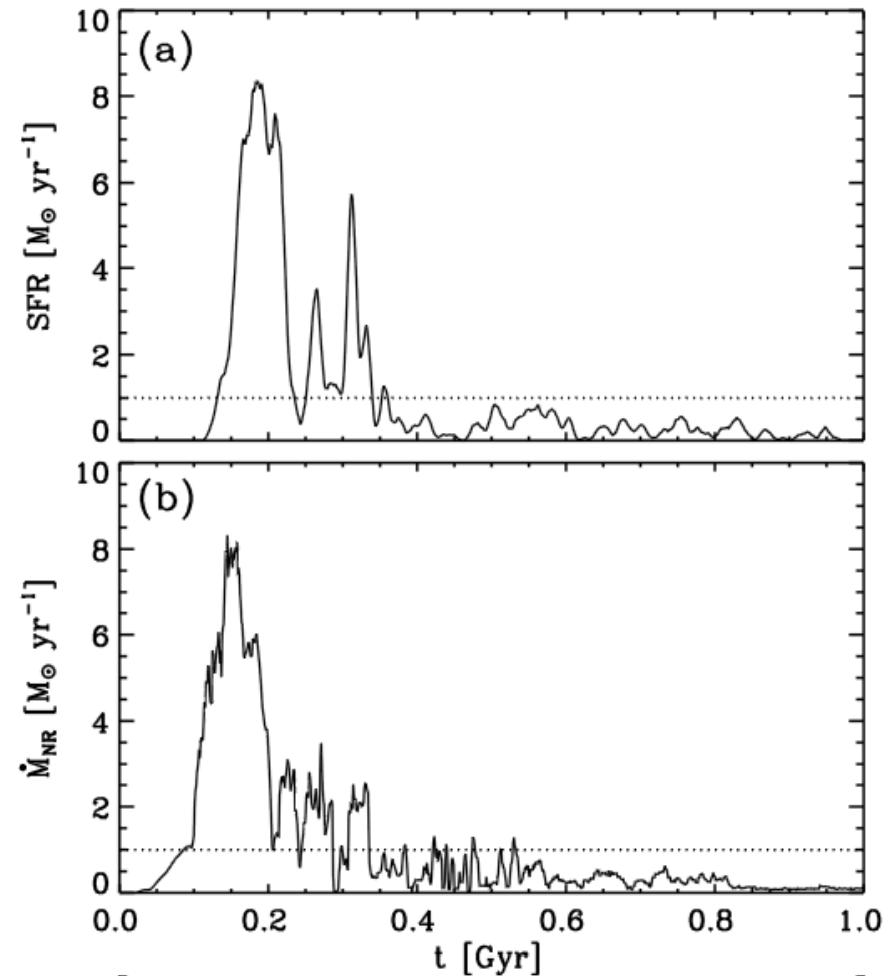
# Star Formation In Nuclear Rings

Model with  $\Sigma=20 M_{\odot} \text{pc}^{-2}$  (Seo & Kim 2013)



# Ring Star Formation Rate

- Star formation rate in the nuclear rings is well correlated with the mass inflow rate to the rings.
- SFR shows a strong primary burst lasting for about 100 Myr and then decays to small values below  $\sim 1 M_{\odot} \text{ yr}^{-1}$ .
  - Contrast to observational results that show that ring star formation is long lived lasting for 1-1.5 Gyr, with multiple episodes (Allard et al. 2006; Sarzi et al. 2007; van der Laan et al 2013)

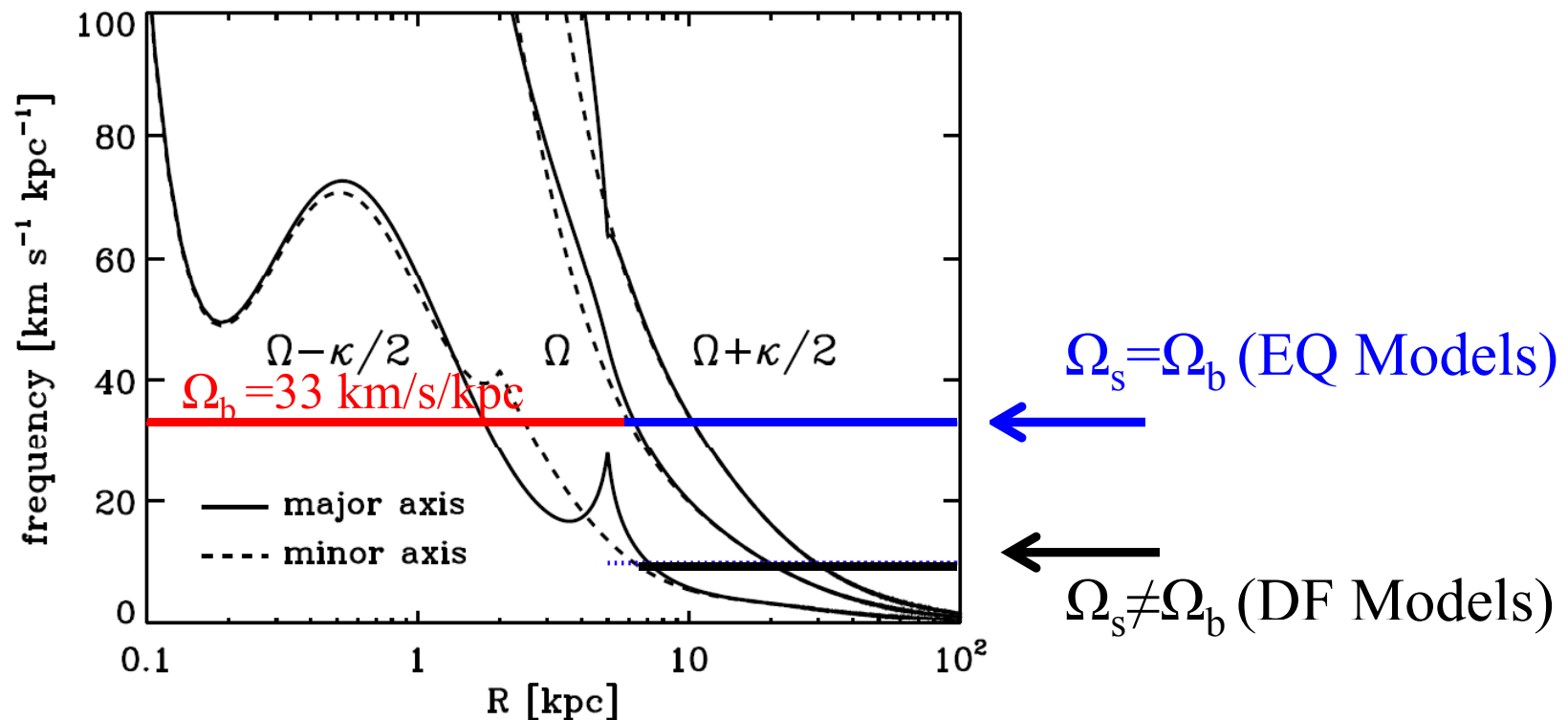


# Necessity of Gas Feeding to the Bar Region

- The gas in the bar regions should be replenished continuously or continually in order to explain observed **strong dust lanes** as well as **prolonged SF** in nuclear rings of barred galaxies.
- Candidate mechanisms for gas feeding
  - angular momentum dissipation by spiral arms (Roberts & Shu 1972; Lubow et al. 1986; Hopkins & Quataert 2011)
  - galactic fountains (e.g., Fraternali & Binney 2006, 2008).
  - cosmic accretion of primordial gas (e.g., Dekel et al. 2009)
    - HVCs,  $\sim 0.7 M_{\odot} \text{ yr}^{-1}$  for M31/Milky-Way-type galaxies (Richter 2012)
- We study the first possibility directly including a spiral potential in our numerical models.

# Models With a Bar and Spiral Arms

- Most barred galaxies have spiral arms at outer regions, as well.
- Some galaxies appear to have a bar and spiral arms rotating at a similar pattern speed, while they have different pattern speeds in other galaxies (Sellwood & Sparke 1988; Fathi et al. 2009; Martinez-Garcia et al. 2011)



# Spiral Arm Potential

- Logarithmic spirals (Local analog of **Lin & Shu 1964, 1966**)

$$\Phi_s(R, \phi; t) = \Phi_{s0} \cos \left( m \left[ \phi + \frac{\ln R}{\tan p_*} - \Omega_s t + \phi_0 \right] \right)$$

over  $R=5$  kpc to 30 kpc

- $p_*$  ( $=20^\circ$ ): pitch angle of the stellar pattern
- $m$  ( $=2$ ): number of arms

- Arm strength is controlled by the dimensionless parameter

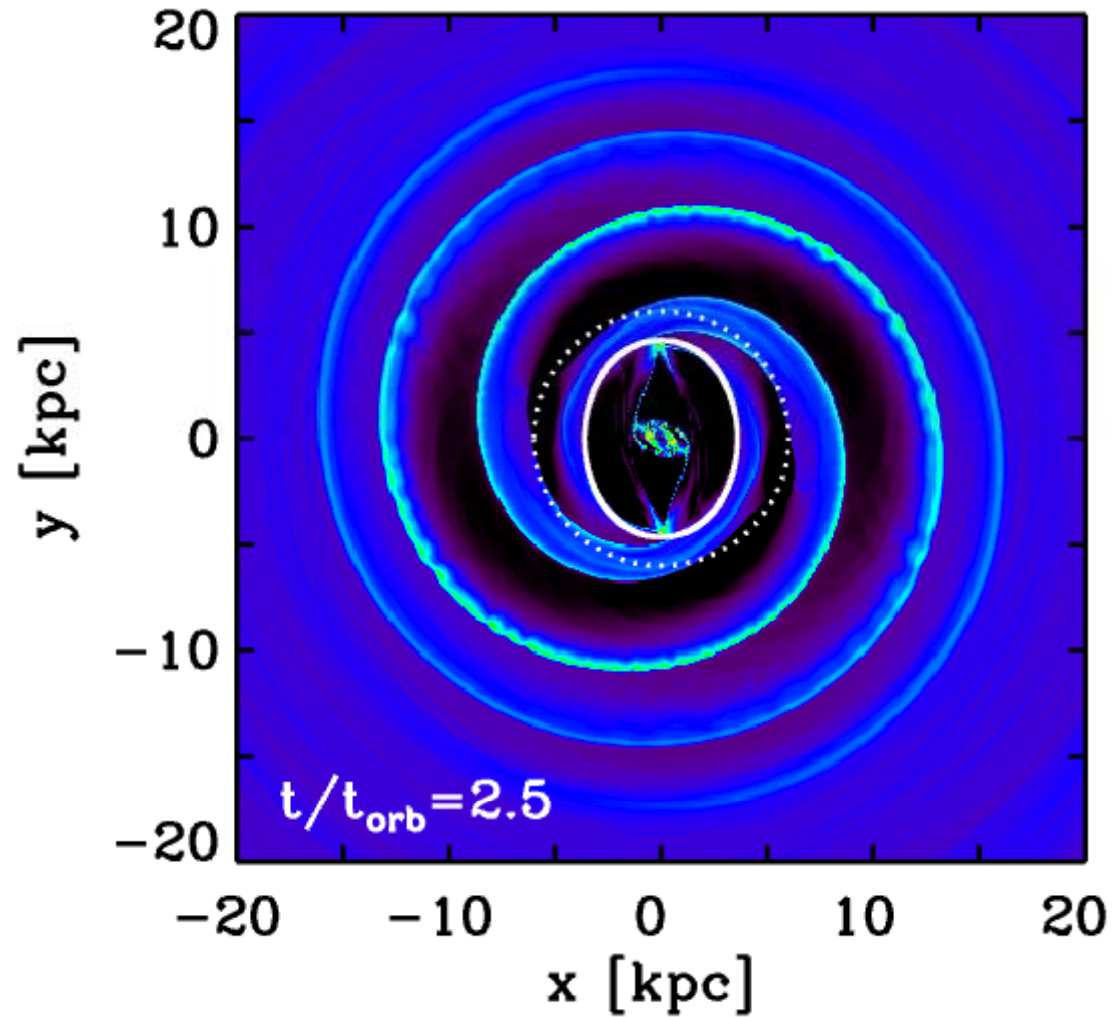
$$\mathcal{F} \equiv \frac{m\Phi_{s0}}{v_c^2 \tan p_*} = 5\text{-}20\% \quad (\text{Roberts 1969; Shu, Milione, \& Roberts 1973})$$

- Pattern speed of the spiral arms

- $\Omega_s = 33$  km/s/kpc (EQ Models) : CR at  $R=6$  kpc
- $\Omega_s = 10$  km/s/kpc (DF Models) : CR at  $R=19.8$  kpc

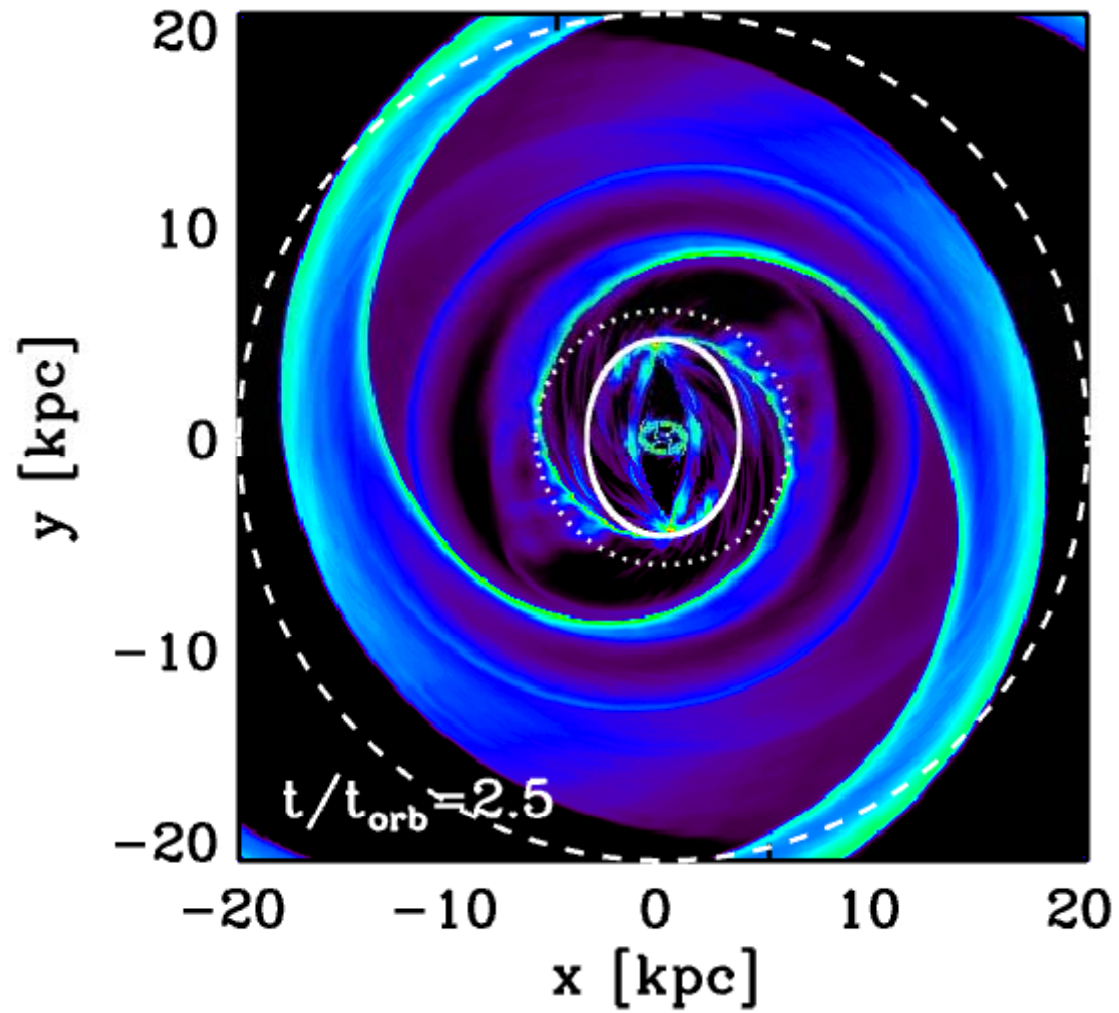
- All simulations are run in a framing corotating with the bar.

# EQ Model with $\mathcal{F}=10\%$



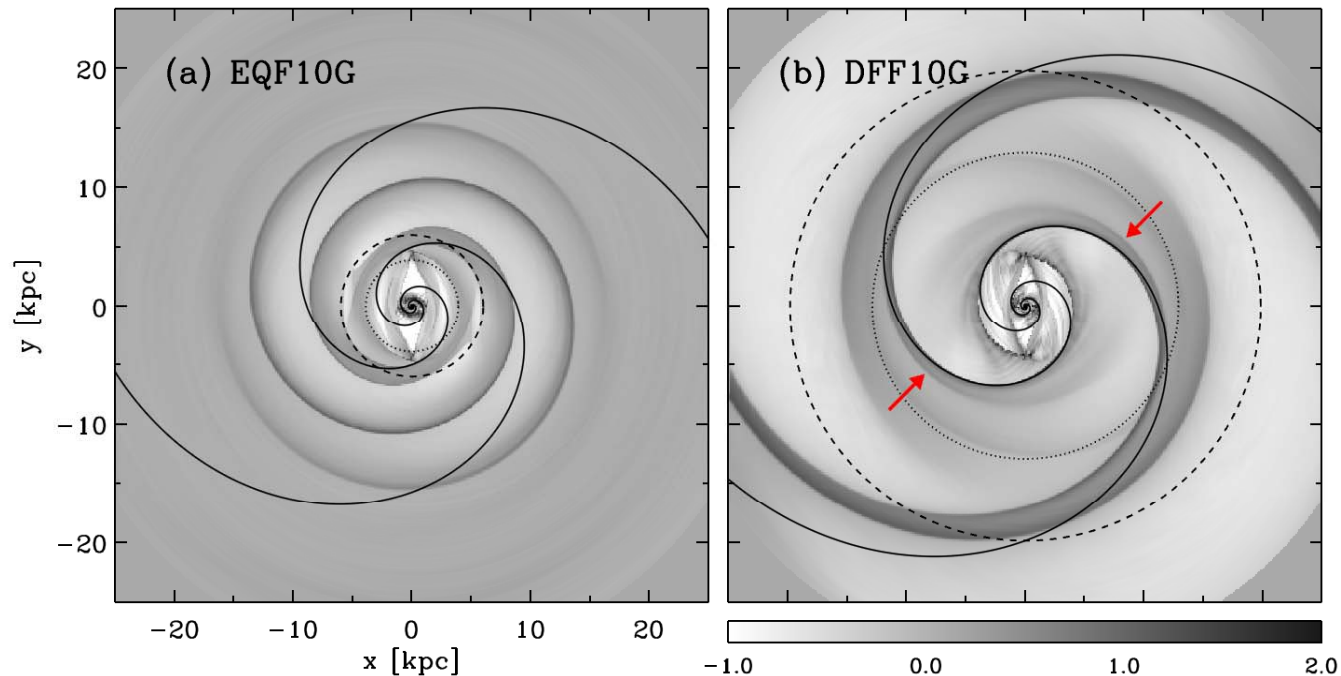
Kim & Kim (ApJ, submitted)

# DF Model with $\mathcal{F}=10\%$



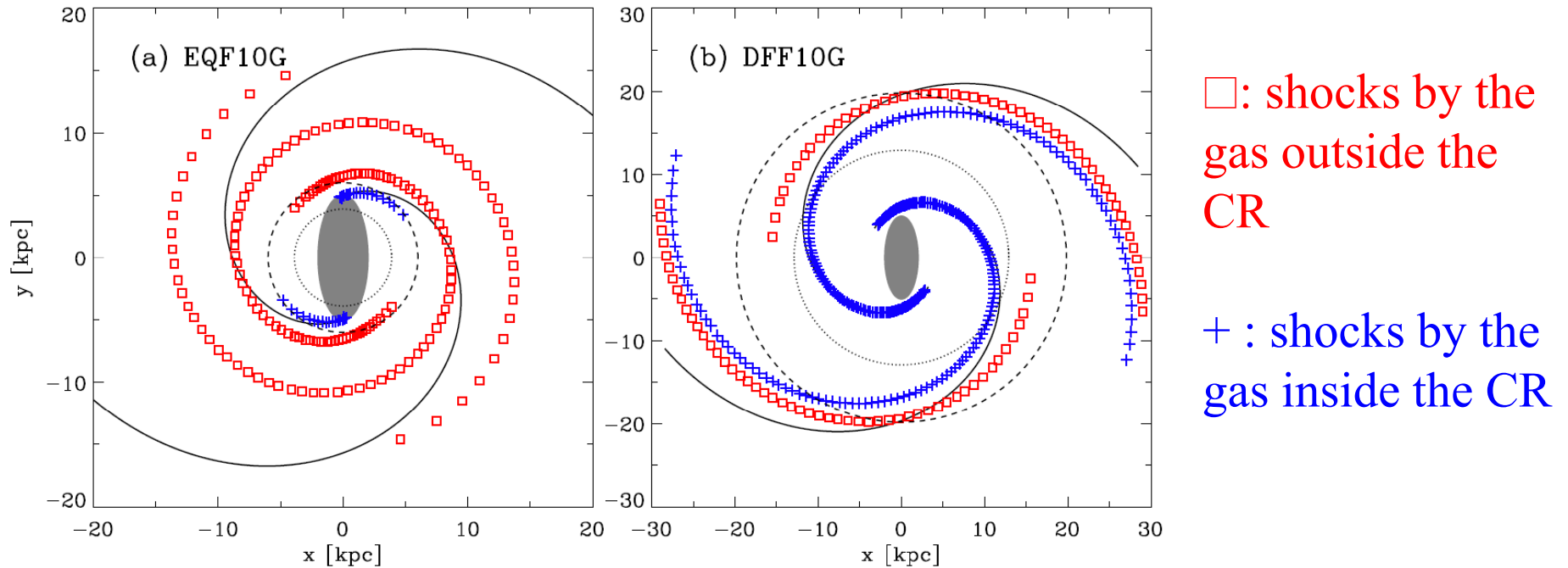
Kim & Kim (ApJ, submitted)

# Resonant Features



- In the DF models, weak features develop from the arms near the 4/1 resonance, similarly to *spurs* identified by [Chakrabarti et al. \(2003\)](#).
  - In the EQ models, any features that may grow are overwhelmed by the bar potential.
- No other resonance features such as branchings, bifurcations, etc., which seem to require spiral arms to be relatively loosely wound with  $p_* > 30^\circ$  (e.g., [Patsis et al. 1994, 1997](#); [Chakrabarti et al. 2003](#); [Yanez et al. 2008](#)).

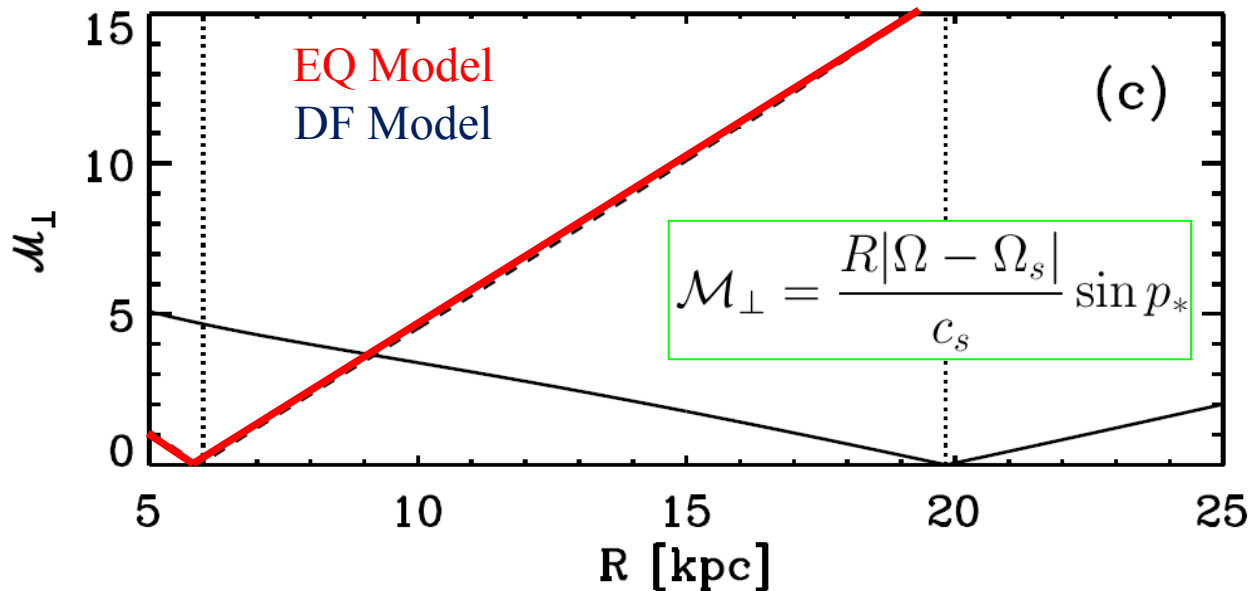
# Extent and Shape of Gaseous Arms



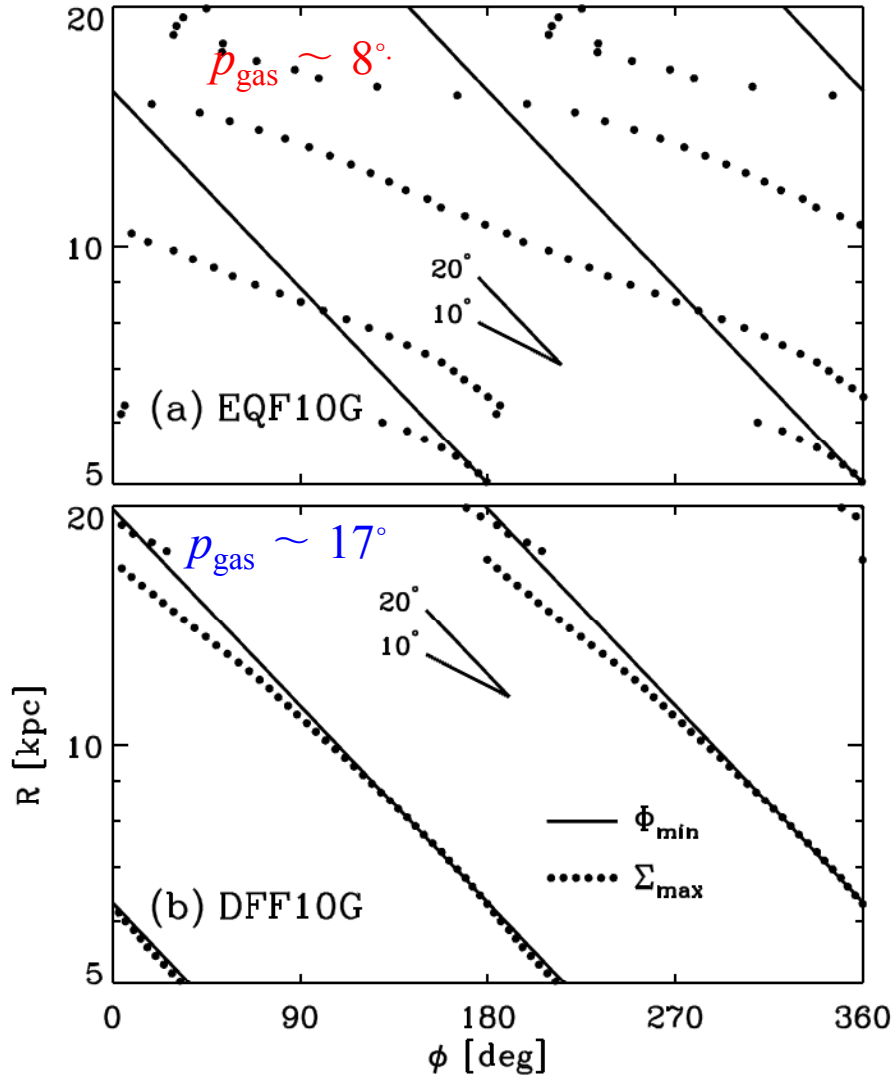
- Extension of spiral shocks
  - EQ models: only up to  $R=15$  kpc
  - DF models: all the way to the outer radial boundary
- Pitch angle of gaseous arms,  $p_{\text{gas}}$ 
  - $p_{\text{gas}} \ll p_*$  in the EQ models
  - $p_{\text{gas}} \leq p_*$  in the DF models

# Perpendicular Mach Number of Spiral Shocks

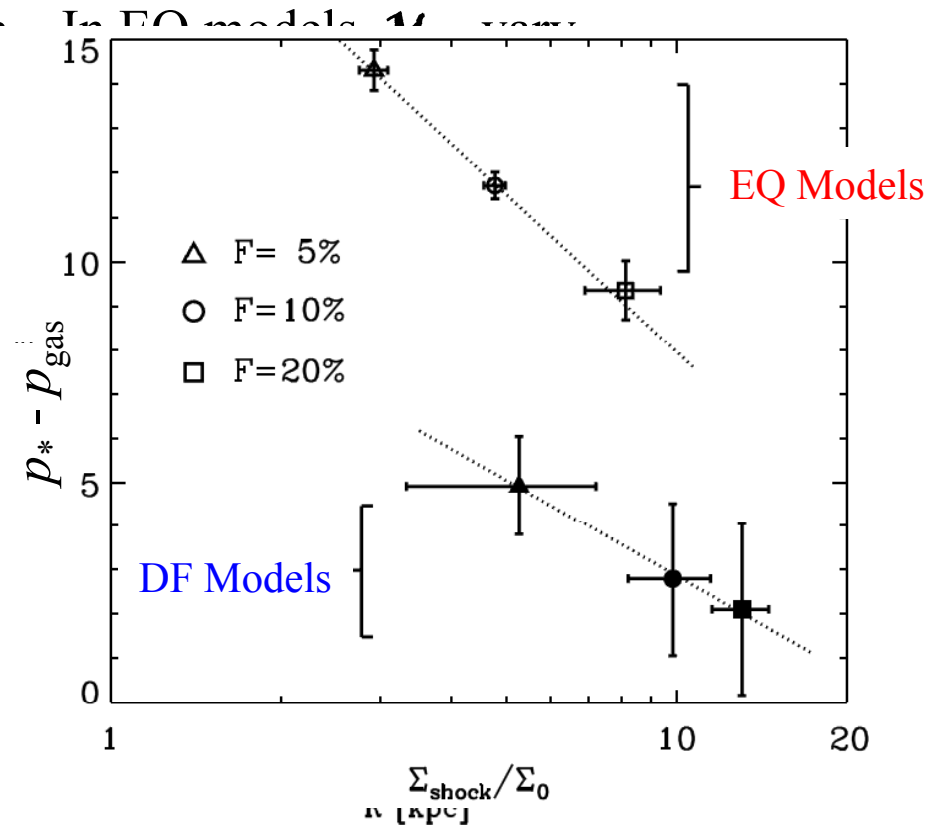
- The time interval between two successive passages of the spiral arms:  
 $t_{\text{arm}} = \pi/|\Omega - \Omega_s|$ ,
- The arm-to-arm sound crossing time :  $t_{\text{sound}} = \pi R/c_s$ .
- If  $t_{\text{sound}}/t_{\text{arm}} = \mathcal{M}_{\perp} / \sin p_* > 30$ , the gas does not have sufficient time to adjust itself to one arm before encountering the next arm.
  - the rapid rotation of the potential effectively makes itself smoothed significantly along the azimuthal direction.



# Pitch Angles of Gaseous Arms



- In a quasi-steady state, stronger spiral shocks tend to form at farther downstream. (Kim & Ostriker 2002; Gittins & Clark 2004)

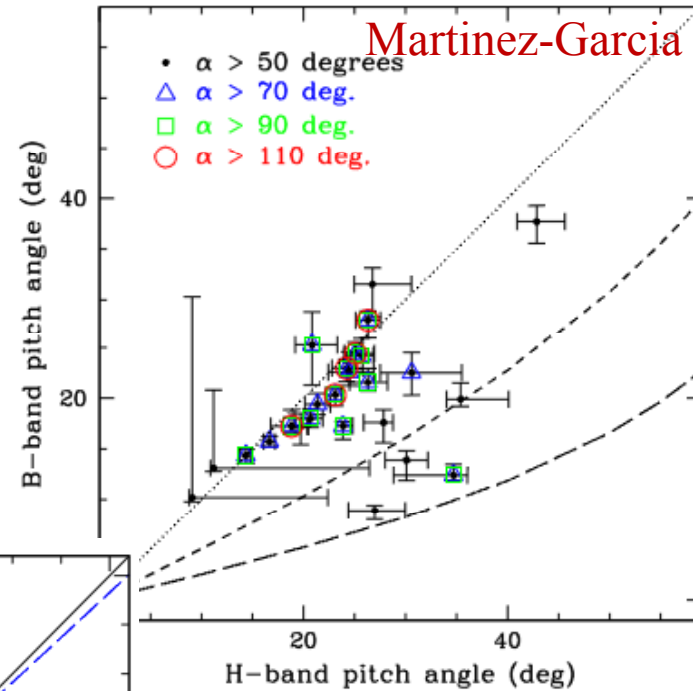


# Observed Arm Pitch Angles

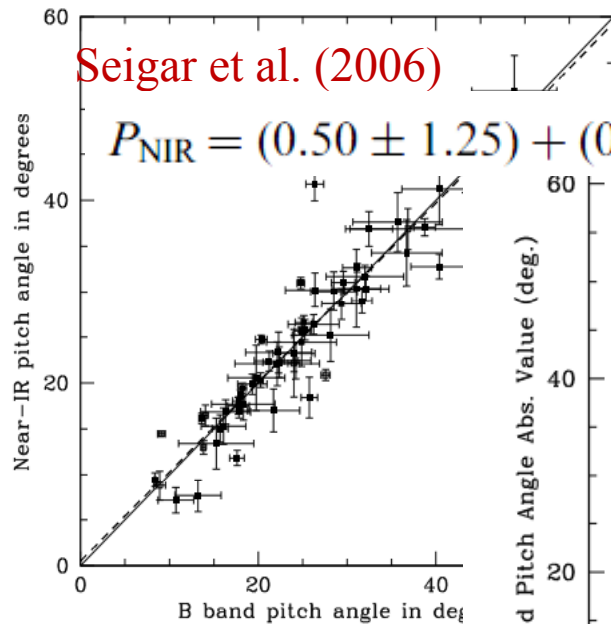
Grosbol & Patsis (1998)

Galaxy	K'	Pitch angle $i_2$		B	$\Delta$	range
		I	V			
NGC 3223	-8°:8	-9°:4	-8°:8	-8°:7	0°:5	25-36''
NGC 5085	-17°:4	-13°:0	-11°:7	-10°:9	0°:5	25-40''
NGC 5247	-34°:1	-31°:8	-29°:9	-27°:4	0°:7	30-50''
NGC 5861	-12°:4	-11°:8	-11°:9	-	0°:5	20-35''
NGC 7083	-22°:1	-20°:3	-17°:6	-15°:0	1°:0	11-18''

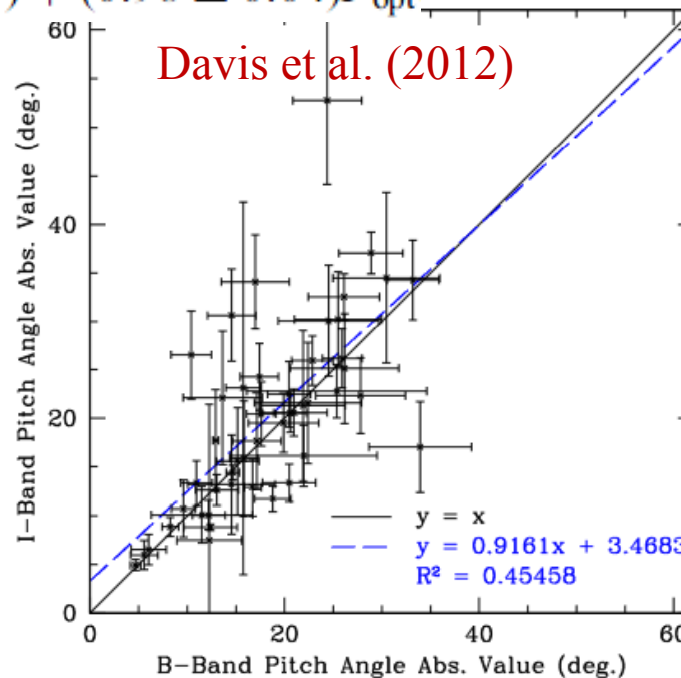
Martinez-Garcia (2012)



Seigar et al. (2006)

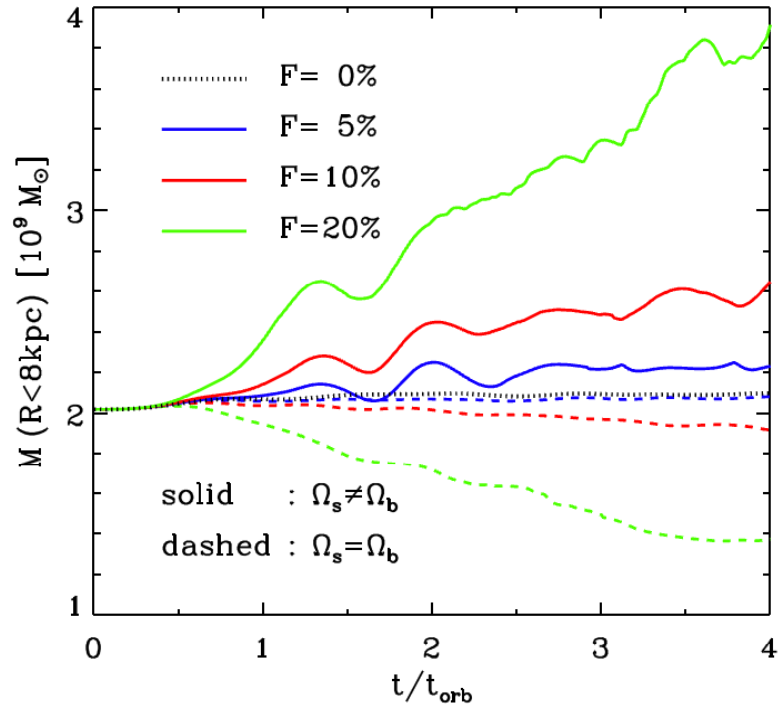


Davis et al. (2012)



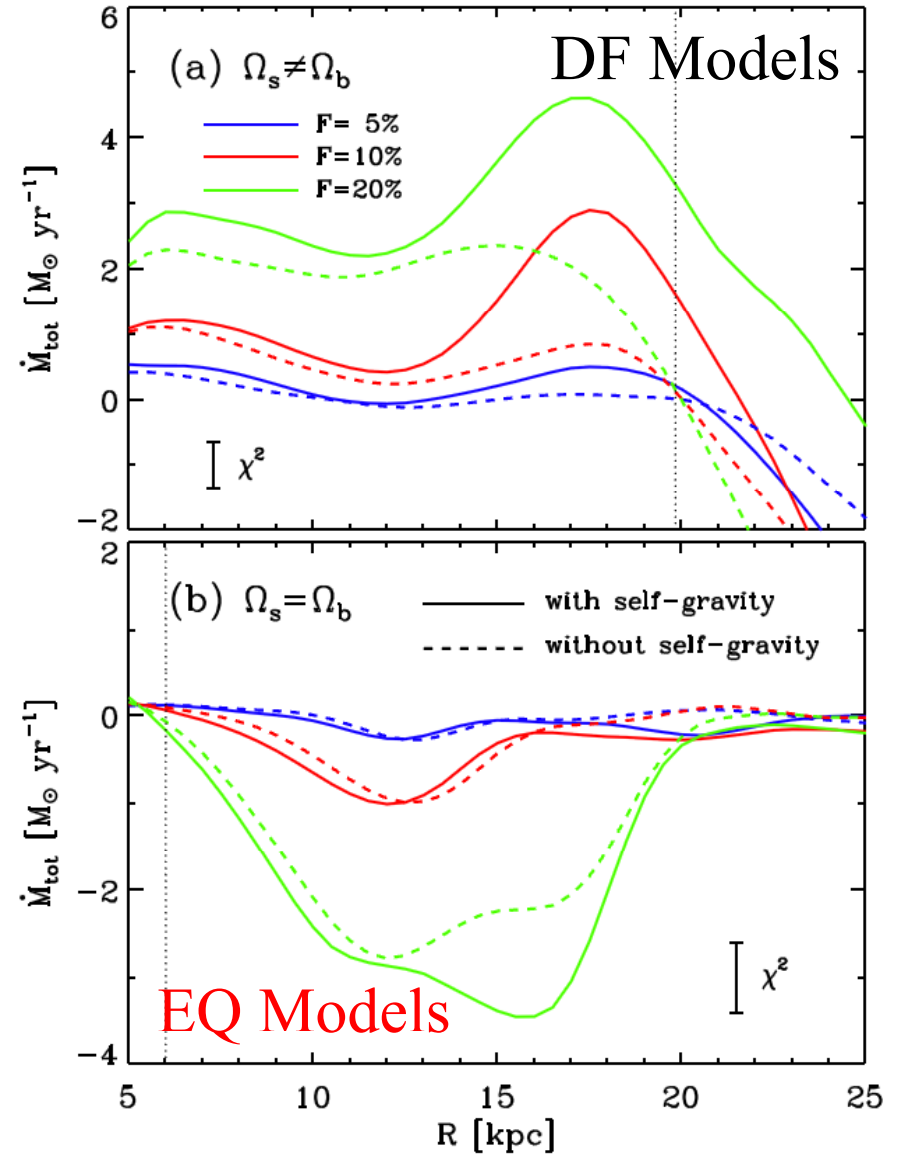
- Overall,  $p_{\text{gas}}$  is smaller by  $\sim 2^\circ$  than  $p_*$  for  $p_* \sim 10^\circ - 30^\circ$ , despite almost 1:1 relations between them.

# Radial Mass Drift



- Temporal changes of the gas mass within 8 kpc

$$M_{\text{tot}} = \frac{dM(R)}{dt}$$



# Mass Drift Rate

- The total rate of gas drift in our models is a combination of three processes:

$$\dot{M}_{\text{tot}} = \dot{M}_{\text{shock}} + \dot{M}_{\text{ext}} + \dot{M}_{\text{self}}$$

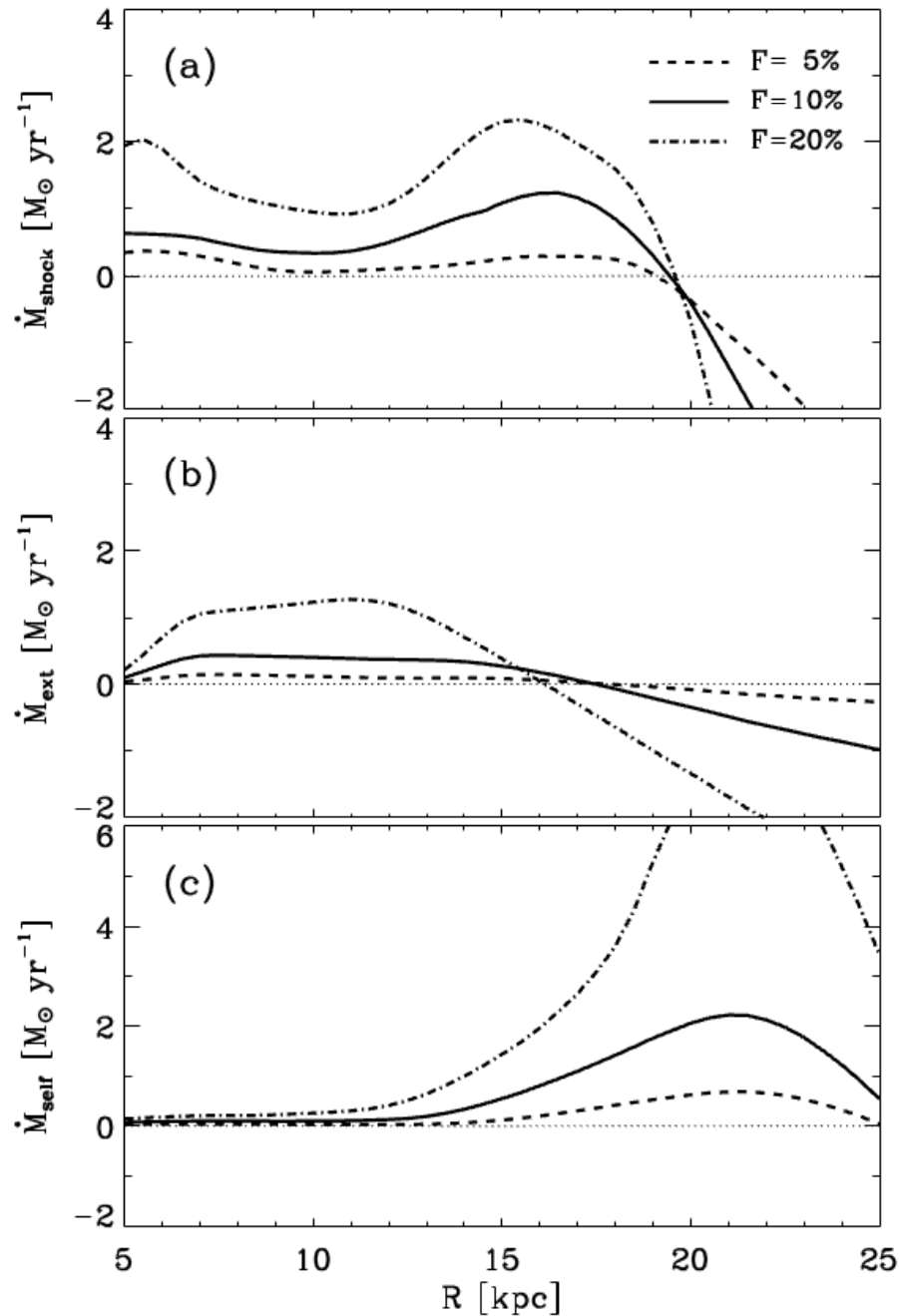
- Dissipation of angular momentum at spiral shocks (**Lubow et al. 1986; Hopkins & Quataert 2011**)
- Torque by the external spiral potential (**Lubow et al. 1986**)

$$\dot{M}_{\text{ext}} = - \left( \frac{1}{R} \frac{\partial R^2 \Omega}{\partial R} \right)^{-1} \int_{-\pi}^{\pi} \Sigma \frac{\partial \Phi_{\text{ext}}}{\partial \phi} d\phi$$

- Torque by the self-gravitational potential

$$\dot{M}_{\text{self}} = - \left( \frac{1}{R} \frac{\partial R^2 \Omega}{\partial R} \right)^{-1} \int_{-\pi}^{\pi} \Sigma \frac{\partial \Phi_{\text{gas}}}{\partial \phi} d\phi$$

# Mass Inflow Rate in DF models



- $\dot{M}_{\text{shock}} > 0$  inside the CR, as expected.
- Shock: extG: selfG  
= 50% : 40%: 10%, on average.
- Total inflow rates:  
 $\sim 0.5\text{--}2.5 M_{\odot} \text{ yr}^{-1}$  ( for  $\mathcal{F}=5\text{--}20\%$ )

$$\dot{M}_{\text{tot}} = 8\mathcal{F}(1 + 3\mathcal{F}) \frac{\Sigma}{\Sigma_0} M_{\odot} \text{ yr}^{-1}$$

cf. Lubow et al. (1986)'s local models yield

$$dM/dt \sim 0.2\text{--}0.4 M_{\odot} \text{ yr}^{-1}$$

corresponding to  $\mathcal{F}=3\%$ .

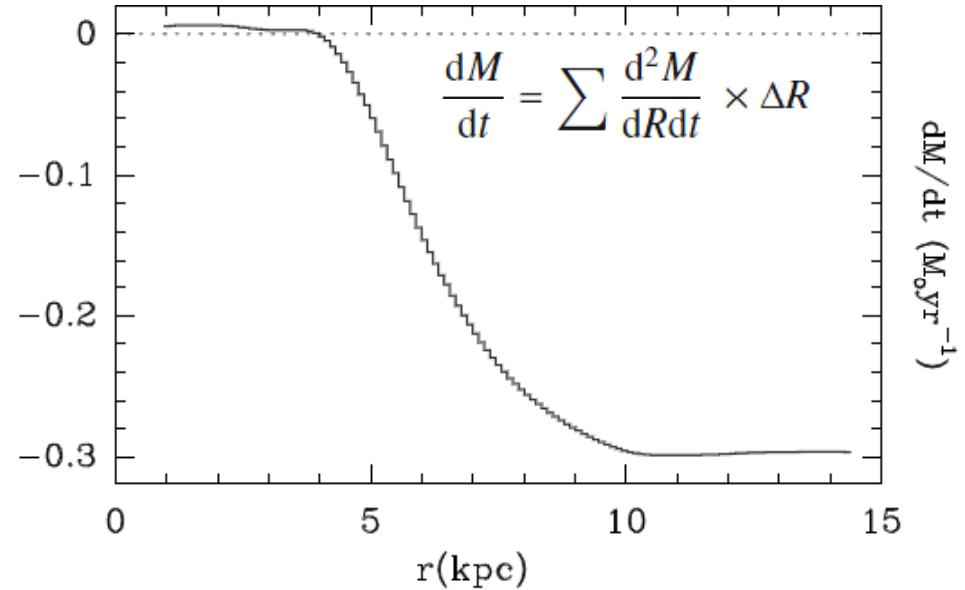
# Gravitational Torque Analysis

NGC4579 from HI gas obs.  
(García-Burillo et al. 2009)

$$t(R) = \frac{\int_{\theta} N(x, y) \times (x F_y - y F_x)}{\int_{\theta} N(x, y)}$$

$$\frac{\Delta L}{L} = \frac{dL}{dt} \Big|_{\theta} \times \frac{1}{L} \Big|_{\theta} \times T_{\text{rot}} = \frac{t(R)}{L_{\theta}} \times T_{\text{rot}}$$

$$\frac{d^2 M}{dR dt} = \frac{dL}{dt} \Big|_{\theta} \times \frac{1}{L} \Big|_{\theta} \times 2\pi R \times N(x, y) \Big|_{\theta}$$



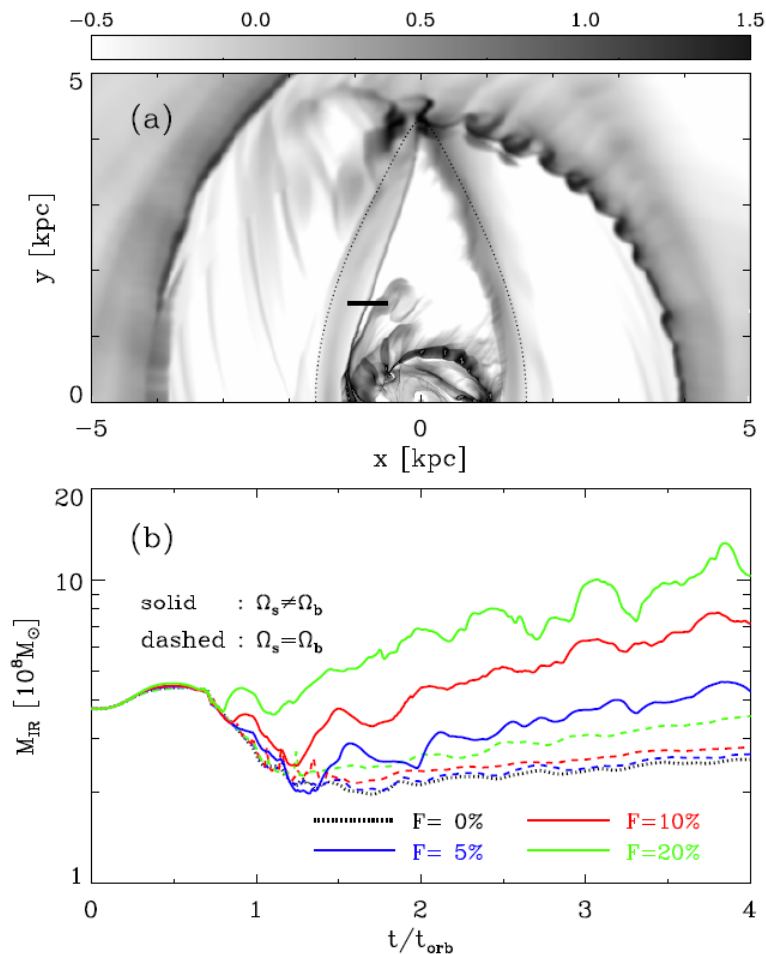
Haan et al. (2009)

**Table 9**  
Gravitational Torque Analysis

Source	$\langle dL/L \rangle$		$\langle  dL/L  \rangle$		$dM_{\text{HI}}/dt$ ( $M_{\odot} \text{ yr}^{-1}$ )	$dM_{\text{mol}}/dt$ ( $M_{\odot} \text{ yr}^{-1}$ )	$R_{\text{max, HI}}$ (kpc)	$R_{\text{max, CO}}$ (kpc)
	H I	CO	H I	CO				
NGC 3368	0.02	-0.50	0.12	0.55	0.04	-11.11	13.0	0.35
NGC 3627	-0.00	0.16	0.26	0.24	-0.10	50.13	6.0	0.75
NGC 4321	0.01	0.02	0.10	0.10	-0.18	1.03	18.0	1.2
NGC 4736	0.02	0.01	0.03	0.09	0.06	-0.01	8.5	0.62
NGC 5248	0.06	-0.02	0.13	0.02	0.49	-22.96	20.5	0.8
NGC 6951	-0.04	-0.05	0.09	0.10	-0.16	-4.29	29.0	1.0
NGC 7217	-0.01	-0.02	0.03	0.03	-0.01	-2.37	15.2	1.4

# Inner Ring Mass

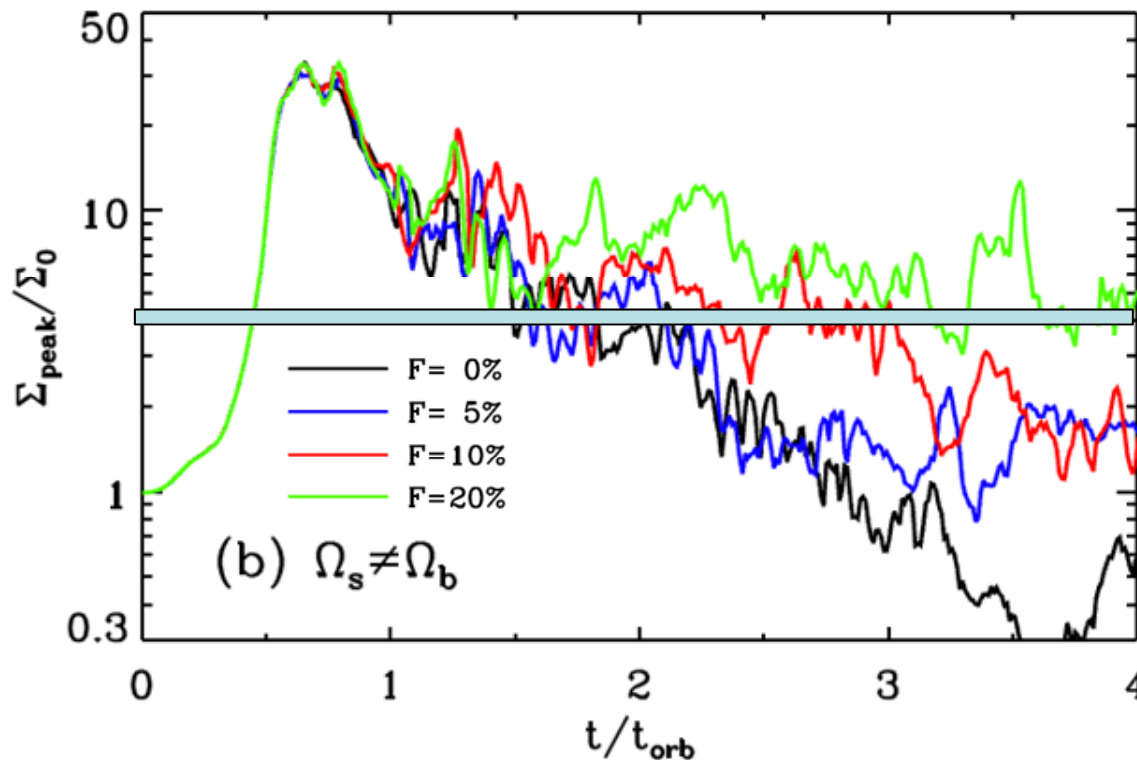
- The inflowing gas due to spiral arms in the DF models can move across the outermost  $x_1$ -orbit and secularly increases the gas mass in the bar region.



- About 15% of the total inflowing gas encircles the bar region outside the outermost  $x_1$ -orbit.
- About 60% is used to increase the gas mass in the inner ring.

# Dust Lane Strength

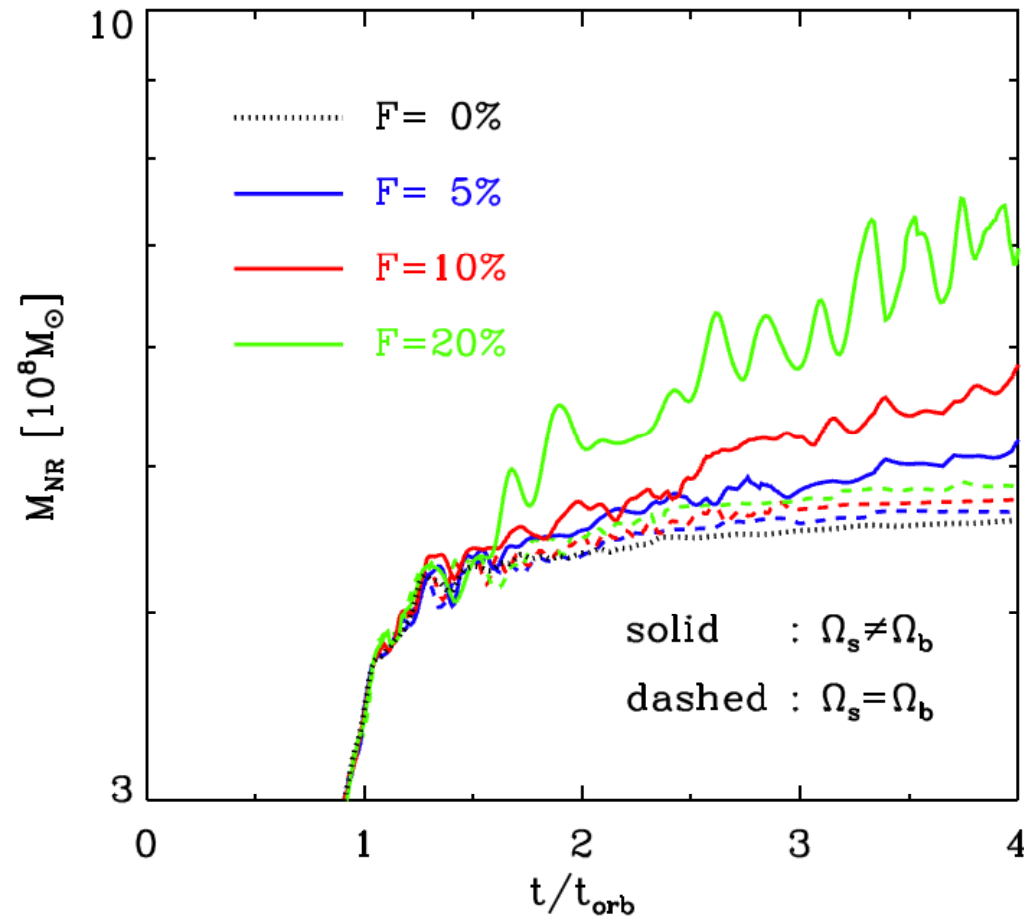
- About 5% of the inflowing gas goes to the dust lanes.
- For  $\mathcal{F}=10\%$ , dust lanes can be readily visible for a long period of time against background stellar radiation.



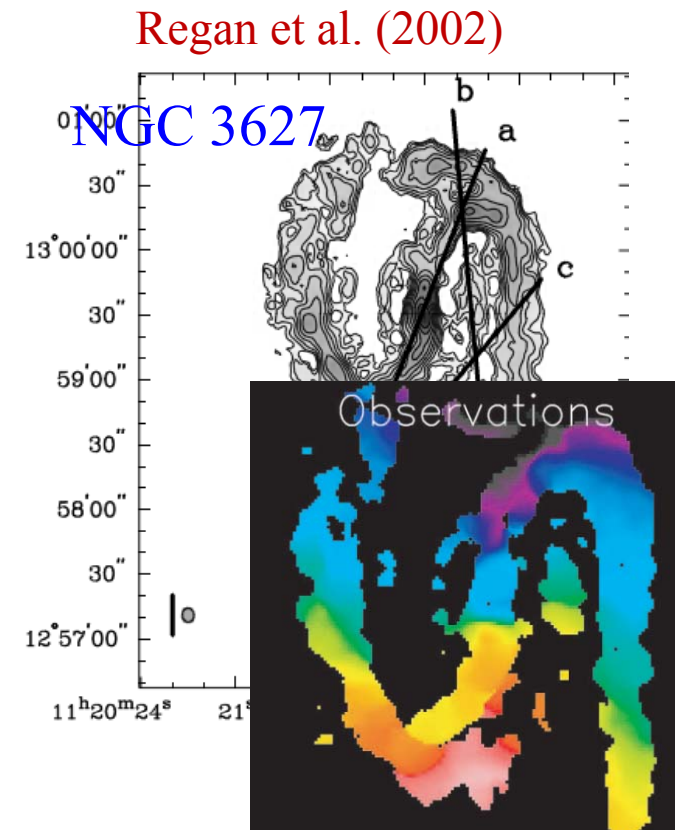
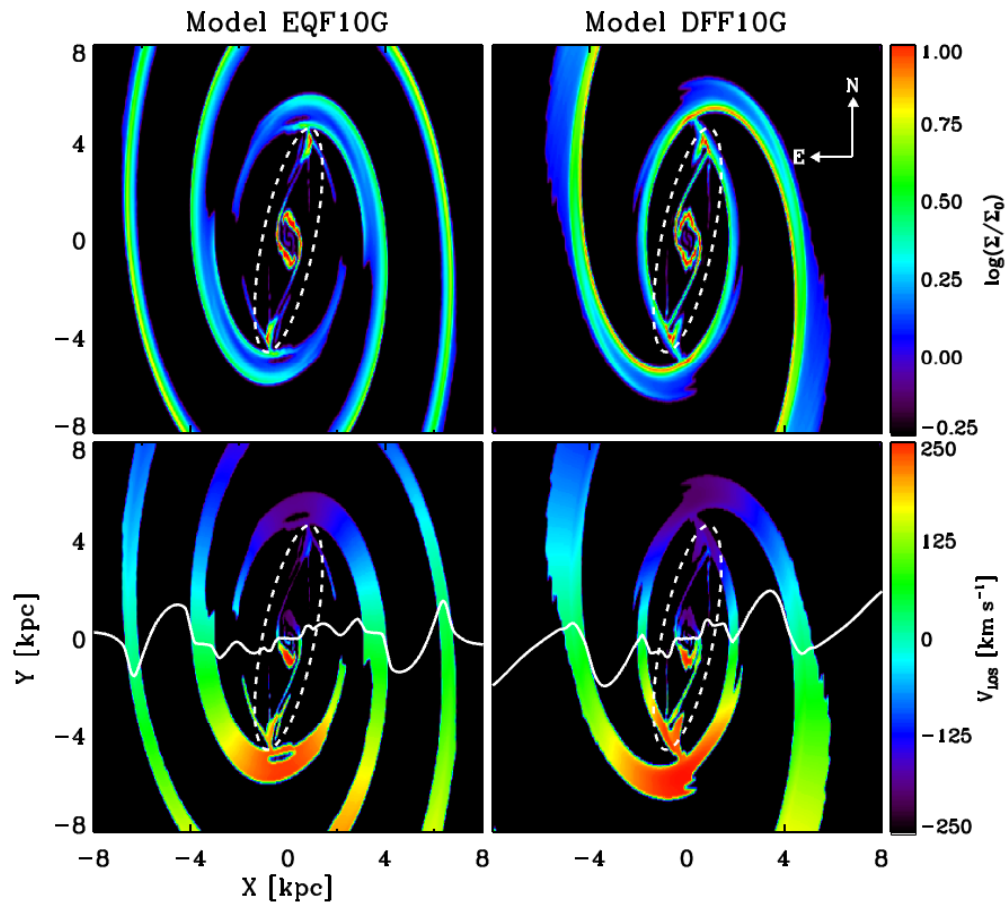
$A_V=3$  for  $\Sigma_0=10 M_\odot \text{ pc}^{-2}$

# Nuclear Ring Mass

- About 20% ( $\sim 0.3 M_{\odot} \text{ yr}^{-1}$  when  $\mathcal{F}=10\%$ ) of the inflowing gas goes to the nuclear ring.



# Kinematic Differences in DF and EQ models



$$\Omega_b = 50 \text{ km s}^{-1} \text{ kpc}^{-1}$$

$$\Omega_s = 23 \text{ km s}^{-1} \text{ kpc}^{-1}$$

(Rand & Wallin 2004)

- Gaseous arms are more loosely wound in DF models.
- The arms have larger density at smaller  $R$  in DF models.
- Due to streaming motions, the zero velocity curve near the western (eastern) arms strongly bends downward (upward) in DF models.

# Summary

- Bar Regions
  - Gaseous bar substructures readily form via interaction with a non-axisymmetric bar potential.
  - Dust lanes are **more straight** in more strongly barred galaxies
  - Nuclear rings form **not by resonances** but by the centrifugal barrier that the inflowing gas cannot overcome.
- Spiral-arm regions
  - Spiral arms are efficient to drive radial mass inflows at the level  $\sim 0.5\text{--}2.5M_{\odot} \text{ yr}^{-1}$ , **provided the arm pattern speed is much smaller than that of the bar**, enhancing the strength of bar substructures.
  - The extent of spiral shocks is limited by too large  $\mathcal{M}_{\perp}$  in EQ models.
  - The arm pitch angle of gaseous arms is in general **smaller** than that of the stellar arms.